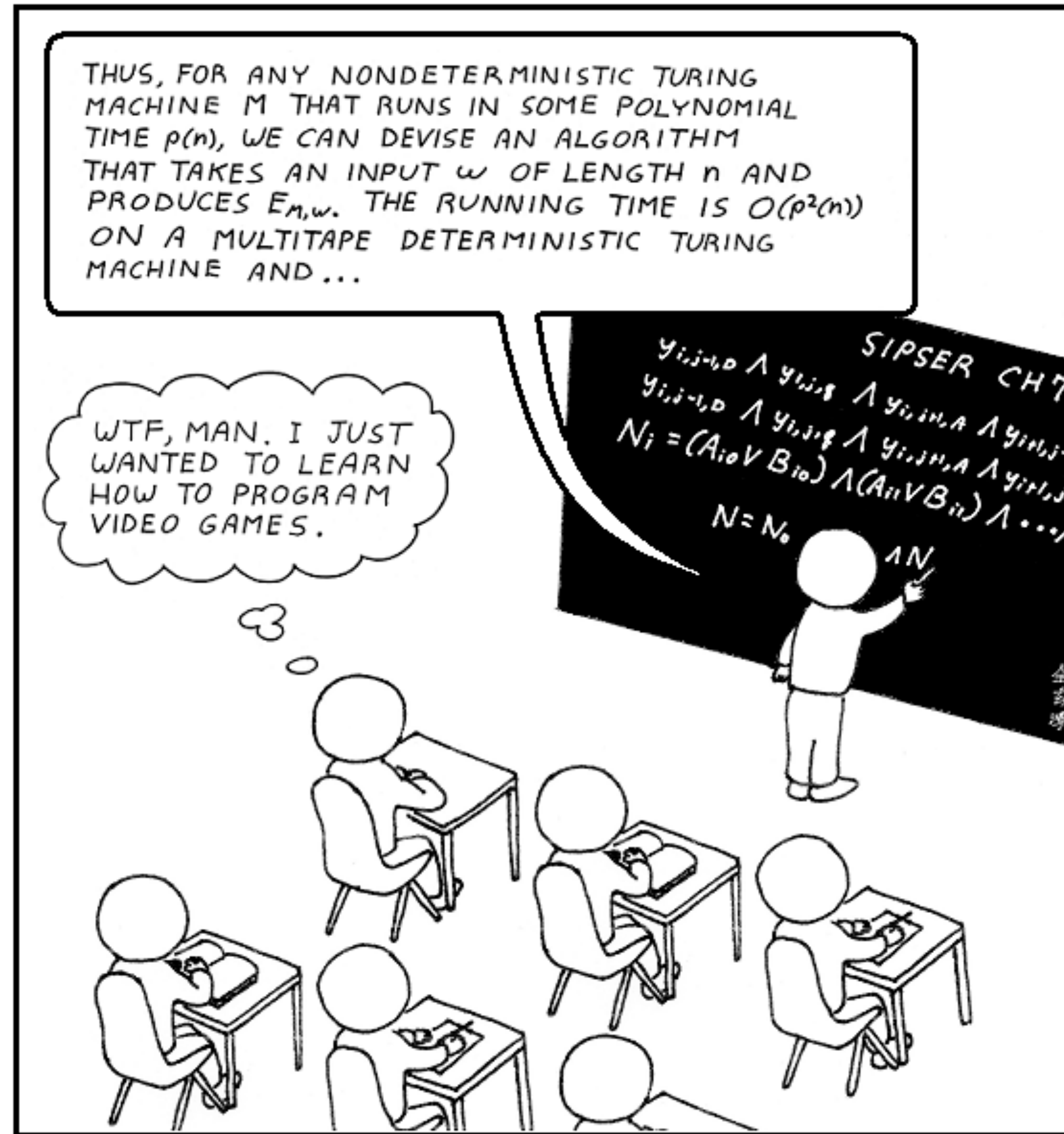


# Computational Approaches to Biological Challenges (algorithmic primer)

Shortest Common Superstring & Lander-  
Waterman Statistics

# What is Computer Science?



# What is Computer Science?

Not actually simple to define constructively

Still debate whether certain areas constitute CS

Computer science is the scientific and practical approach to computation and its applications. It is the systematic study of the feasibility, structure, expression, and mechanization of the methodical procedures (or algorithms) that underlie the acquisition, representation, processing, storage, communication of, and access to information\* ...

\*<http://www.cs.bu.edu/AboutCS/WhatIsCS.pdf>

# What is Computer Science?

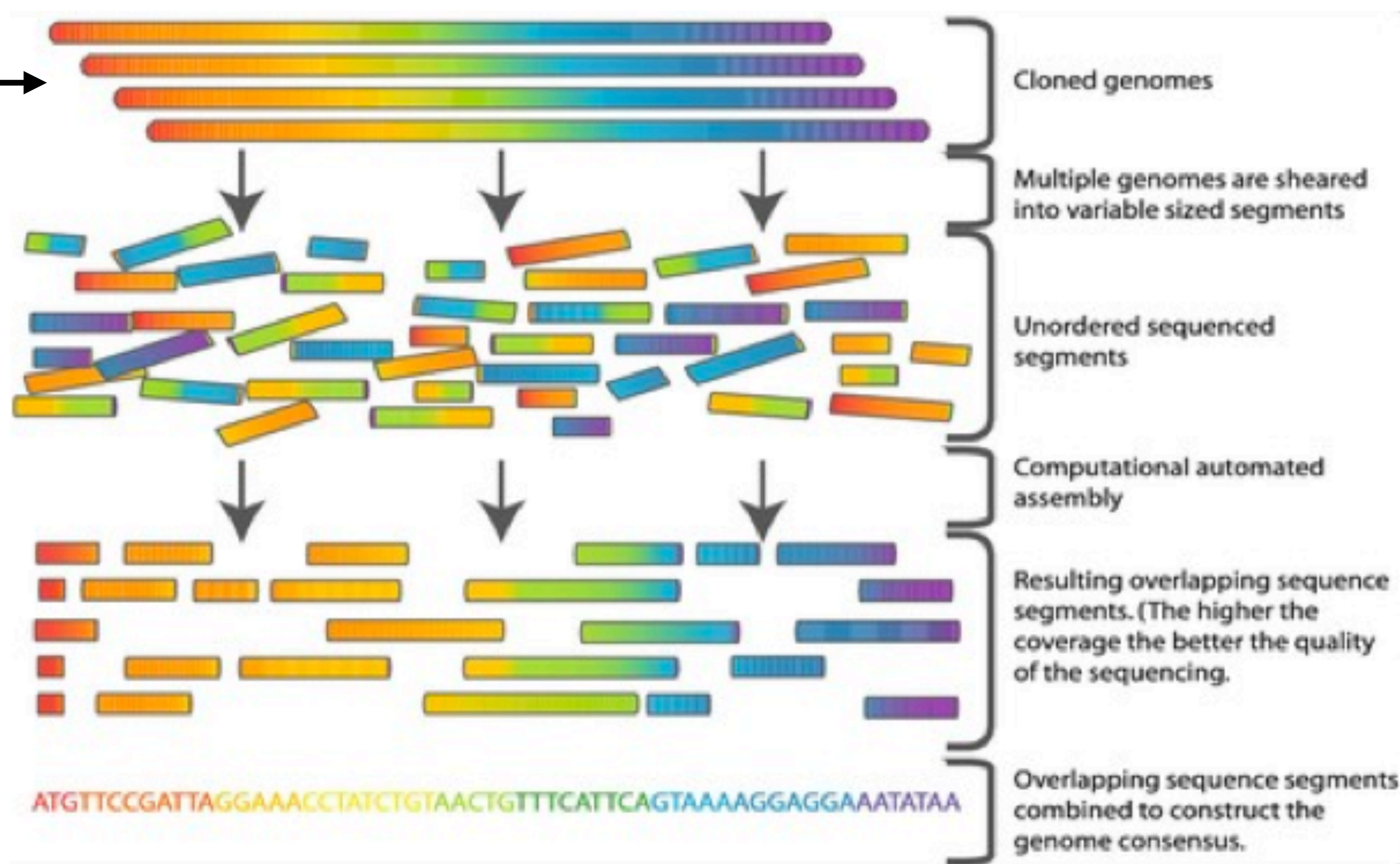
Concerned with the development of provably **correct** and **efficient** computational procedures (algorithms & data structures) to answer **well-specified** problems.

To answer a computational question, we first need a well-formulated problem.

It turns out that a **major challenge** in bioinformatics will simply be determining how to frame the *computational problem* corresponding to a *biological question* in a well-posed and meaningful way!

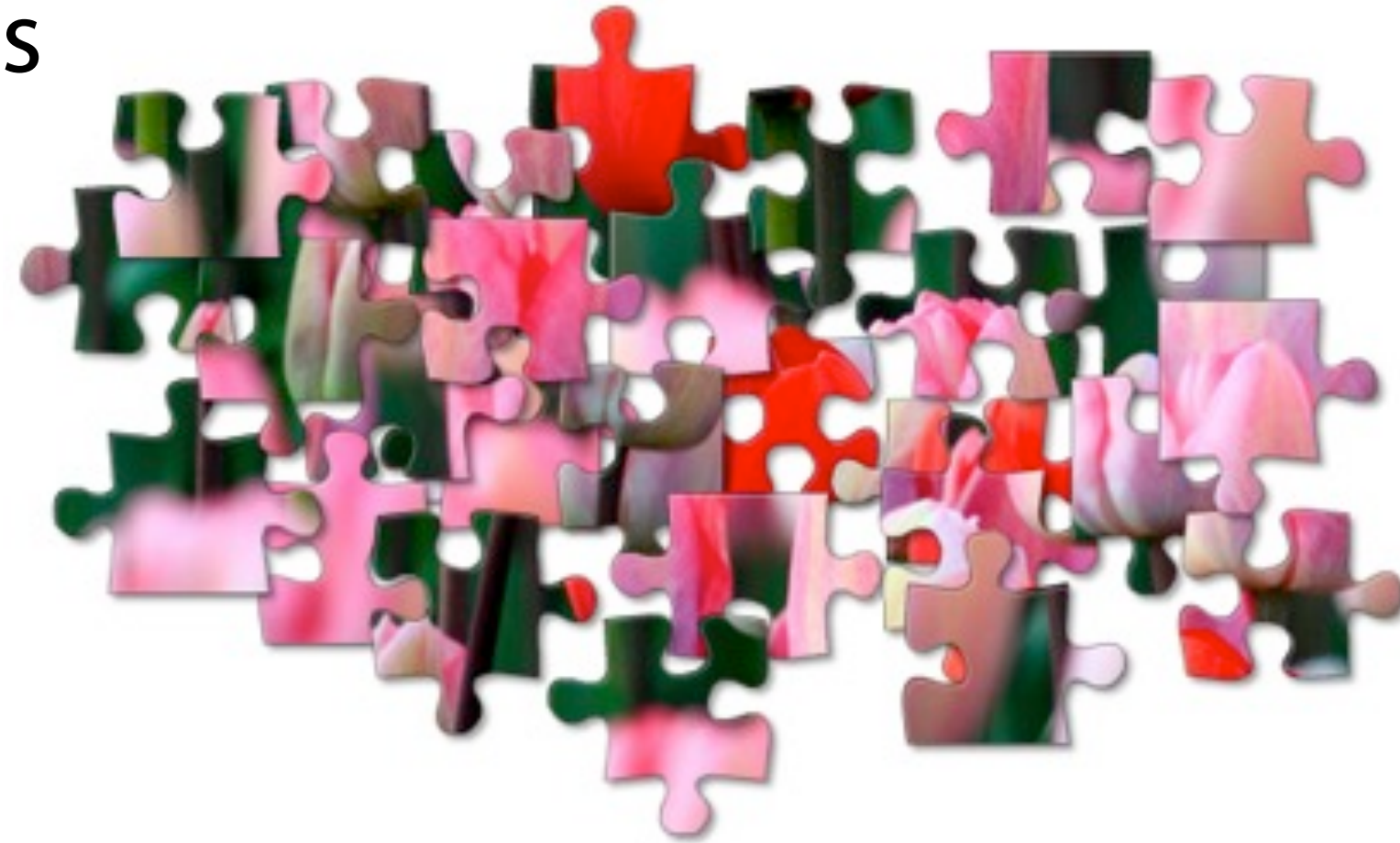
# What is genome assembly: intuitively?

Why start with many cloned genomes and not just one? →



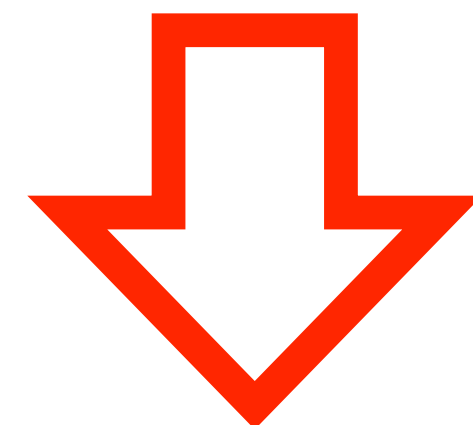
# Assembly

Reads



+

Reference genome



Input DNA



How to assemble puzzle without the benefit of knowing what the finished product looks like?

# Assembly

Whole-genome “shotgun” sequencing starts by copying and fragmenting the DNA

(“Shotgun” refers to the random fragmentation of the whole genome; like it was fired from a shotgun)

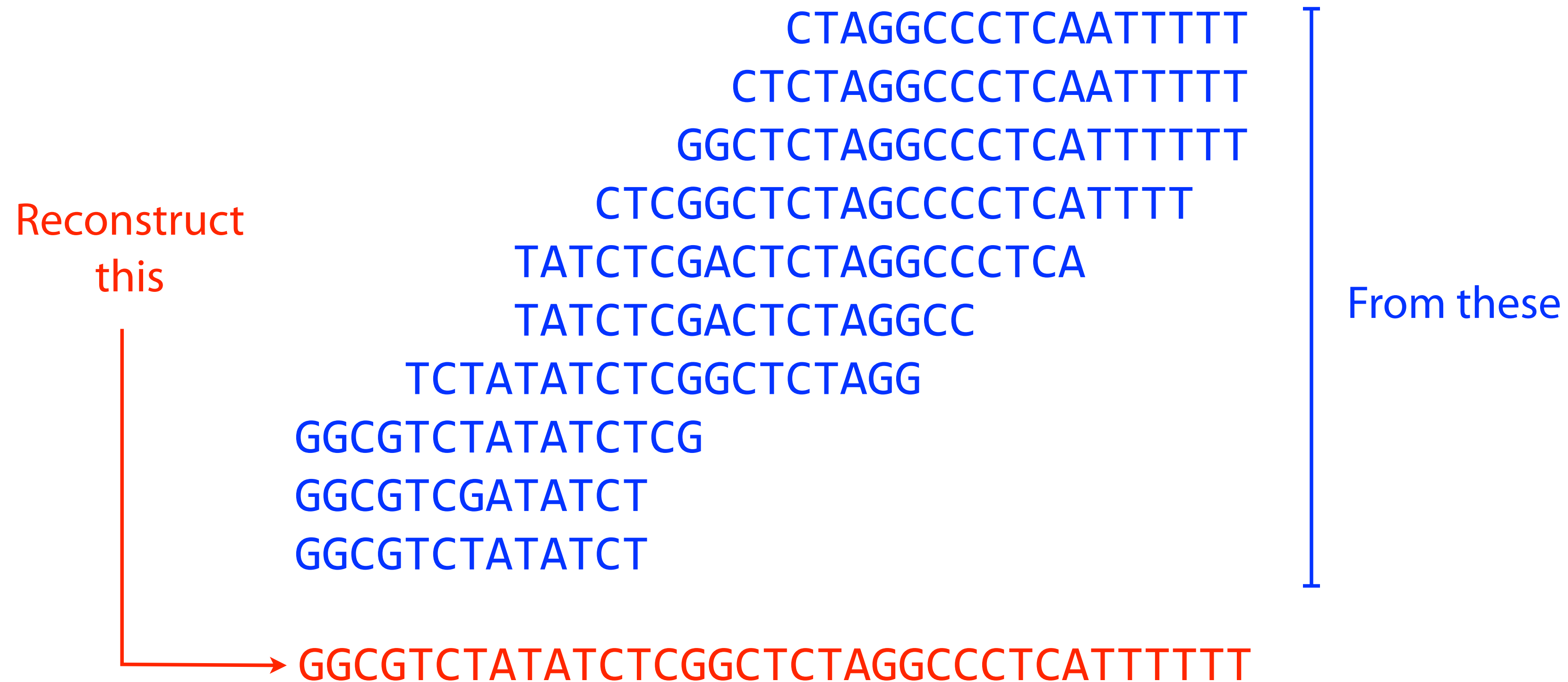
Input: GCGTCTATATCTCGGCTCTAGGCCCTCATTTTTTT

Copy: GCGTCTATATCTCGGCTCTAGGCCCTCATTTTTTT  
GCGTCTATATCTCGGCTCTAGGCCCTCATTTTTTT  
GCGTCTATATCTCGGCTCTAGGCCCTCATTTTTTT  
GCGTCTATATCTCGGCTCTAGGCCCTCATTTTTTT

Fragment: GCGTCTA TATCTCGG CTCTAGGCCCTC ATTTTTT  
GGC GTCTATAT CTCGGCTCTAGGCCCTCA TTTTTT  
GCGTC TATATCT CGGCTCTAGGCCCT CATTTTTTT  
GCGTCTAT ATCTCGGCTCTAG GCCCTCA TTTTTT

# Assembly

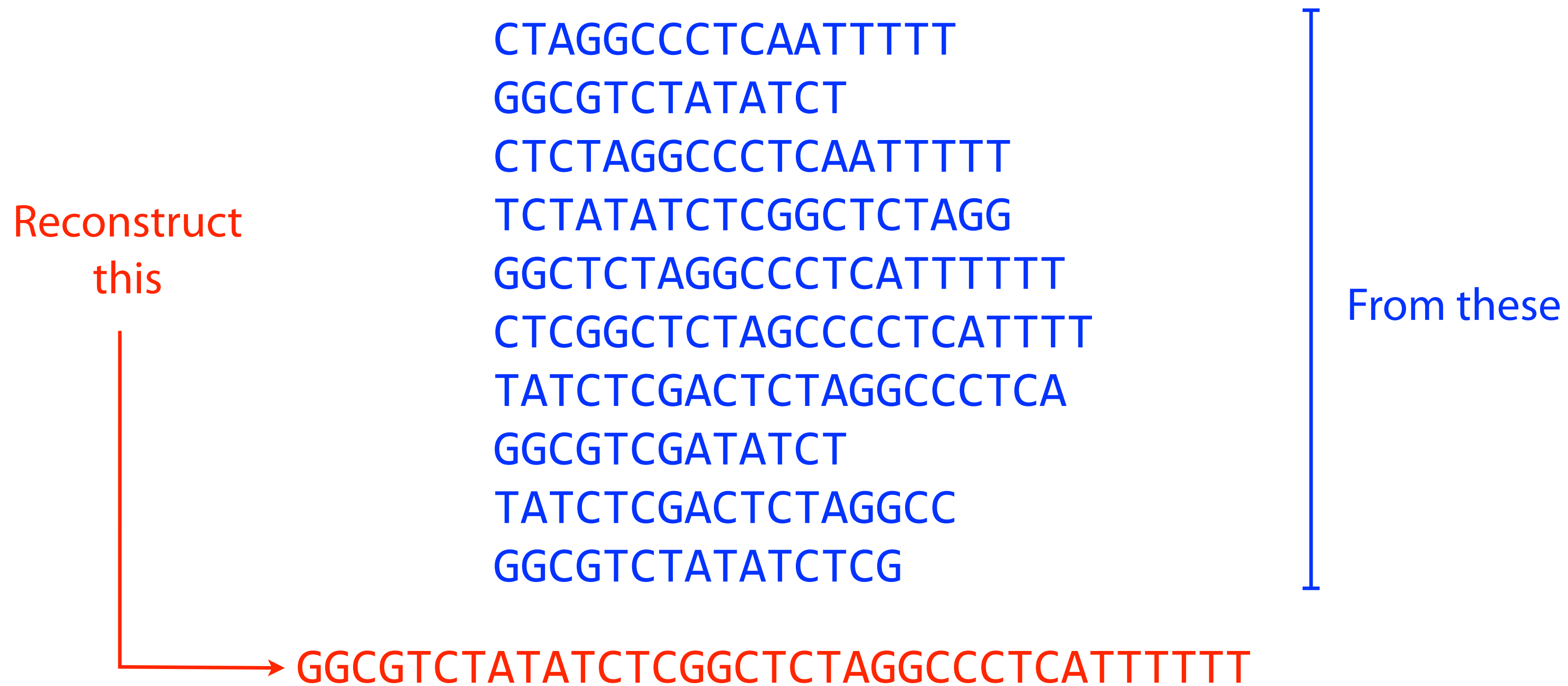
Assume sequencing produces such a large # fragments that almost all genome positions are *covered* by many fragments...



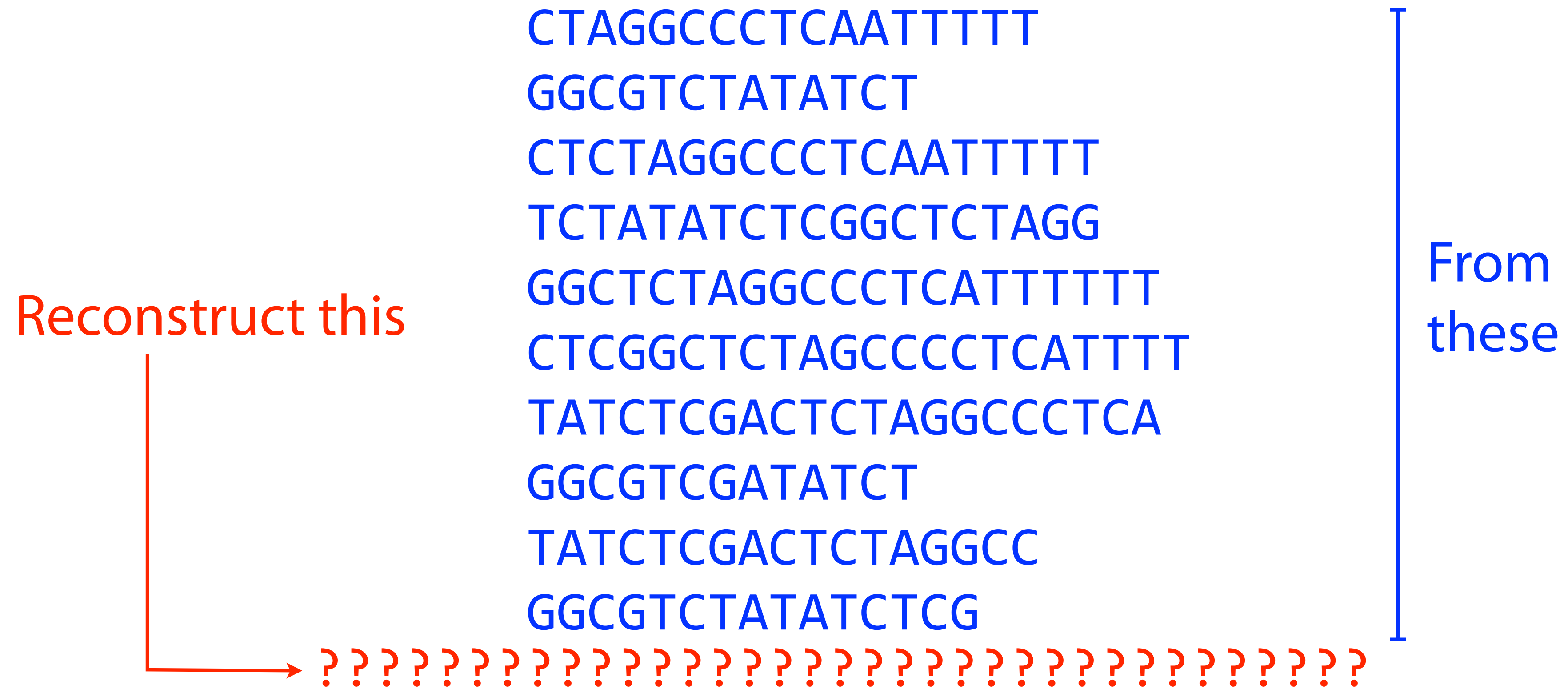


# Assembly

...but we don't know what came from where



# Assembly



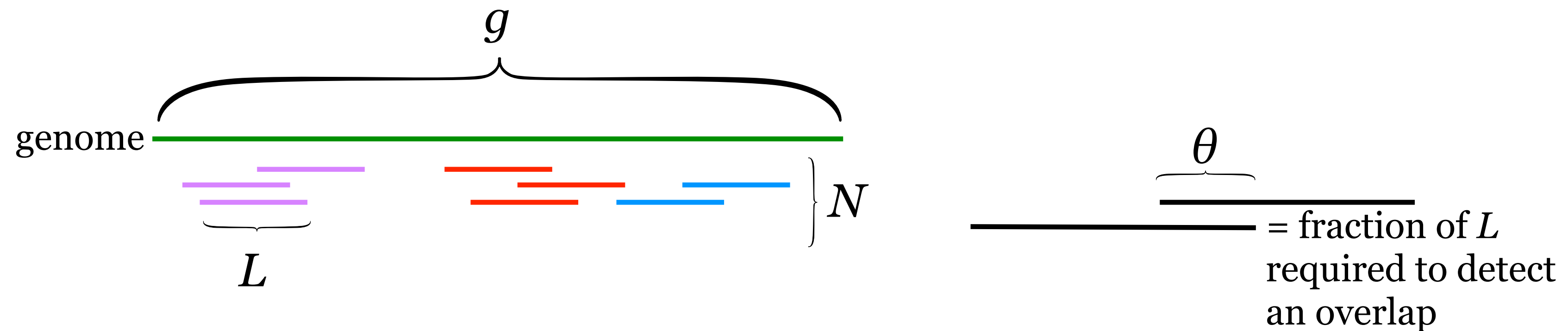
In general: we don't even know exactly how *long* the original string was!

# Aside: How Much Coverage is Enough?

## Lander-Waterman Statistics

Lander ES, Waterman MS (1988). "Genomic mapping by fingerprinting random clones: a mathematical analysis". *Genomics* 2 (3): 231–239

How many reads do we need to be sure we cover the whole genome?



An **island** is a contiguous group of reads that are connected by overlaps of length  $\geq \theta L$ .  
(Various colors above)

Want: Expression for expected # of islands given  $N, g, L, \theta$ .

# Expected # of Islands

$\lambda := N/g$  = probability a read starts at a given position  
(assuming random sampling)

Pr( $k$  reads start in an interval of length  $x$ )

$x$  trials, want  $k$  “successes”, small probability  $\lambda$  of success

Expected # of successes =  $\lambda x$

Poisson approximation to binomial distribution:

$$\text{Pr}(k \text{ reads in length } x) = e^{-\lambda x} \frac{(\lambda x)^k}{k!}$$

Expected # of islands =  $N \times \text{Pr}(\text{read is at rightmost end of island})$

$$\begin{aligned} \underbrace{\quad \quad \quad}_{(1-\theta)L} \quad \theta L &= N \times \text{Pr}(0 \text{ reads start in } (1-\theta)L) \\ &= N e^{-\lambda(1-\theta)L} \frac{\lambda^0}{0!} \quad (\text{from above}) \\ &= N e^{-\lambda(1-\theta)L} \\ &= N e^{-(1-\theta)LN/g} \quad \leftarrow LN/g \text{ is called the } \mathbf{coverage} \mathbf{ } c. \end{aligned}$$

## Expected # of Islands, 2

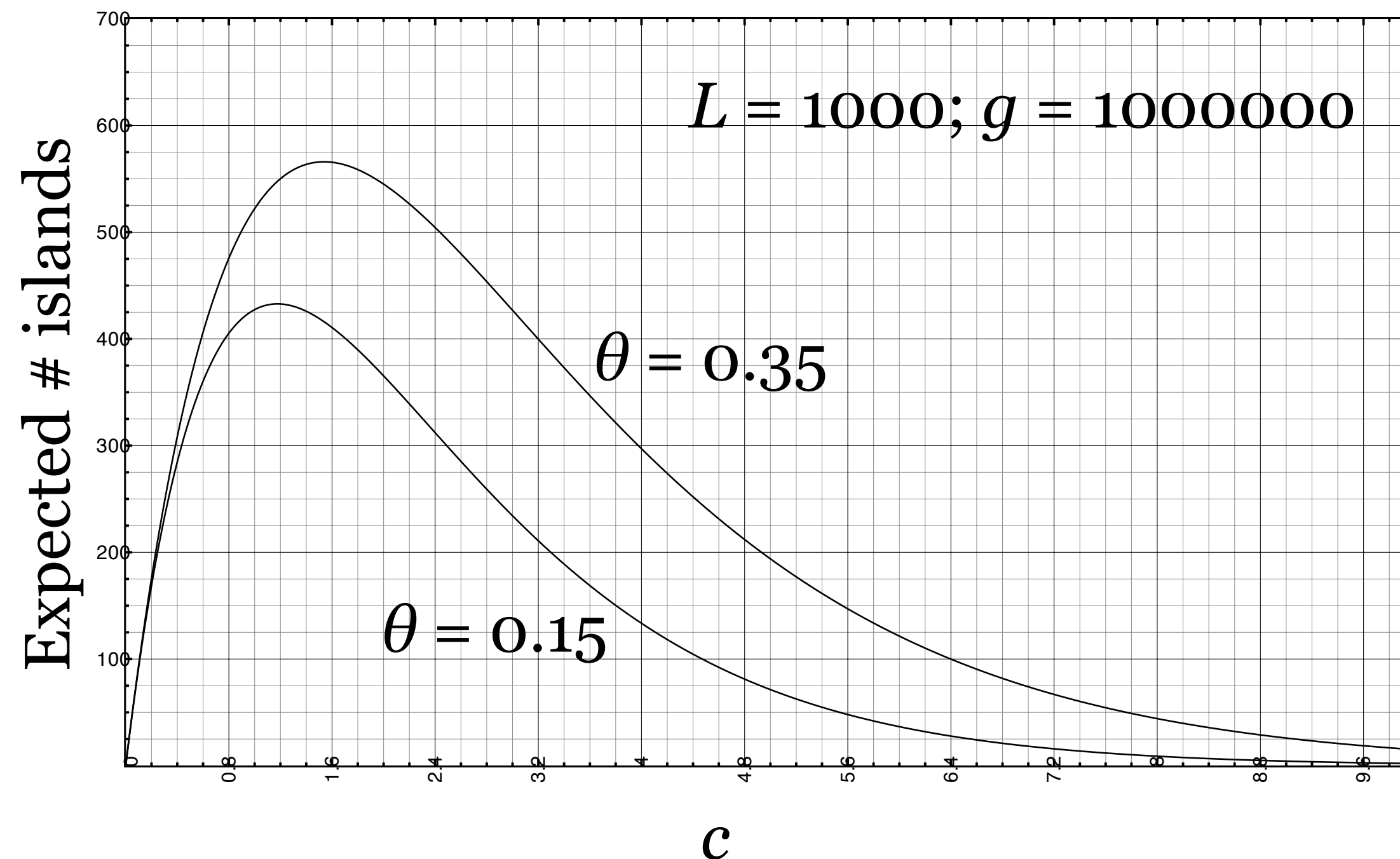
We can rewrite this expression to depend more directly on the things we can control:  $c$  and  $\theta$

$$\text{Expected \# of islands} = N e^{-(1-\theta)LN/g}$$

$$= N e^{-(1-\theta)c}$$

$$= \frac{L/g}{L/g} N e^{-(1-\theta)c}$$

$$= \frac{g}{L} c e^{-(1-\theta)c}$$



# What is Computer Science?

Concerned with the development of provably **correct** and **efficient** computational procedures (algorithms & data structures) to answer **well-specified** problems.

To answer a computational question, we first need a well-formulated problem.

**Given:** a collection,  $R$ , of sequencing reads (strings)

**Find:** The genome (string),  $G$ , that generated them

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~~**Given:** a collection,  $R$ , of sequencing reads (strings)~~

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**Not** well-specified.

What makes one genome more likely than another?

What constraints do we place on the space of solutions?

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To answer a computational question, we first need a well-formulated problem.

**Given:** a collection,  $R$ , of sequencing reads (strings)

**Find:** The shortest genome (string),  $G$ , that contains all of them





# Shortest Common Superstring

**Given:** a collection,  $S = \{s_1, s_2, \dots, s_k\}$ , of sequencing reads (strings)

**Find\*:** The shortest possible genome (string),  $G$ , such that  $s_1, s_2, \dots, s_k$  are all substrings of  $G$

**How**, might we go about solving this problem?

\*for reasons we'll explore later, this isn't actually a great formulation for genome assembly.

# Shortest common superstring

Given a collection of strings  $S$ , find  $SCS(S)$ : the shortest string that contains all strings in  $S$  as substrings

Without requirement of "shortest," it's easy: just concatenate them

Example:  $S$ : BAA AAB BBA ABA ABB BBB AAA BAB

Concatenation: BAAAABBBBAABAABBBBBBAAABAB  
└────────────────── 24 ─────────────────┘

$SCS(S)$ : AAABBBBABAA  
└── 10 ─┘

AAA  
AAB  
ABB  
BBB  
BBA  
BAB  
ABA  
BAA

Idea: pick order for strings in  $S$  and construct superstring

order 1: AAA AAB ABA ABB BAA BAB BBA BBB  
AAA

Idea: pick order for strings in  $S$  and construct superstring

order 1: AAA AAB ABA ABB BAA BAB BBA BBB  
AAAB

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*order 1:* AAA AAB ABA ABB BAA BAB BBA BBB  
AAABABB

Idea: pick order for strings in  $S$  and construct superstring

*order 1:* AAA AAB ABA ABB BAA BAB BBA BBB

AAABABBAABABBABBB ← superstring 1

Idea: pick order for strings in  $S$  and construct superstring

*order 1:* AAA AAB ABA ABB BAA BAB BBA BBB

AAABABBAABABBABB ← superstring 1

*order 2:* AAA AAB ABA BAB ABB BBB BAA BBA

AAABABBBBAABBA ← superstring 2

Try all possible orderings and pick shortest superstring

If  $S$  contains  $n$  strings,  $n!$  ( $n$  factorial) orderings possible



*order 1:* AAA AAB ABA ABB BAA BAB BBA BBB

AAABABBAABABBABB ← superstring 1

*order 2:* AAA AAB ABA BAB ABB BBB BAA BBA

AAABABBBBAABBA ← superstring 2

If  $S$  contains  $n$  strings,  $n!$  ( $n$  factorial) orderings possible

# Shortest common superstring

Can we solve it?

Imagine a modified overlap graph where each edge has cost = - (length of overlap)

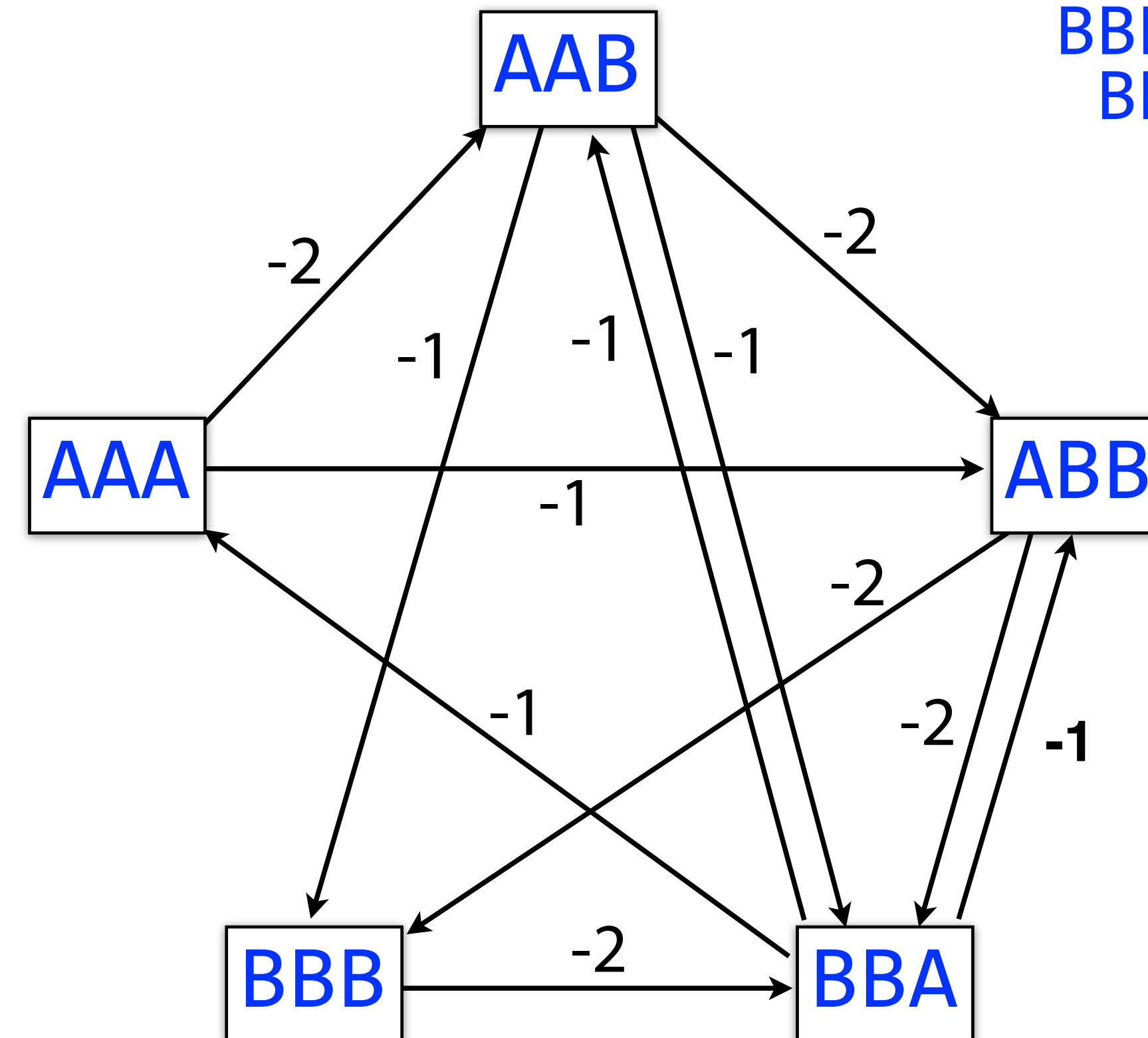
SCS corresponds to a path that visits every node once, minimizing total cost along path

That's the *Traveling Salesman Problem (TSP)*, which is NP-hard!

S: AAA AAB ABB BBB BBA

SCS(S): AAABBBBA

AAA  
AAB  
ABB  
BBB  
BBA



# Shortest common superstring

Say we disregard edge weights and just look for a path that visits all the nodes exactly once

That's the *Hamiltonian Path* problem: NP-complete

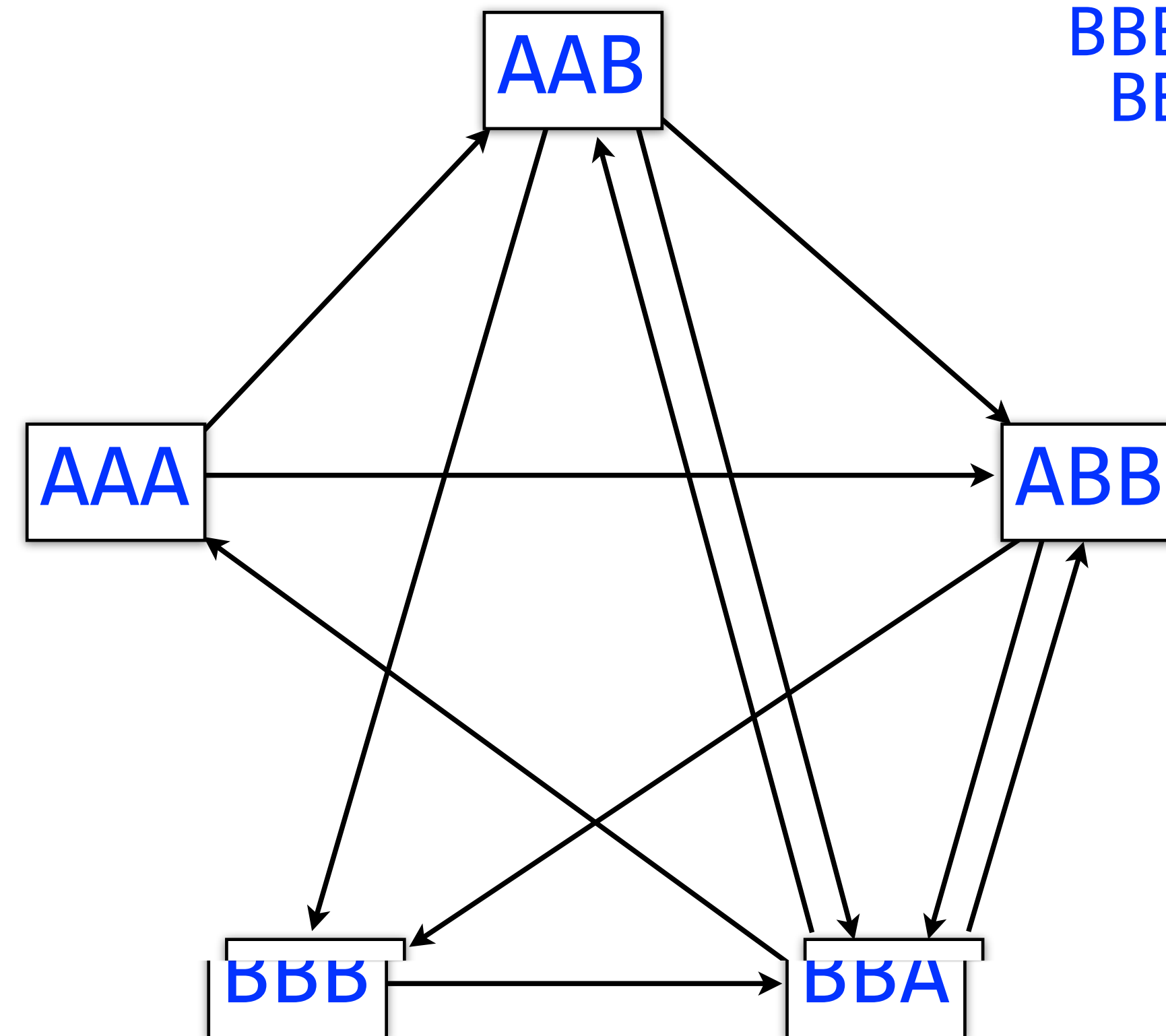
So, it's not even the weights that make visiting all nodes once hard

Indeed, it's well established that SCS is NP-hard

S: AAA AAB ABB BBB BBA

SCS(S): AAABBBA

AAA  
AAB  
ABB  
BBB  
BBA



# Shortest common superstring & friends

Traveling Salesman, Hamiltonian Path, and Shortest Common Superstring are all NP-hard

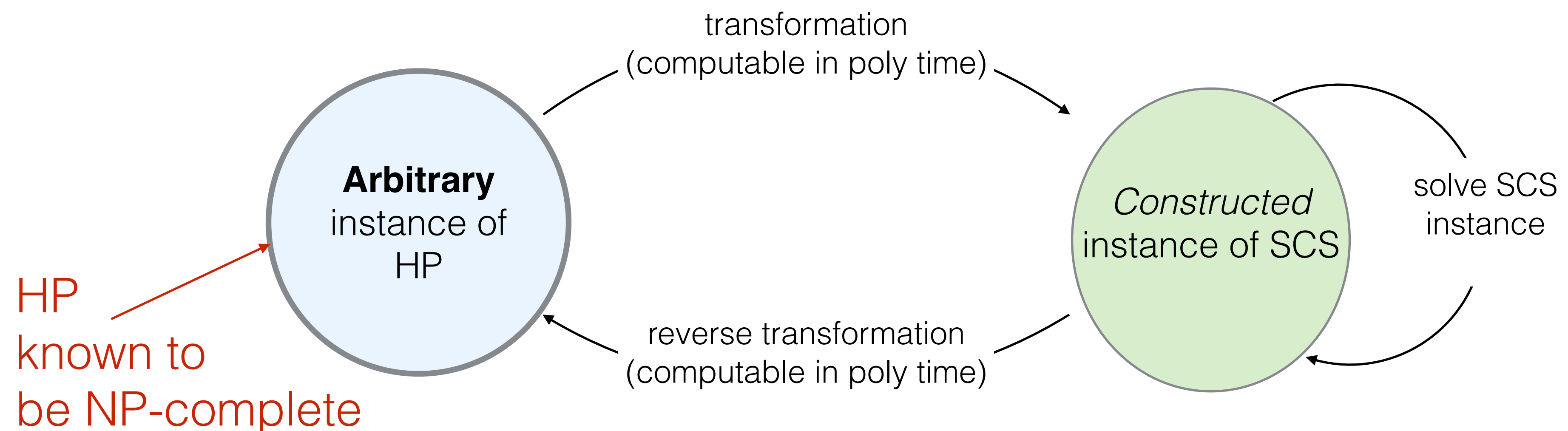
For refreshers on Traveling Salesman, Hamiltonian Path, NP-hardness and NP-completeness, see Chapters 34 and 35 of "Introduction to Algorithms" by Cormen, Leiserson, Rivest and Stein, or Chapters 8 and 9 of "Algorithms" by Dasgupta, Papadimitriou and Vazirani (free online: <http://www.cs.berkeley.edu/~vazirani/algorithms>)

Who remembers reductions from 351?

**Important note:** The fact that we modeled SCS as NP-hard problems (TSP and HP) **does not** prove that (the decision version of) SCS is NP-complete. To do that, we must **reduce** a known NP-complete problem to **SCS**.

**Given** an instance  $I$  of a known hard problem, **generate** an instance  $I'$  of SCS such that if we can solve  $I'$  in polynomial time, then we can solve  $I$  in polynomial time. This *implies* that SCS is *at least* as hard as the hard problem.

This can be done e.g. with HAMILTONIAN PATH



# Shortest Common Superstring

The fact that (the decision version of) SCS is **NP-complete** means that it is unlikely that there exists *any* algorithm that can solve a general instance of this problem in time polynomial in  $n$  — the number of input strings (i.e. reads in the case of genome assembly).

If we give up on finding a *shortest* possible superstring  $G$ , and instead look for one that's “near-shortest”, how does the situation change?

# Shortest Common Superstring

There's a "greedy" *heuristic* that turns out to be an *approximation algorithm* (provides a solution within a constant factor of the optimum)

At *each step*, chose the *pair of strings* with the *maximum overlap*, merge them, and return the merged string to the collection.

*Greedy conjecture* factor of 2-OPT *is* the worst case

*Open conjecture!* We can prove 3.5, but many believe the factor is actually 2.

Different approx. (**not all greedy**)

ratio	authors	year
approximating SCS		
3	Blum, Jiang, Li, Tromp and Yannakakis [4]	1991
$2\frac{8}{9}$	Teng, Yao [23]	1993
$2\frac{5}{6}$	Czumaj, Gasieniec, Piotrow, Rytter [8]	1994
$2\frac{50}{63}$	Kosaraju, Park, Stein [15]	1994
$2\frac{3}{4}$	Armen, Stein [1]	1994
$2\frac{50}{69}$	Armen, Stein [2]	1995
$2\frac{2}{3}$	Armen, Stein [3]	1996
$2\frac{25}{42}$	Breslauer, Jiang, Jiang [5]	1997
$2\frac{1}{2}$	Sweedyk [21]	1999
$2\frac{1}{2}$	Kaplan, Lewenstein, Shafrir, Sviridenko [12]	2005
$2\frac{1}{2}$	Paluch, Elbassioni, van Zuylen [18]	2012
$2\frac{11}{23}$	Mucha [16]	2013

# Shortest common superstring: greedy

Greedy-SCS: in each round, merge pair of strings with maximal overlap.  
Stop when no more overlaps exist. Concatenate resulting strings.  $l =$   
minimum overlap.

Algorithm in action ( $l = 1$ ):



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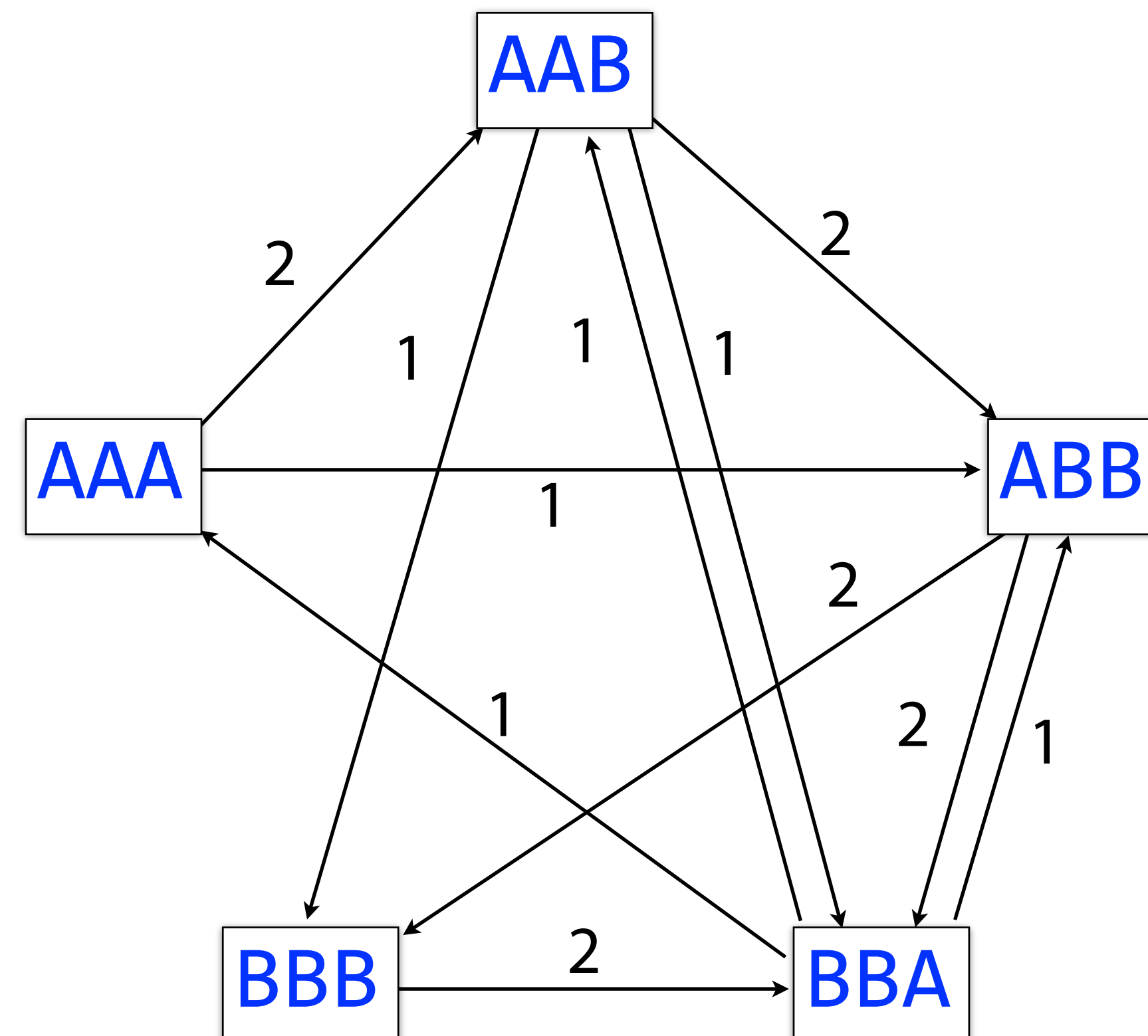
┌─── Input strings ──┐  
AAA AAB ABB BBB BBA

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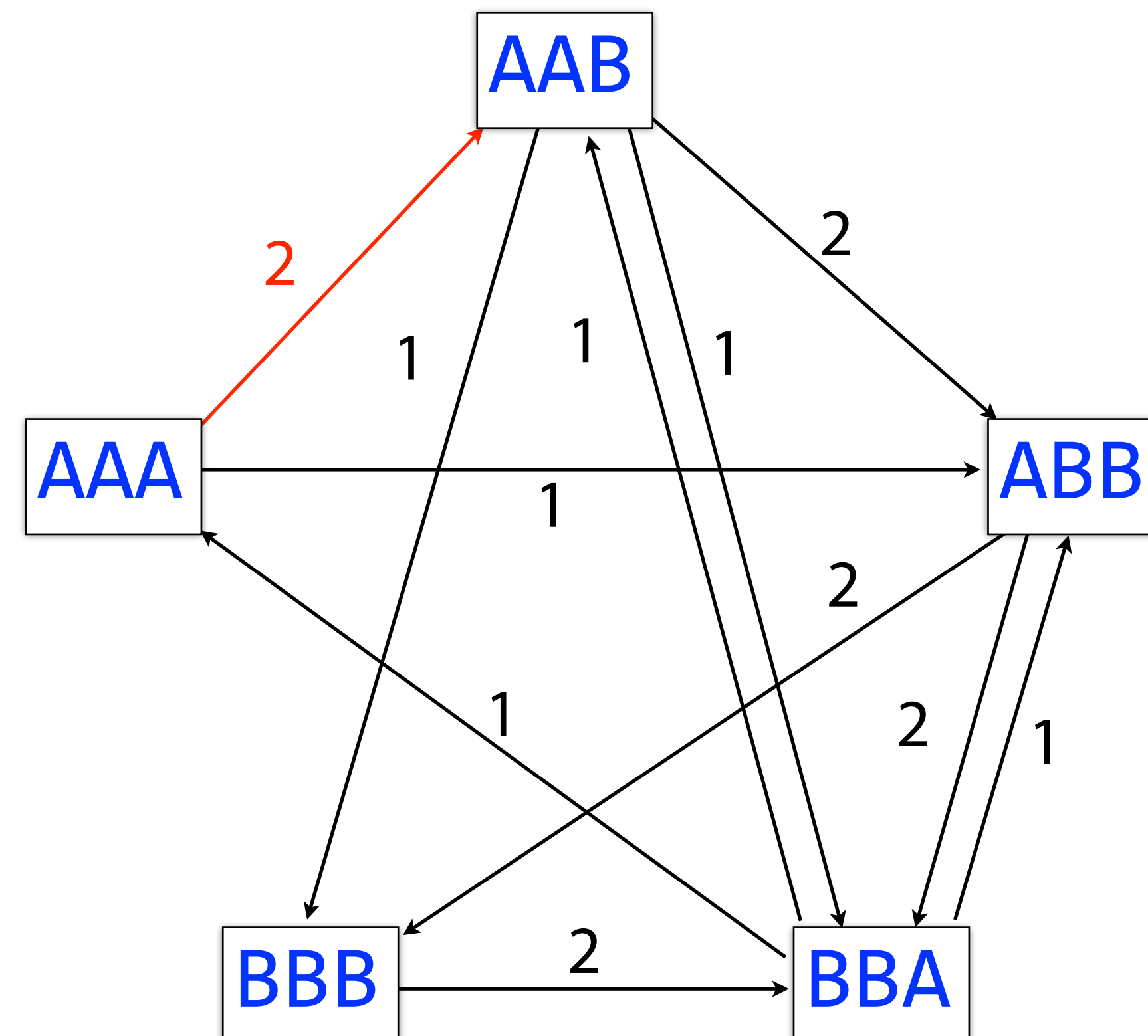


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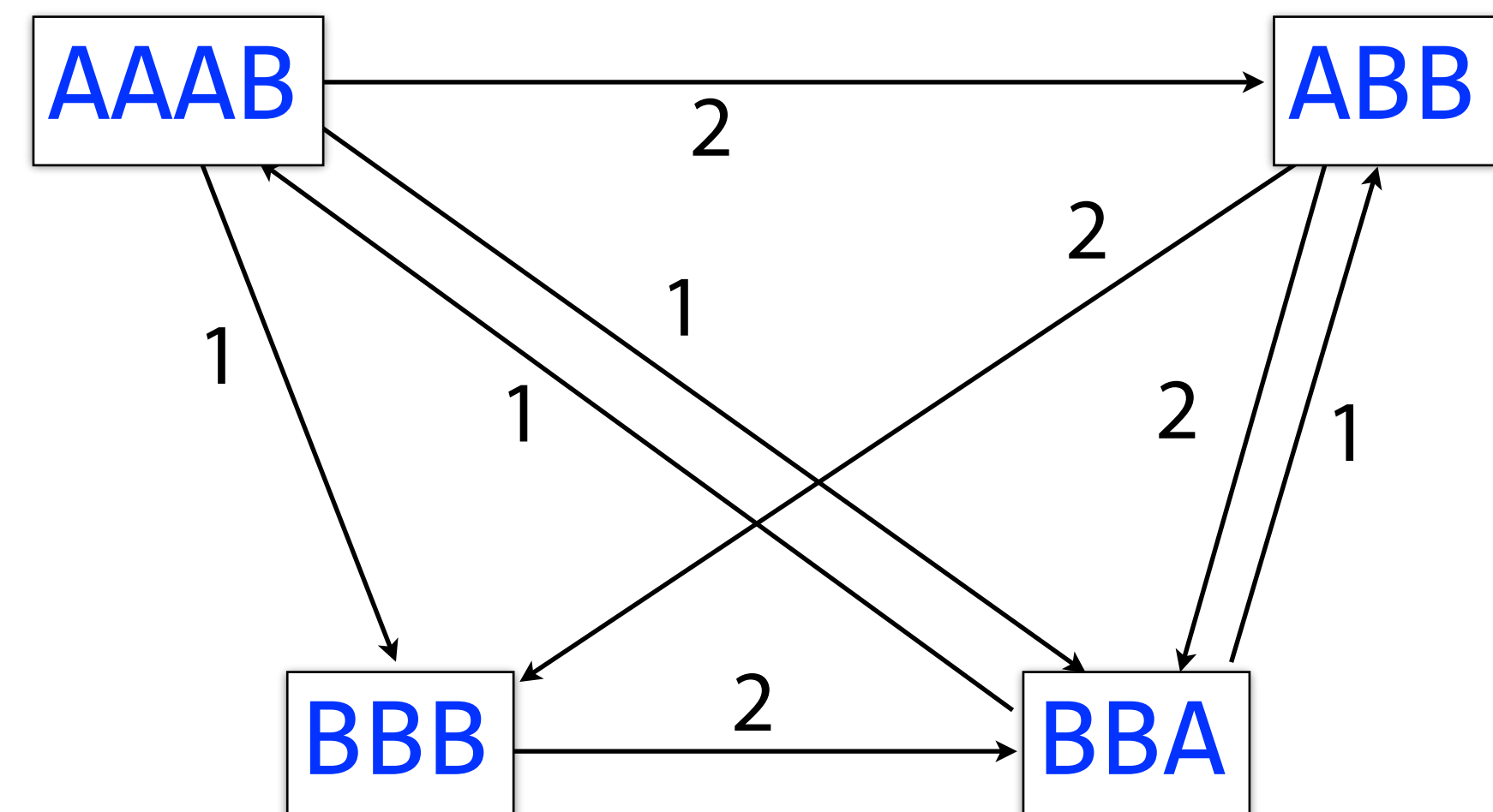
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AAA AAB ABB BBB BBA

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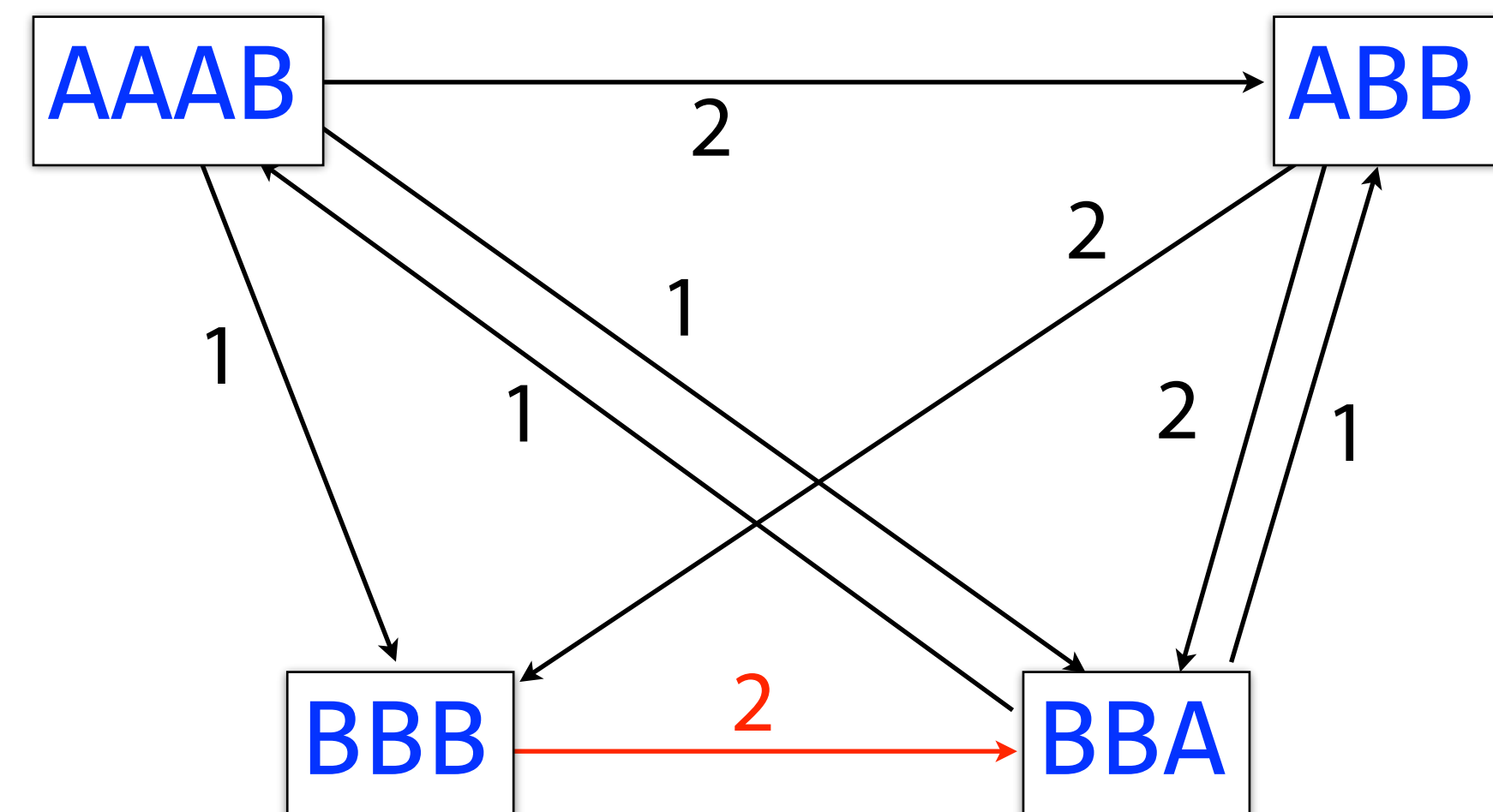
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AAAB ABB BBB BBA



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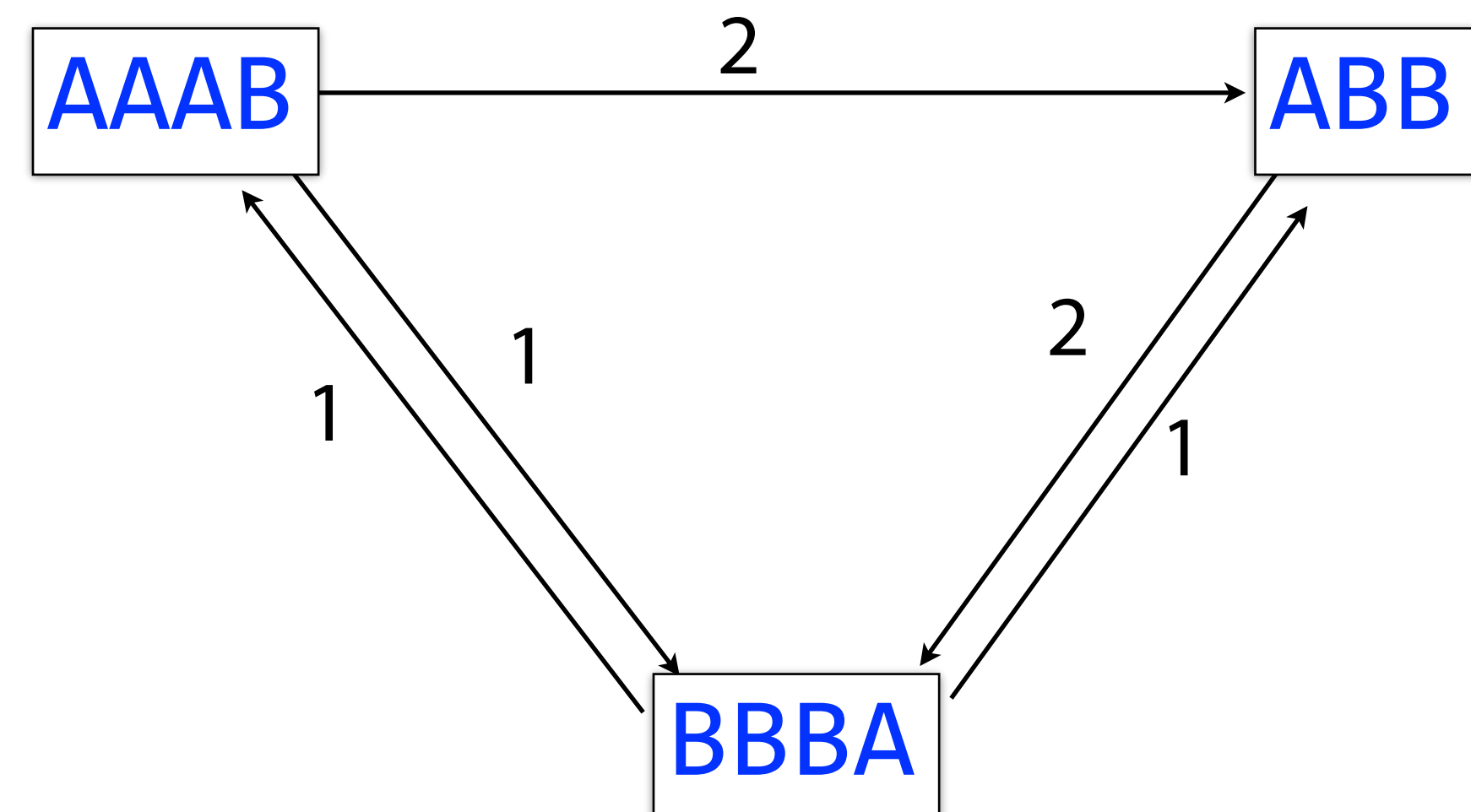
┌─── Input strings ──┐

AAA AAB ABB BBB BBA

AAA AAB ABB BBB BBA

AAAB ABB BBB BBA

AAAB BBBA ABB



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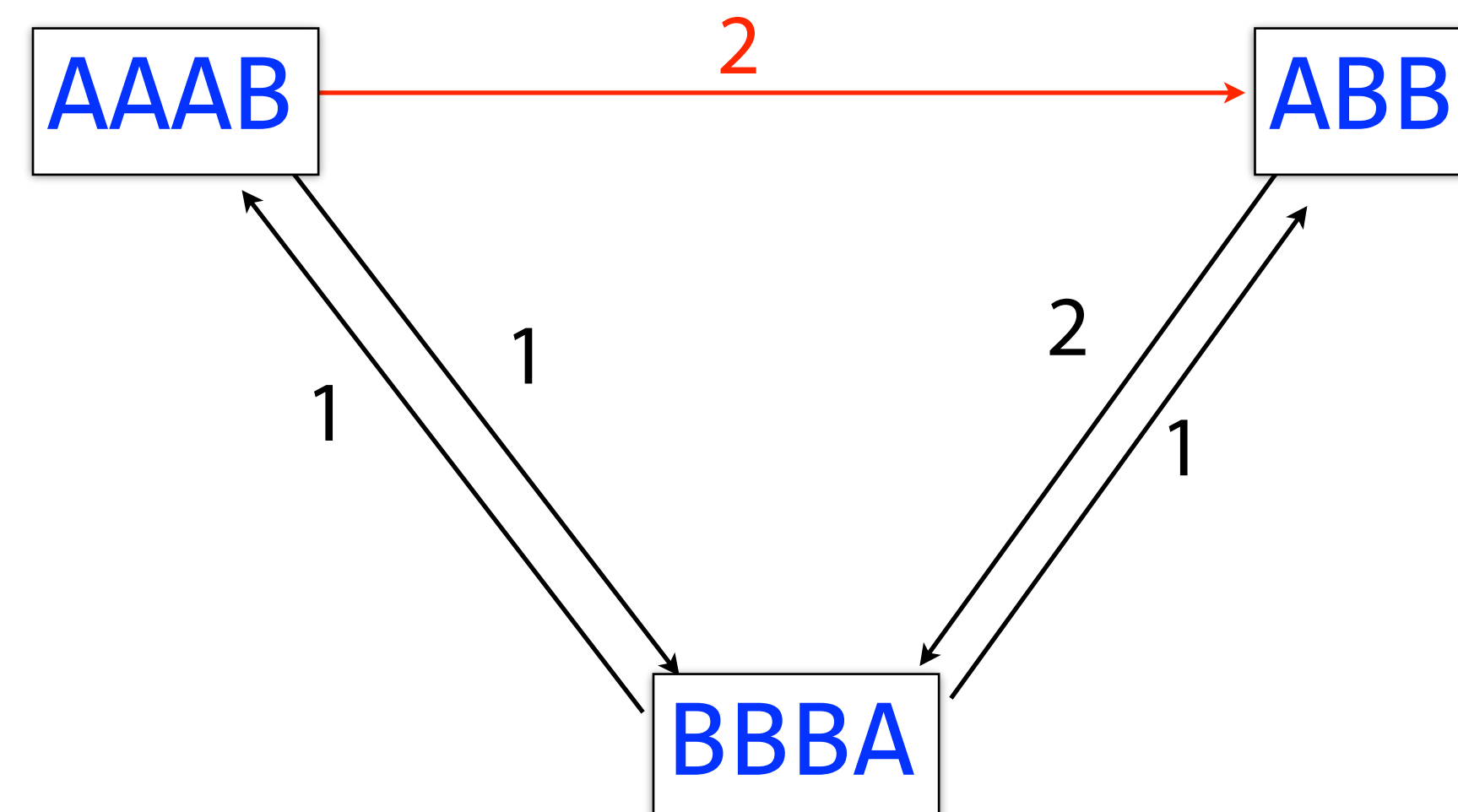
┌─── Input strings ──┐

AAA AAB ABB BBB BBA

AAA AAB ABB BBB BBA

AAAB ABB BBB BBA

AAAB BBBA ABB



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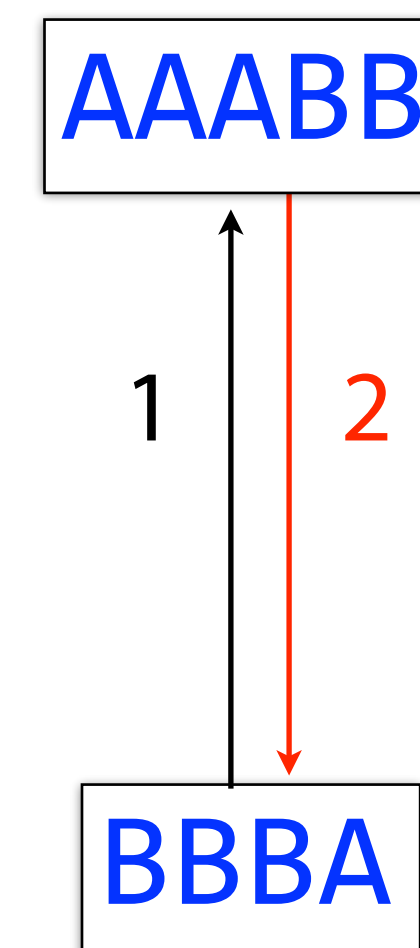
AAA AAB ABB BBB BBA

AAA AAB ABB BBB BBA

AAAB ABB BBB BBA

AAAB BBBA ABB

AAABB BBBA





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AAA AAB ABB BBB BBA

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AAAB ABB BBB BBA

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AAABBBA

AAABBBA

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AAA AAB ABB BBB BBA

AAAB ABB BBB BBA

AAAB BBBA ABB

AAABB BBBA

AAABBBA

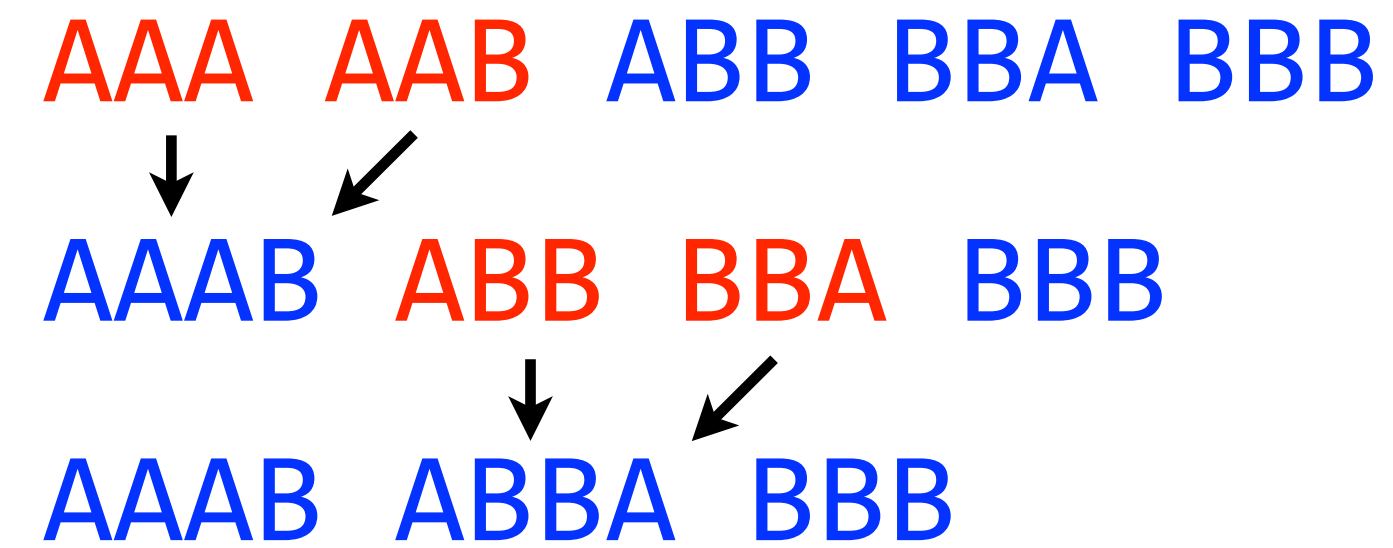
AAABBBA

That's the SCS

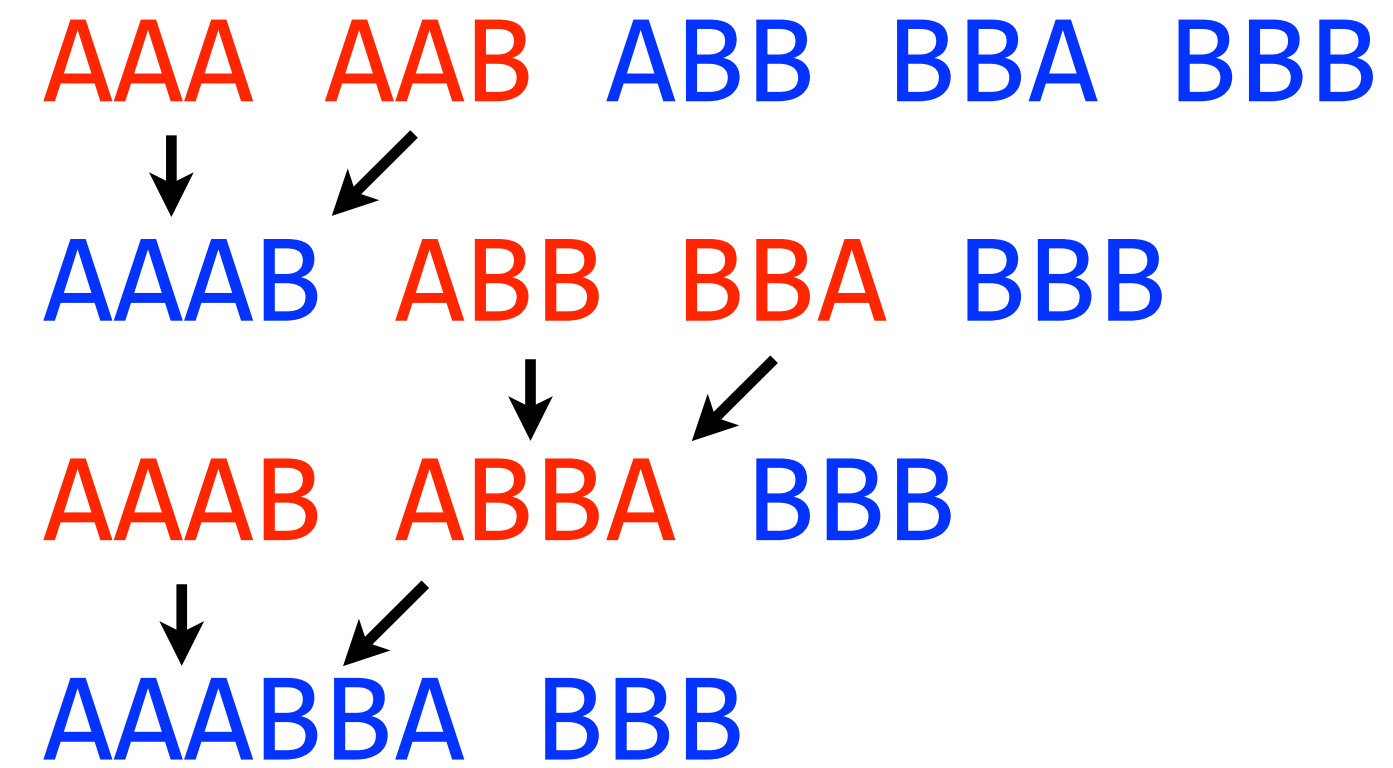
# Greedy shortest common superstring (when is it not optimal?)

AAA AAB ABB BBA BBB  
↓ ↙  
AAAB ABB BBA BBB

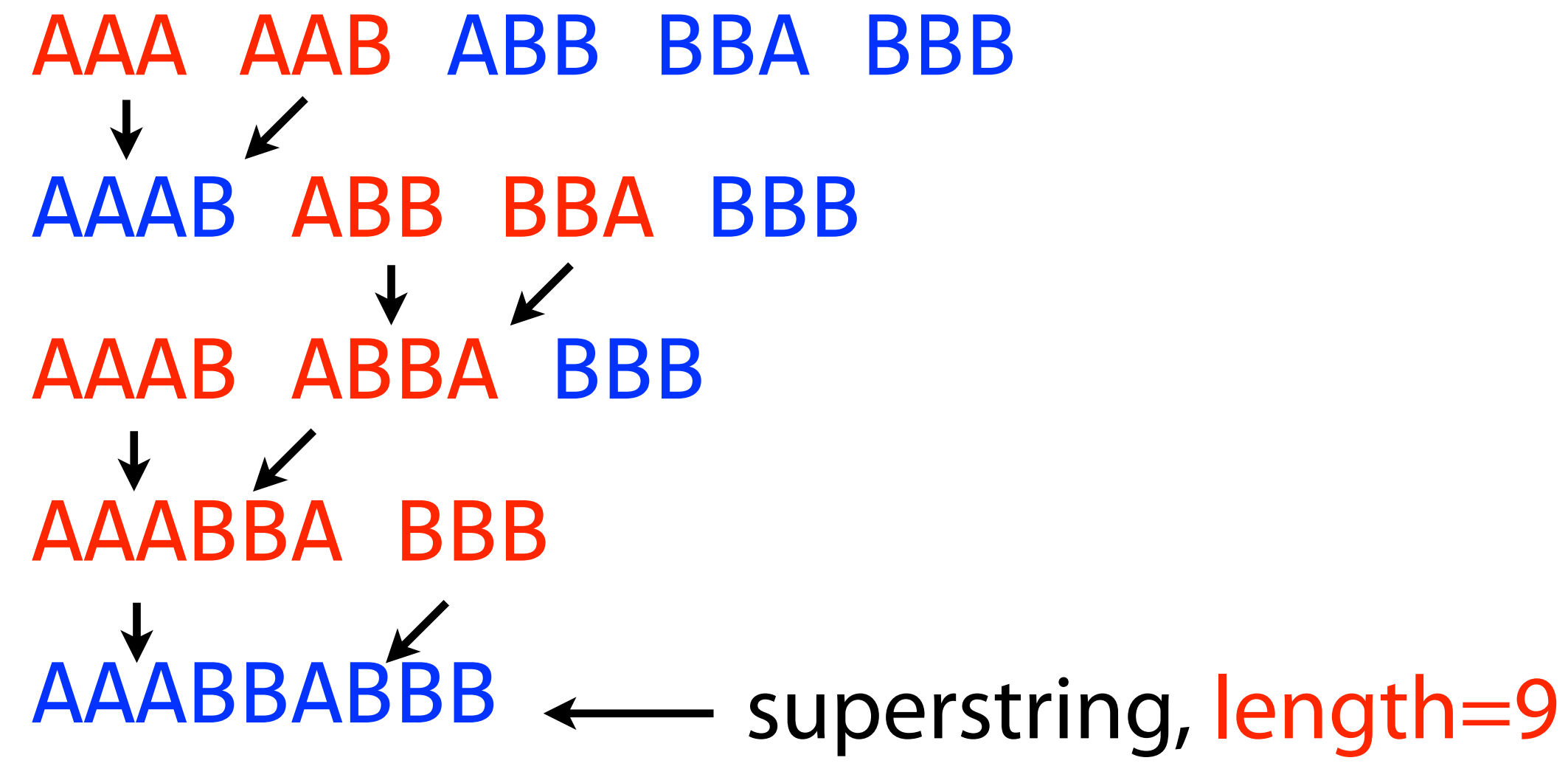
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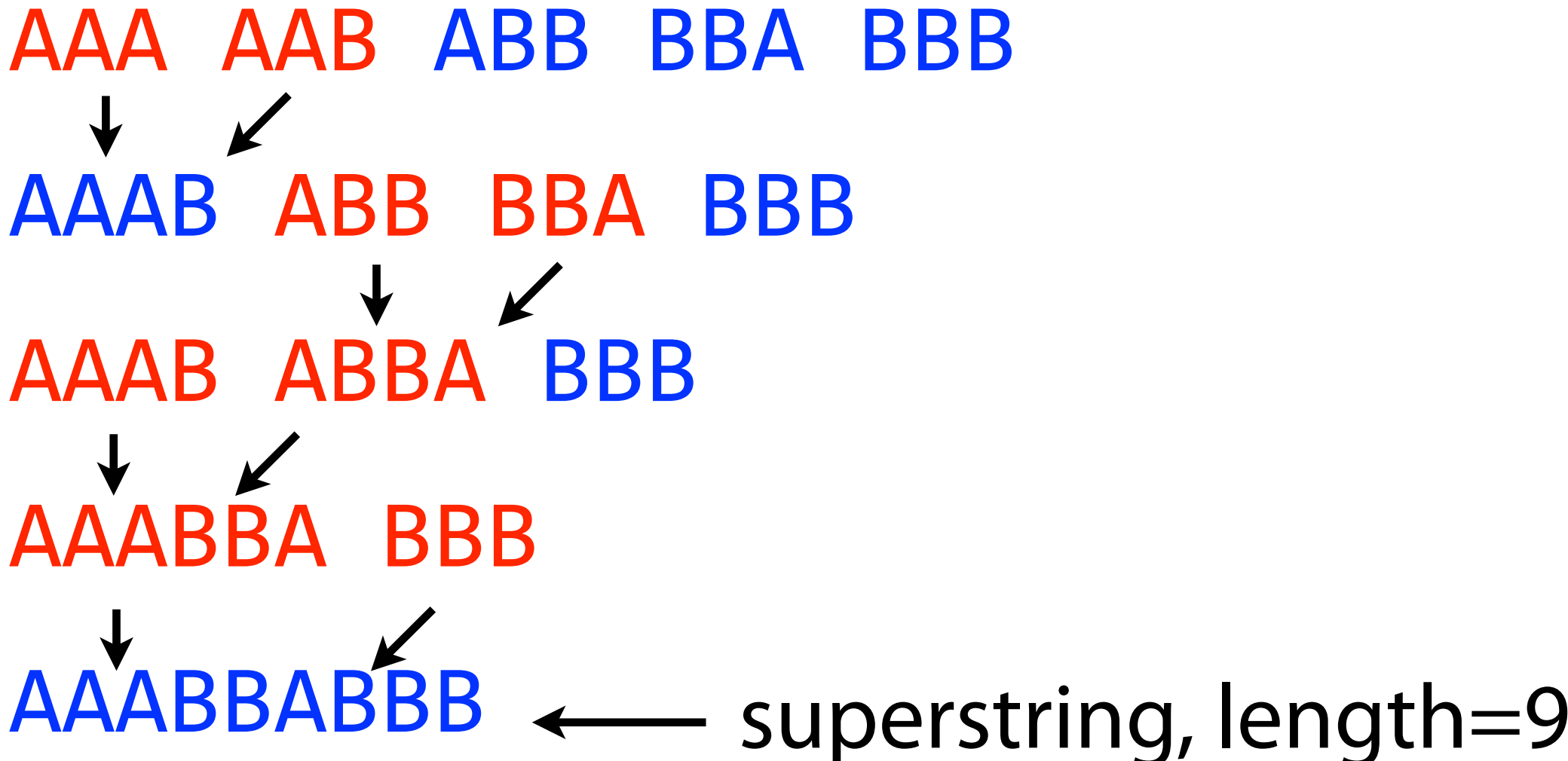
# Greedy shortest common superstring (when is it not optimal?)



# Greedy shortest common superstring (when is it not optimal?)



# Greedy shortest common superstring (when is it not optimal?)



AAABBBA ← superstring, length=7

Greedy answer isn't necessarily optimal

# Shortest common superstring: greedy

Why else might it not be a good model for assembly?

Greedy-SCS assembling all substrings of length 6 from:

[a\\_long\\_long\\_long\\_time](#).  $l = 3$ .



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`a_long_long_long_time`.  $l = 3$ .

`ng_lon _long_ a_long long_l ong_ti ong_lo long_t g_long g_time ng_tim`

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```
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ng_time ng_lon _long_ a_long long_l ong_ti ong_lo long_t g_long
```

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ng_time ng_lon _long_ a_long long_l ong_ti ong_lo long_t g_long  
ng_time g_long_ ng_lon a_long long_l ong_ti ong_lo long_t
```

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ng_time ng_lon _long_ a_long long_l ong_ti ong_lo long_t g_long
ng_time g_long_ ng_lon a_long long_l ong_ti ong_lo long_t
ng_time long_ti g_long_ ng_lon a_long long_l ong_lo
```

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```
ng_lon _long_ a_long long_l ong_ti ong_lo long_t g_long g_time ng_tim
ng_time ng_lon _long_ a_long long_l ong_ti ong_lo long_t g_long
ng_time g_long_ ng_lon a_long long_l ong_ti ong_lo long_t
ng_time long_ti g_long_ ng_lon a_long long_l ong_lo
ng_time ong_lon long_ti g_long_ a_long long_l
```

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```
ng_lon _long_ a_long long_l ong_ti ong_lo long_t g_long g_time ng_tim
ng_time ng_lon _long_ a_long long_l ong_ti ong_lo long_t g_long
ng_time g_long_ ng_lon a_long long_l ong_ti ong_lo long_t
ng_time long_ti g_long_ ng_lon a_long long_l ong_lo
ng_time ong_lon long_ti g_long_ a_long long_l
ong_lon long_time g_long_ a_long long_l
```

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```
ng_lon _long_ a_long long_l ong_ti ong_lo long_t g_long g_time ng_tim
ng_time ng_lon _long_ a_long long_l ong_ti ong_lo long_t g_long
ng_time g_long_ ng_lon a_long long_l ong_ti ong_lo long_t
ng_time long_ti g_long_ ng_lon a_long long_l ong_lo
ng_time ong_lon long_ti g_long_ a_long long_l
ong_lon long_time g_long_ a_long long_l
long_lon long_time g_long_ a_long
```

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```
ng_lon _long_ a_long long_l ong_ti ong_lo long_t g_long g_time ng_tim
ng_time ng_lon _long_ a_long long_l ong_ti ong_lo long_t g_long
ng_time g_long_ ng_lon a_long long_l ong_ti ong_lo long_t
ng_time long_ti g_long_ ng_lon a_long long_l ong_lo
ng_time ong_lon long_ti g_long_ a_long long_l
ong_lon long_time g_long_ a_long long_l
long_lon long_time g_long_ a_long
long_lon g_long_time a_long
```



# Shortest common superstring: greedy

Why else might it not be a good model for assembly?

Greedy-SCS assembling all substrings of length 6 from:

`a_long_long_long_time`.  $l = 3$ .

```
ng_lon _long_ a_long long_l ong_ti ong_lo long_t g_long g_time ng_tim
ng_time ng_lon _long_ a_long long_l ong_ti ong_lo long_t g_long
ng_time g_long_ ng_lon a_long long_l ong_ti ong_lo long_t
ng_time long_ti g_long_ ng_lon a_long long_l ong_lo
ng_time ong_lon long_ti g_long_ a_long long_l
ong_lon long_time g_long_ a_long long_l
long_lon long_time g_long_ a_long
long_lon g_long_time a_long
long_long_time a_long
```

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```
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ng_time ng_lon _long_ a_long long_l ong_ti ong_lo long_t g_long
ng_time g_long_ ng_lon a_long long_l ong_ti ong_lo long_t
ng_time long_ti g_long_ ng_lon a_long long_l ong_lo
ng_time ong_lon long_ti g_long_ a_long long_l
ong_lon long_time g_long_ a_long long_l
long_lon long_time g_long_ a_long
long_lon g_long_time a_long
long_long_time a_long
a_long_long_time
```

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ng_lon _long_ a_long long_l ong_ti ong_lo long_t g_long g_time ng_tim
ng_time ng_lon _long_ a_long long_l ong_ti ong_lo long_t g_long
ng_time g_long_ ng_lon a_long long_l ong_ti ong_lo long_t
ng_time long_ti g_long_ ng_lon a_long long_l ong_lo
ng_time ong_lon long_ti g_long_ a_long long_l
ong_lon long_time g_long_ a_long long_l
long_lon long_time g_long_ a_long
long_lon g_long_time a_long
long_long_time a_long
a_long_long_time
```



Foiled by repeat!

# Shortest common superstring: greedy

Same example, but increased the substring length from 6 to 8

```
long_lon ng_long_ _long_lo g_long_t ong_long g_long_l ong_time a_long_l _long_ti long_tim
long_time long_lon ng_long_ _long_lo g_long_t ong_long g_long_l a_long_l _long_ti
_long_time long_lon ng_long_ _long_lo g_long_t ong_long g_long_l a_long_l
_long_time a_long_lo long_lon ng_long_ g_long_t ong_long g_long_l
_long_time ong_long_ a_long_lo long_lon g_long_t g_long_l
g_long_time ong_long_ a_long_lo long_lon g_long_l
g_long_time ong_long_ a_long_lo g_long_l
g_long_time ong_long_l a_long_lo
g_long_time a_long_lo
a_long_lo
a_long_lo
```

Got the whole thing: [a\\_long\\_lo](#)

# Shortest common superstring: greedy

Why are substrings of length 8 long enough for Greedy-SCS to figure out there are 3 copies of `long`?

`a_long_long_long_time`

# Shortest common superstring: greedy

Why are substrings of length 8 long enough for Greedy-SCS to figure out there are 3 copies of `long`?

`a_long_long_long_time`

`g_long_l`

# Shortest common superstring: greedy

Why are substrings of length 8 long enough for Greedy-SCS to figure out there are 3 copies of `long`?

`a_long_long_long_time`

`g_long_l`

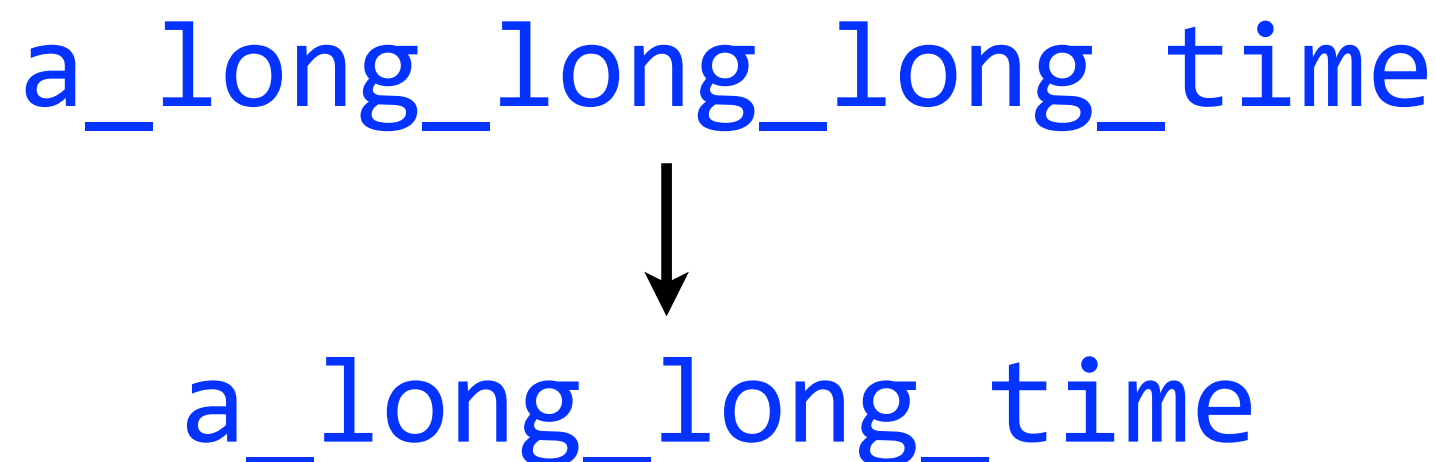


One length-8 substring spans all three `longs`

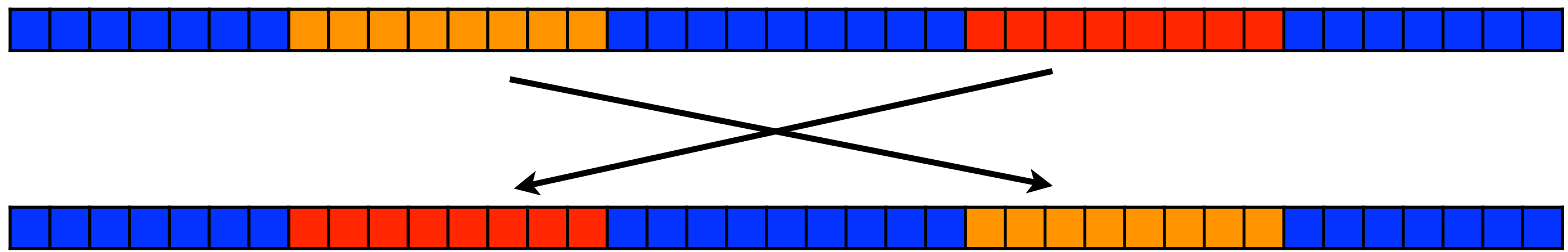
# Third law of assembly

Repeats make assembly difficult; whether we can assemble without mistakes depends on length of reads and repetitive patterns in genome

Collapsing a tandem repeat:



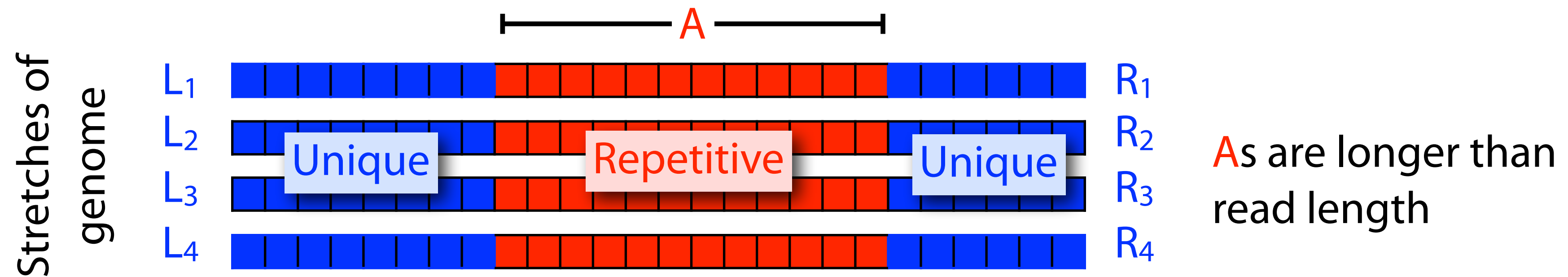
Spurious rearrangement:





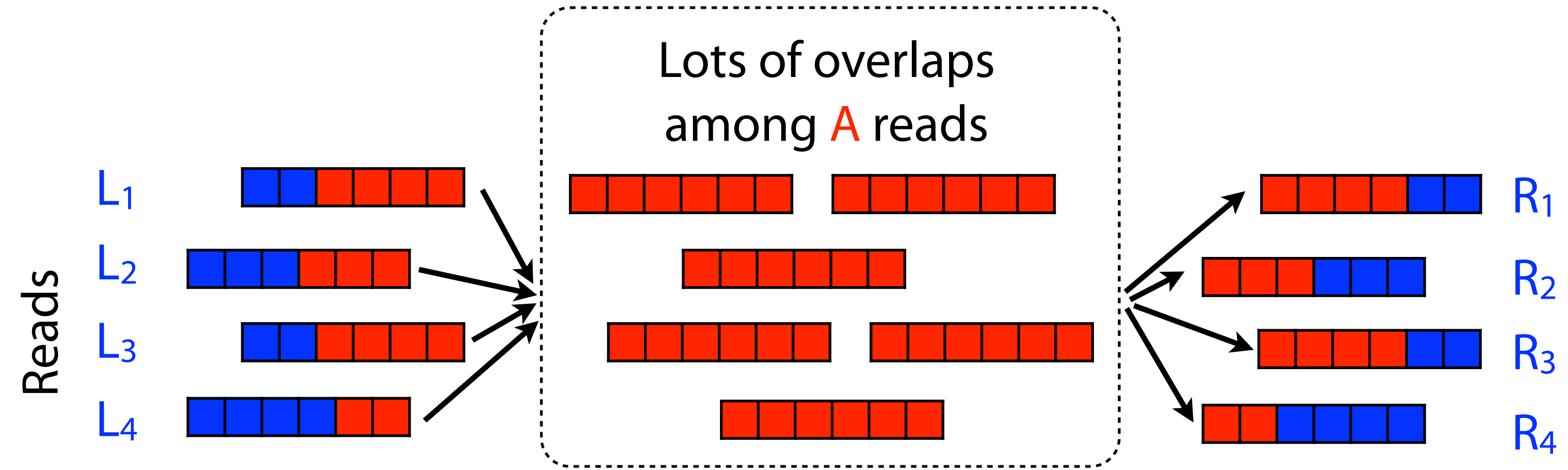
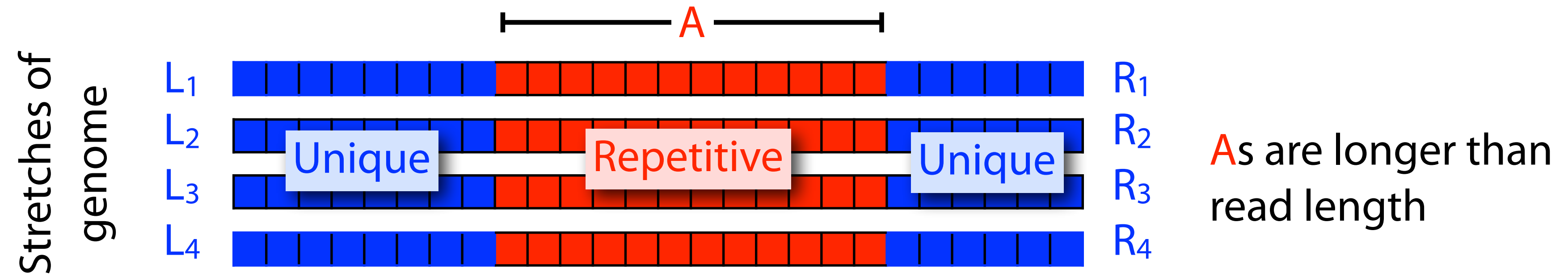
# Repeats foil assembly

Portion of overlap graph involving repeat family **A**



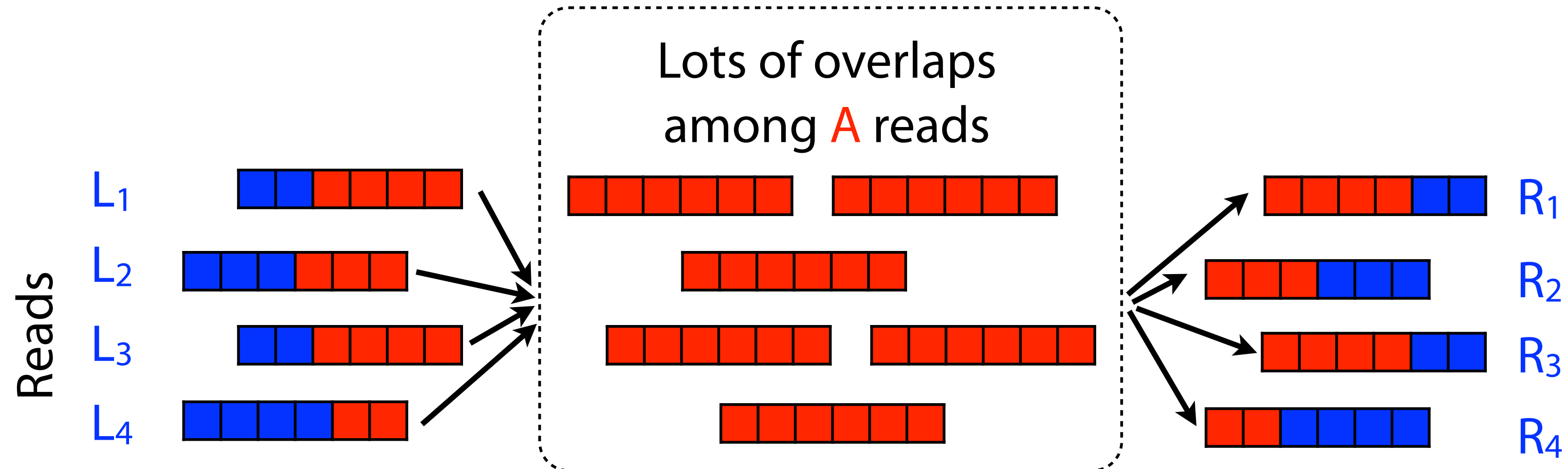
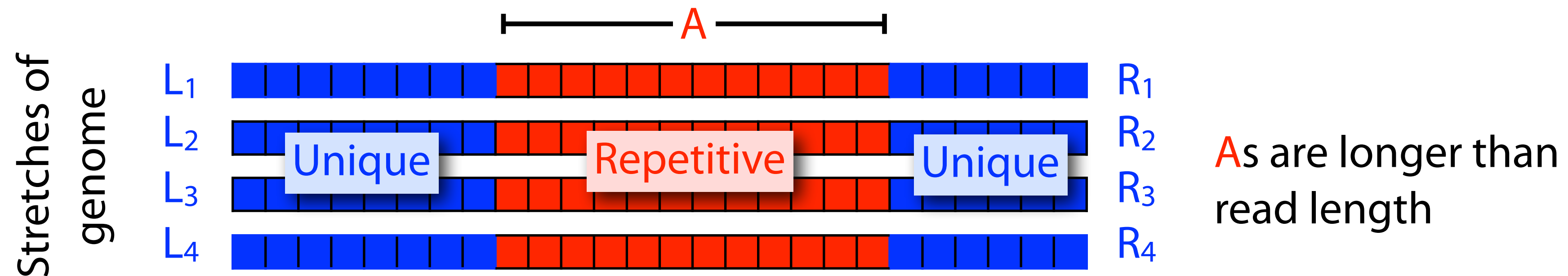
# Repeats foil assembly

Portion of overlap graph involving repeat family **A**



# Repeats foil assembly

Portion of overlap graph involving repeat family **A**



Even if we avoid collapsing copies of **A**, we can't know which paths in correspond to which paths out

# Take-home message:

We are interested in *correct and efficient algorithms* for solving *well-specified* problems.

We must be careful about how we *pose* the problems.

Actually, shortest common superstring is a rather poor model for sequence assembly, due to repeats and errors.