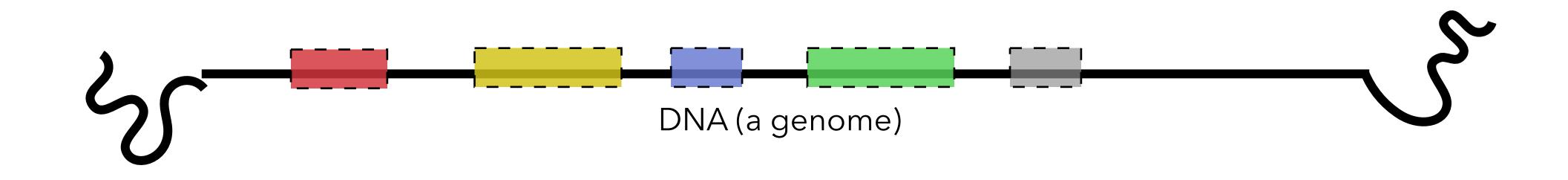
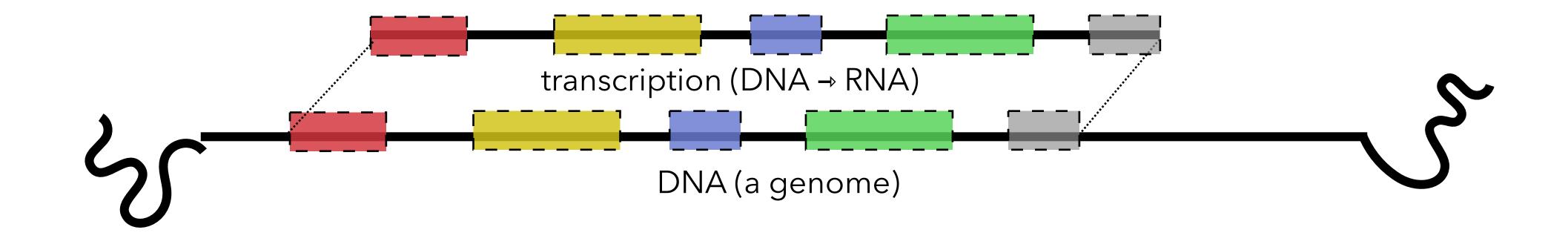
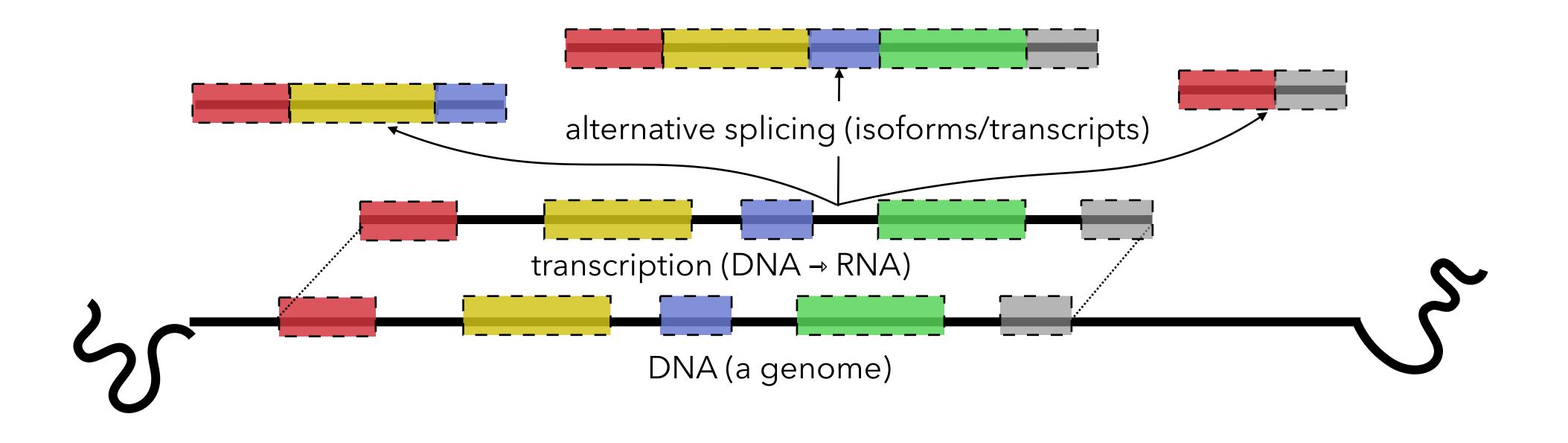
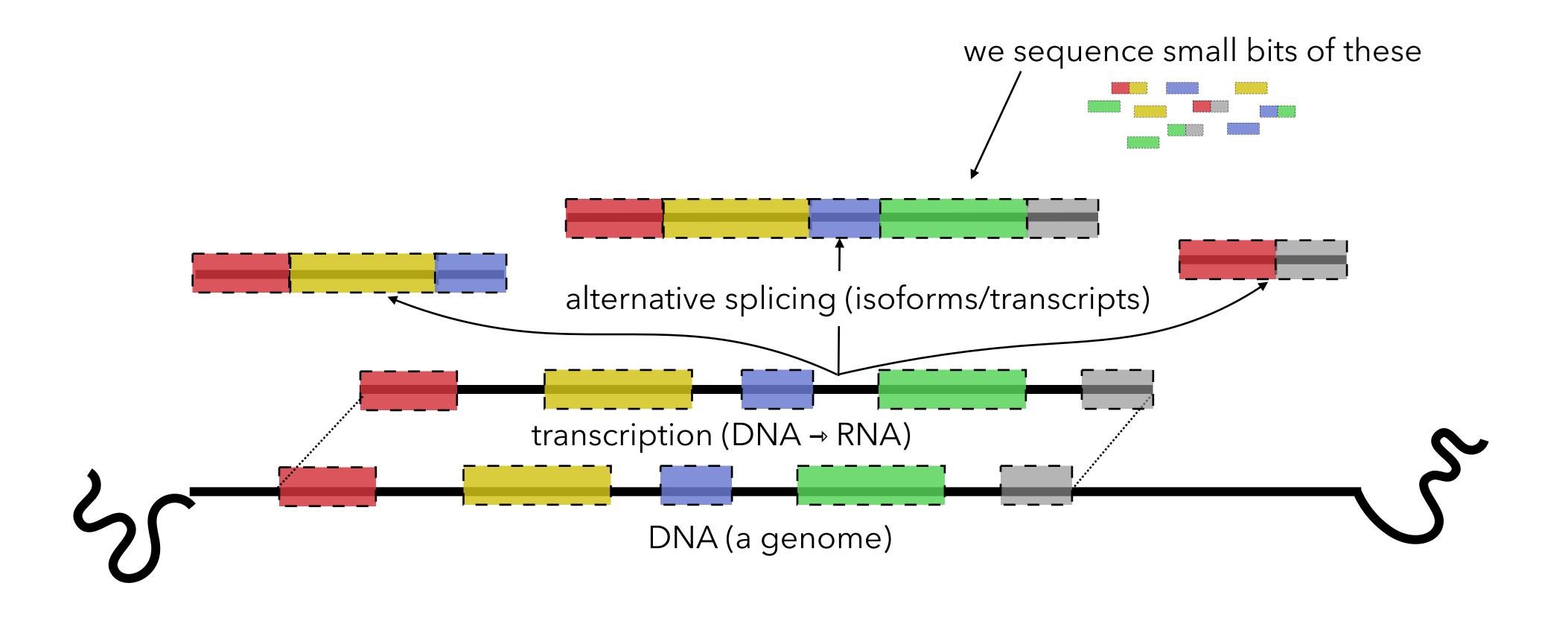


Transcript assembly using RNA-seq data

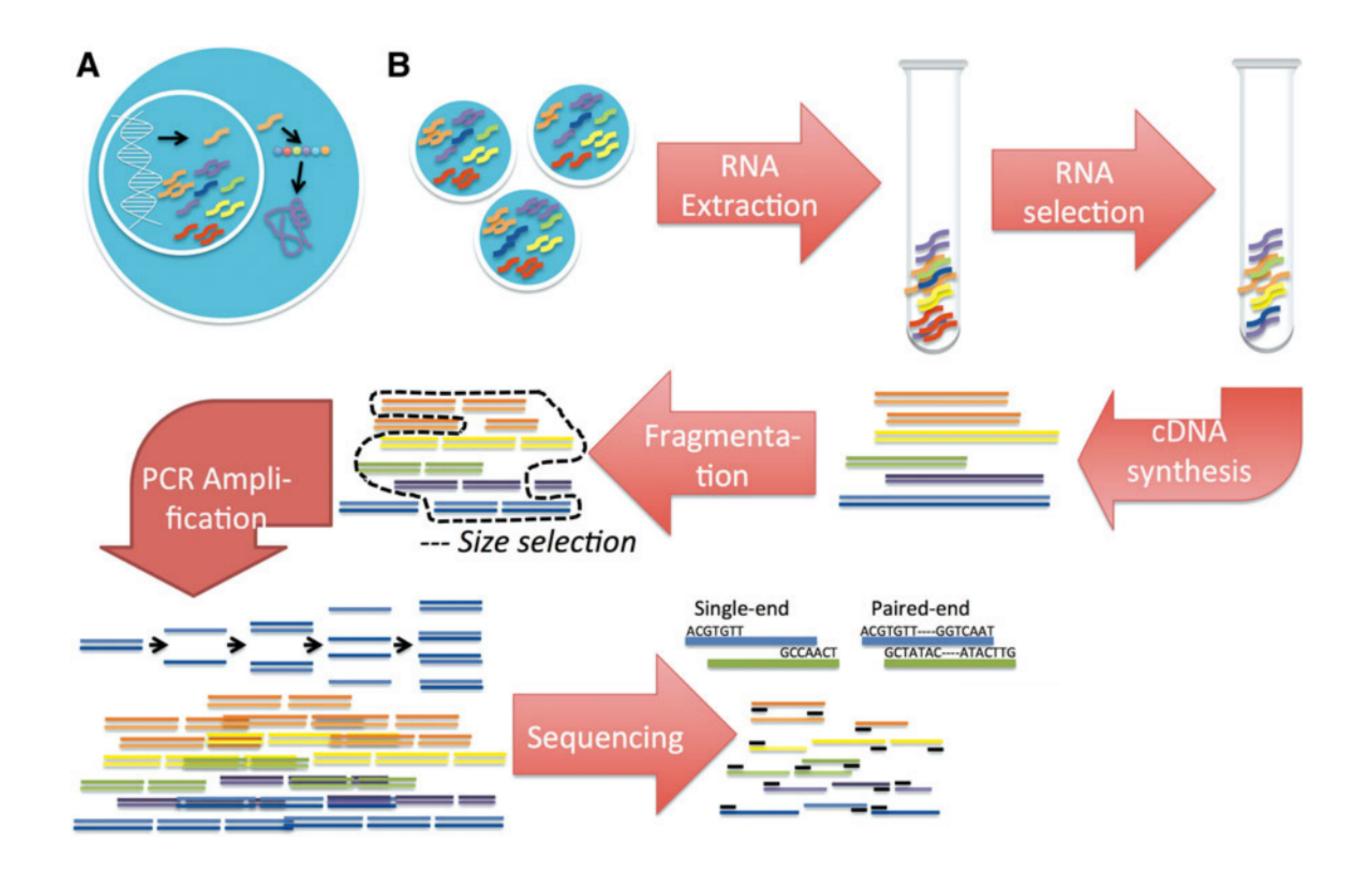








Actual protocols are much more involved



Prakash, Celine, and Arndt Von Haeseler. "An Enumerative Combinatorics Model for Fragmentation Patterns in RNA Sequencing Provides Insights into Nonuniformity of the Expected Fragment Starting-Point a of Computational Biology 24.3 (2017): 200-212.



RNA-seq data has many uses in transcriptome analysis. Some common uses include:

Fusion/chimera detection Variant (SNP, SV, CNV) detection

Transcript assembly Genome guided & de novo

Transcript quantification

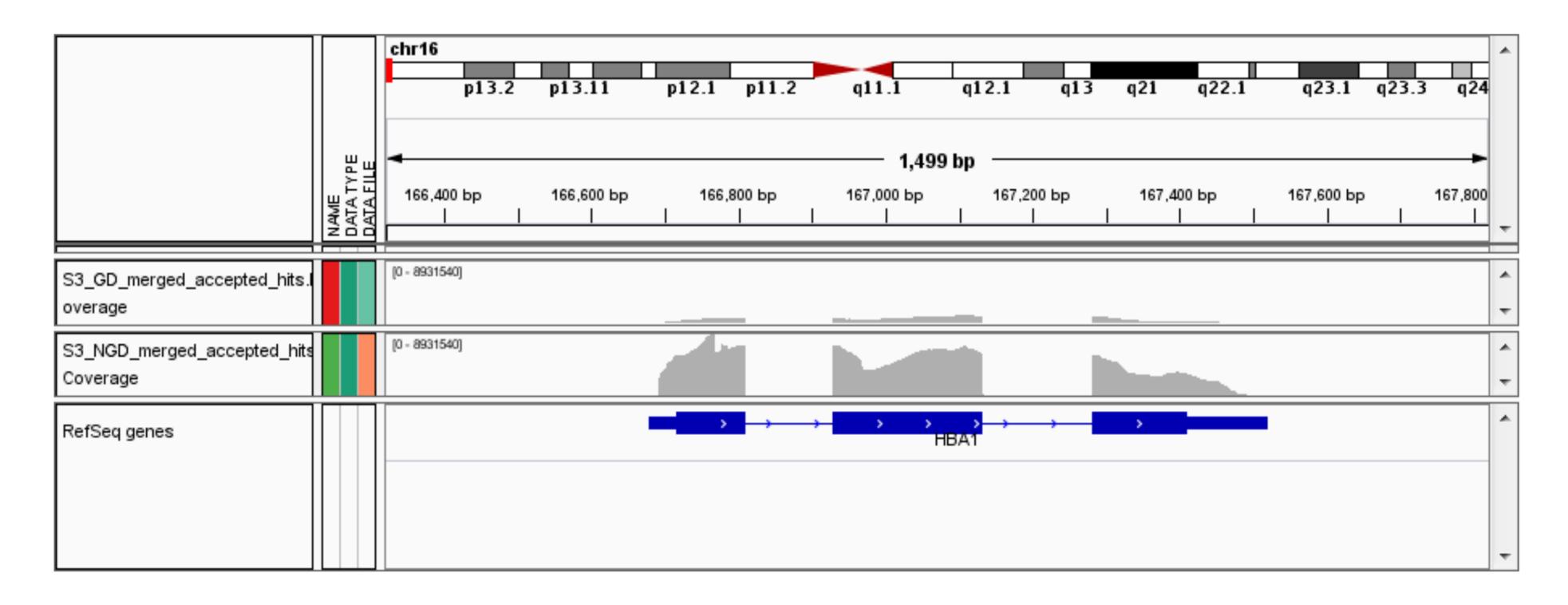
Differential expression, alternative splicing analysis

Build higher-level models of transcription

co-expression networks -> regulatory networks

Many uses of RNA-seq for transcriptome analysis

The benefit is reads are drawn directly from transcripts!



RNA-Seq reads come from a spliced transcript — if we can map them back to the genome, they give us evidence of **transcribed** regions.

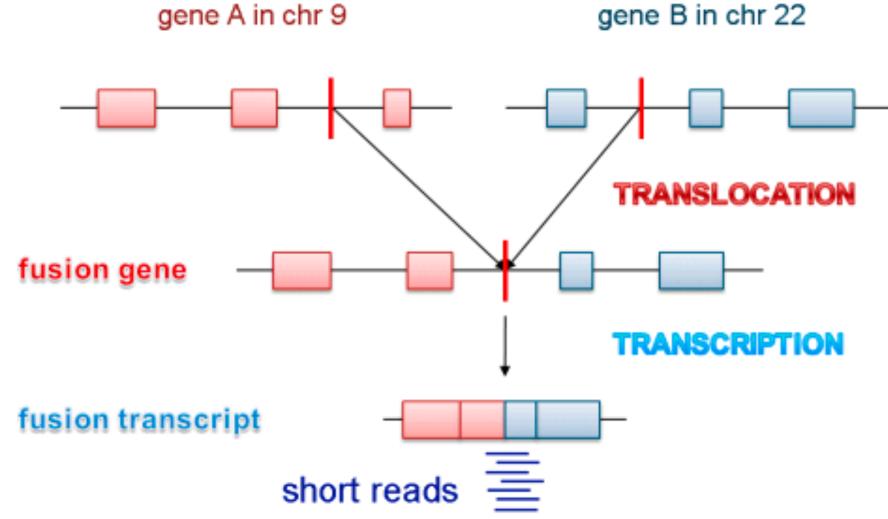
Human genome contains > 14,000 pseudogenes [Pei et al. Genome Biology 2012]

Image from: Shin, Heesun, et al. "Variation in RNA-Seq Transcriptome Profiles of Peripheral Whole Blood from Healthy Individuals with and without Globin Depletion." PloS one 9.3 (2014): e91041.



This means you see what is there, not just what is annotated

Fusion/chimera detection



Variant (SNP, SV, CNV) detection

Find small (SNP) or large (SV) variation in how read map back to their genes of origin

Find differences in the number of copies of a gene in the DNA (CNV)

image from: <u>http://biome.ewha.ac.kr:8080/FusionGene/</u>



Many uses of RNA-seq for transcriptome analysis

RNA-seq data has many uses in transcriptome analysis. Some common uses include:

Fusion/chimera detection Variant (SNP, SV, CNV) detection

Transcript assembly

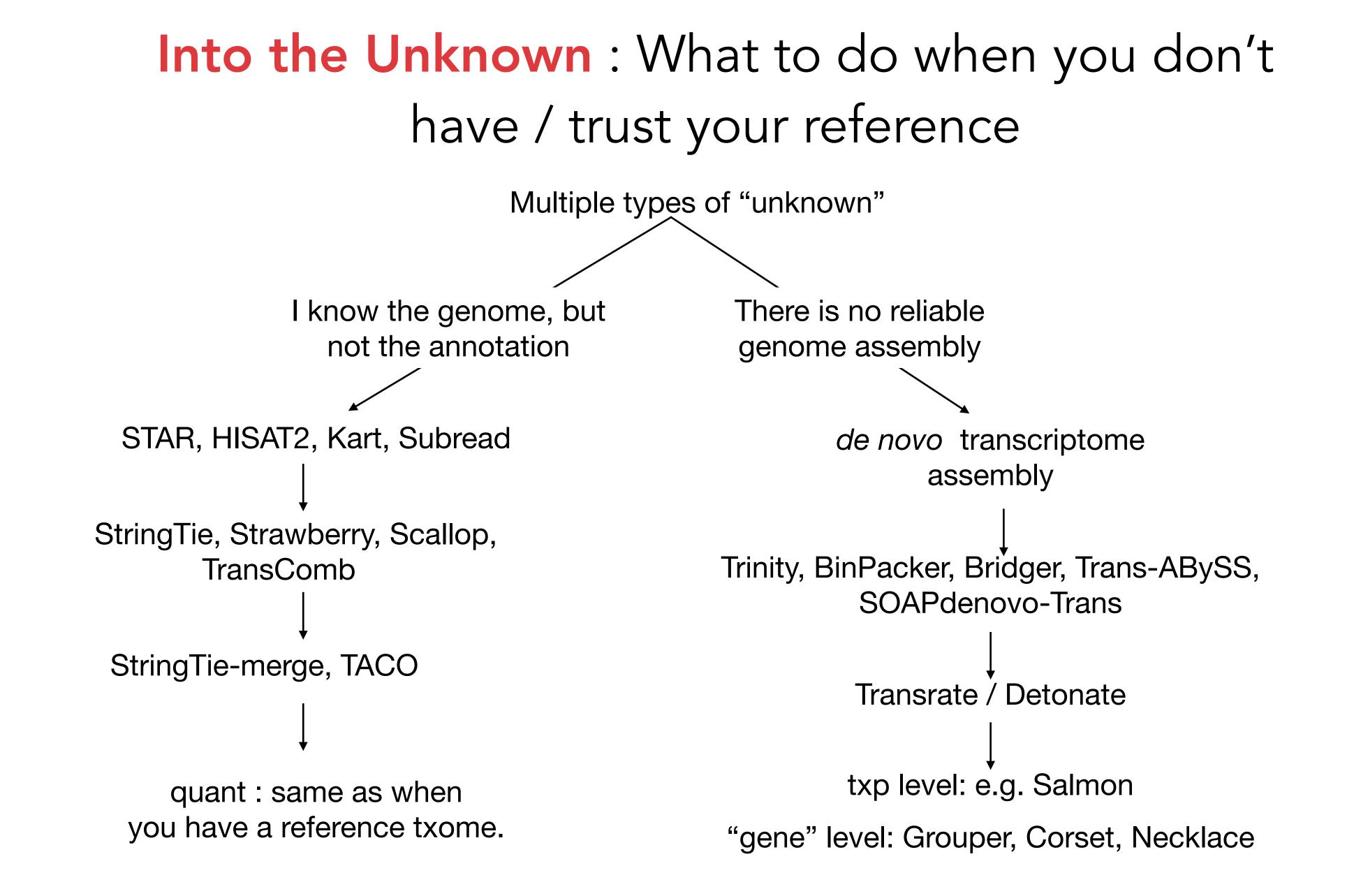
Genome guided & de novo

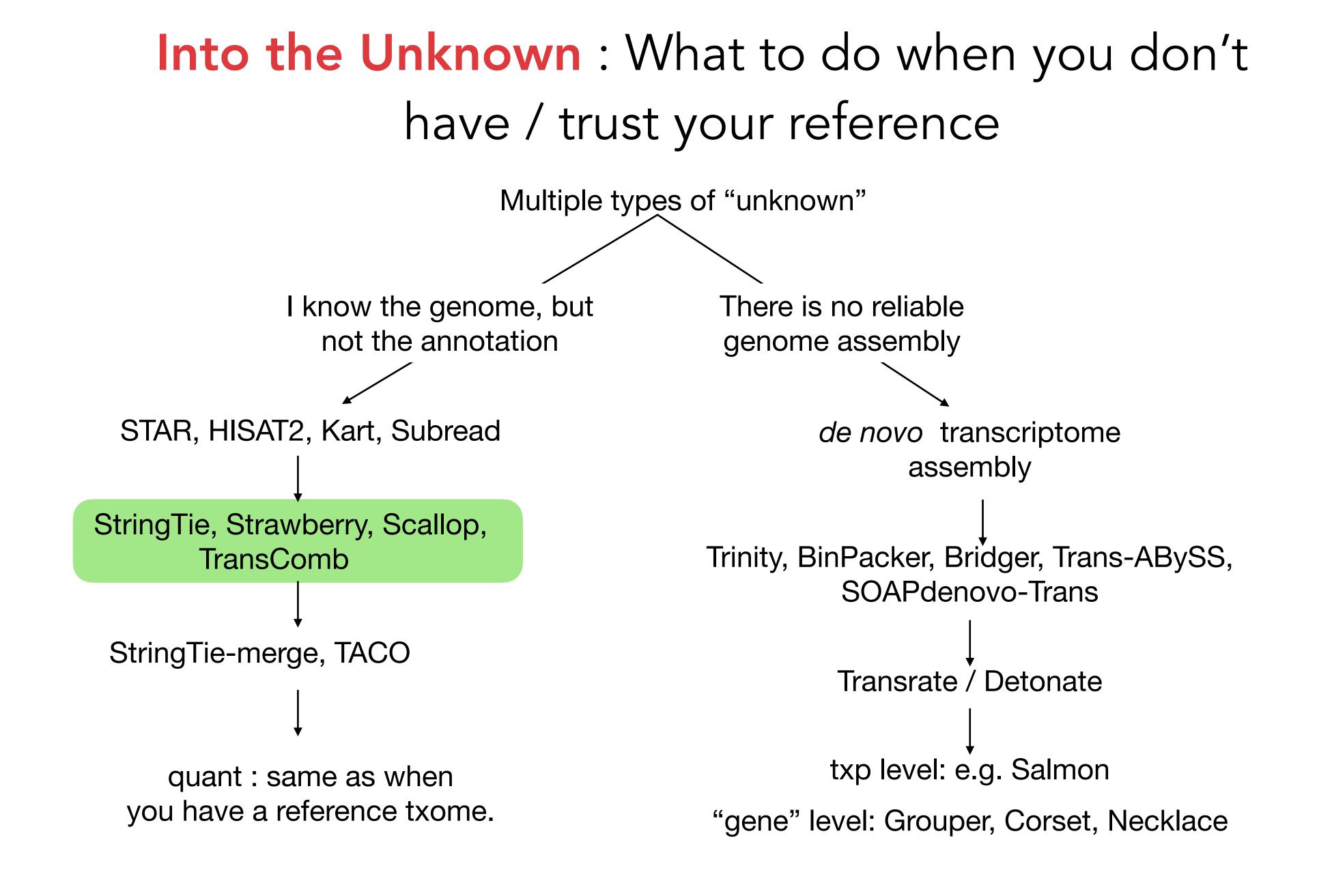
Transcript quantification

Differential expression, alternative splicing analysis

Build higher-level models of transcription

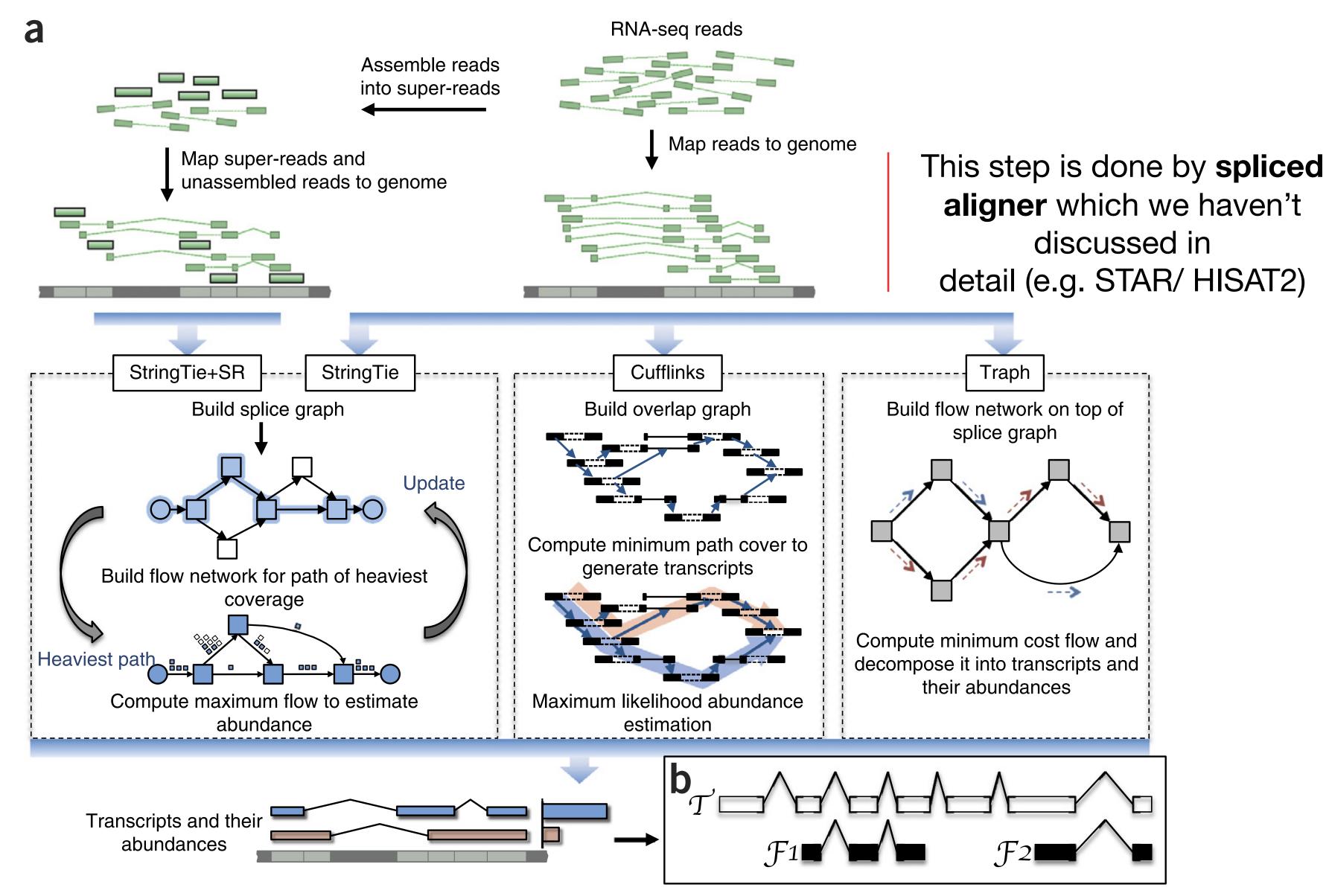
co-expression networks -> regulatory networks





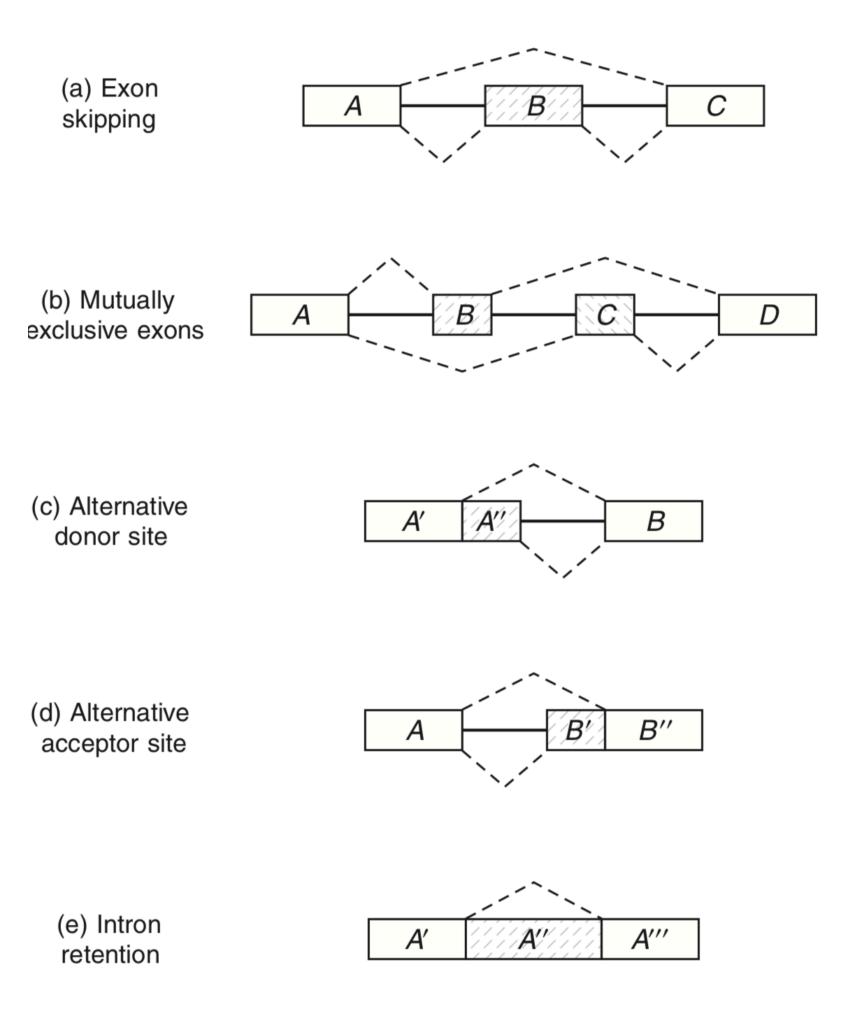
I'll focus mostly on *reference-guided* assembly.

Outline of transcript assembly workflow



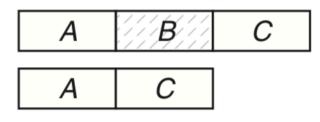
Pertea, Mihaela, et al. "StringTie enables improved reconstruction of a transcriptome from RNA-seq reads." Nature biotechnology 33.3 (2015): 290.

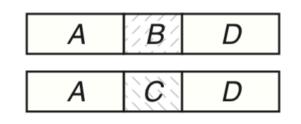




Beretta, Stefano, et al. "Modeling alternative splicing variants from RNA-Seq data with isoform graphs." Journal of Computational Biology 21.1 (2014): 16-40.

Resulting alternative isoforms





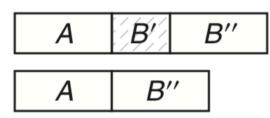
В

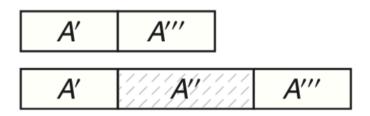
В

A"

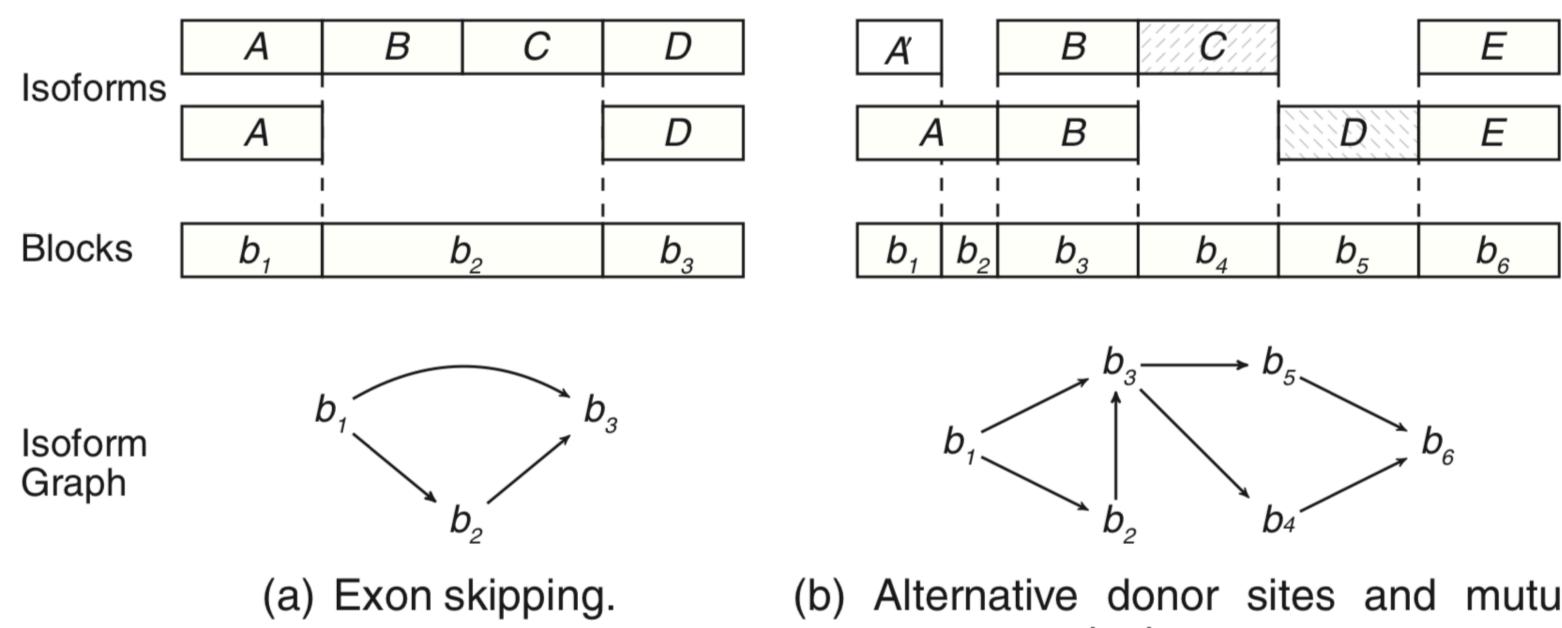
A'

A'

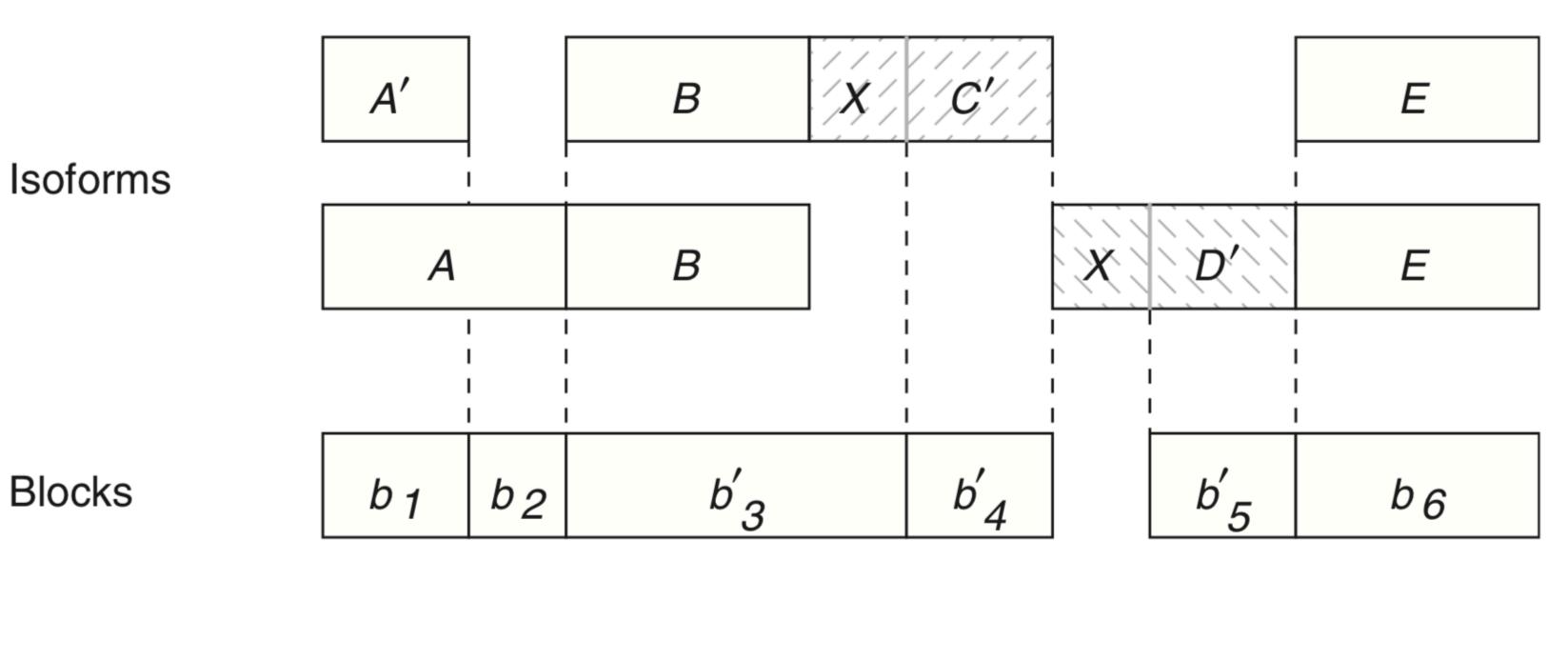


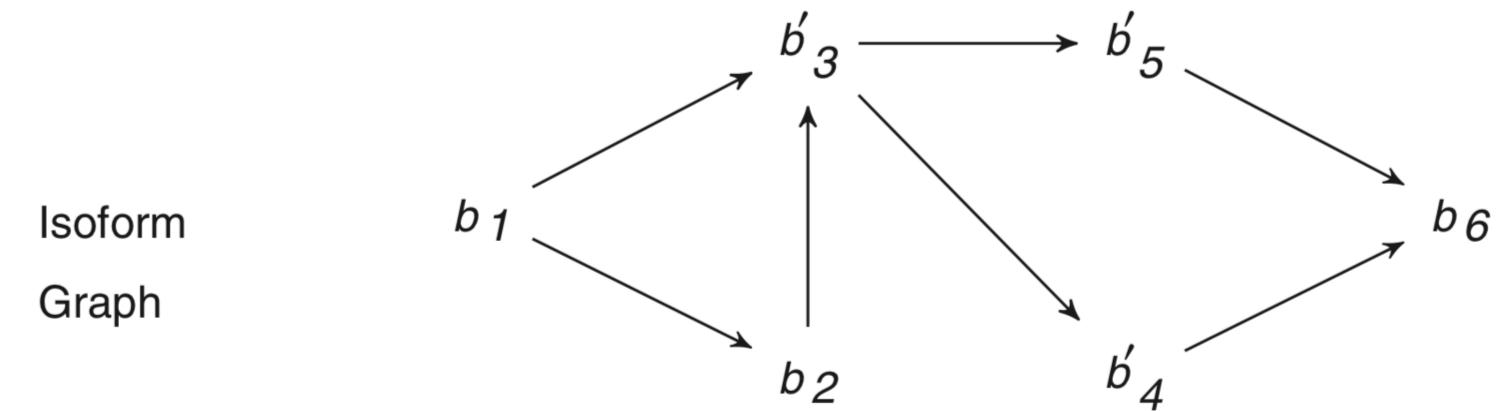


In reality we observe coverage by reads, not exons. Therefore, we end up building a slightly different (data-dependent) graph.

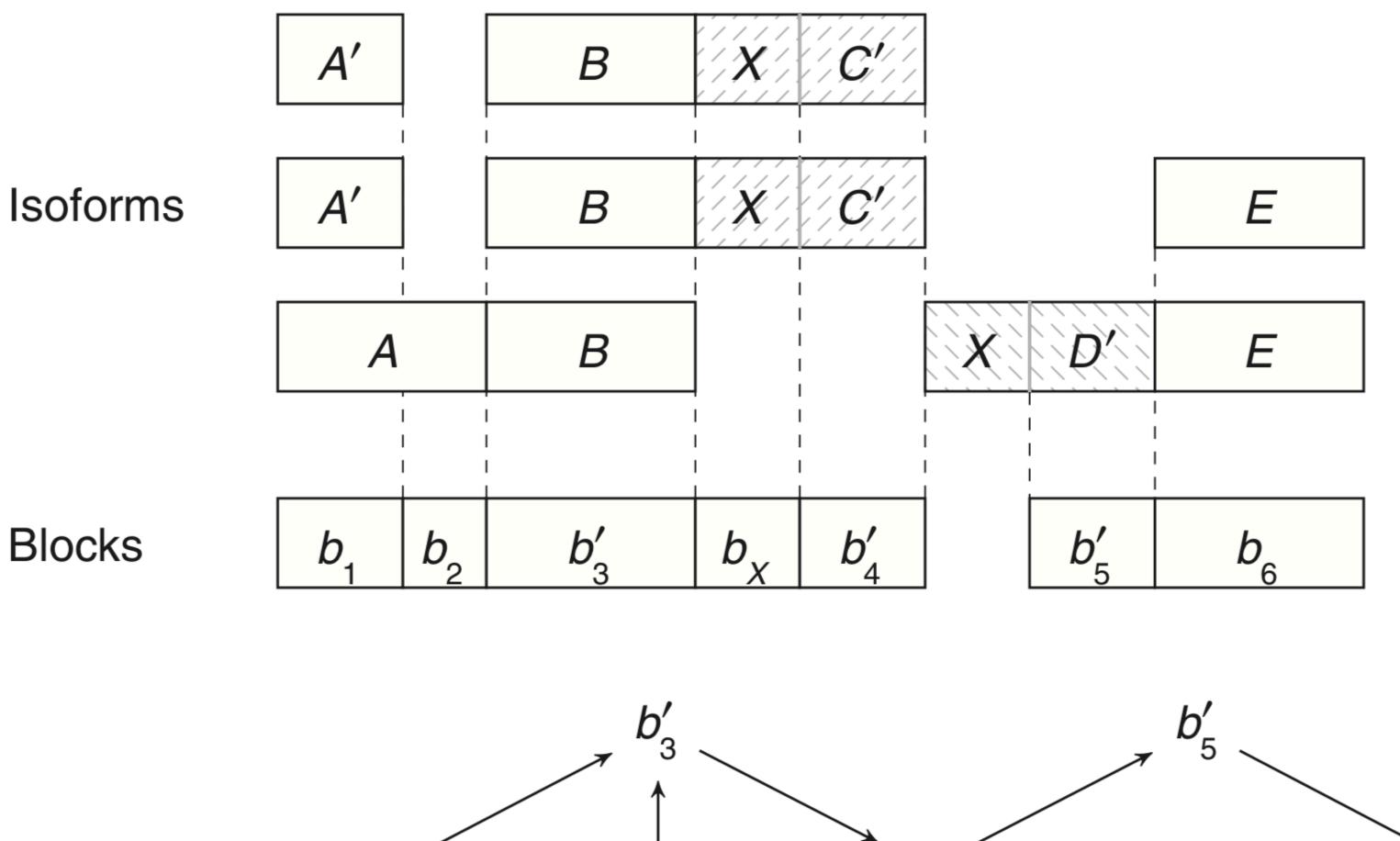


Alternative donor sites and mutually exclusive exons.





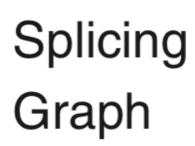
Beretta, Stefano, et al. "Modeling alternative splicing variants from RNA-Seq data with isoform graphs." Journal of Computational Biology 21.1 (2014): 16-40.

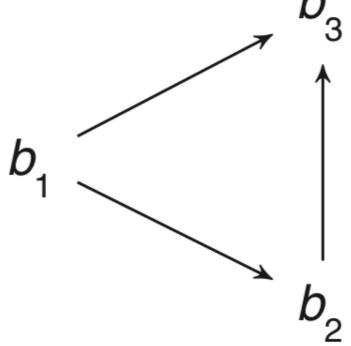


 b_{X}

X

Ď





Beretta, Stefano, et al. "Modeling alternative splicing variants from RNA-Seq data with isoform graphs." Journal of Computational Biology 21.1 (2014): 16-40.

 b_{6}

Building of Splice Graph

StringTie builds an alternative splicing graph (ASG) from all reads at a genomic locus.

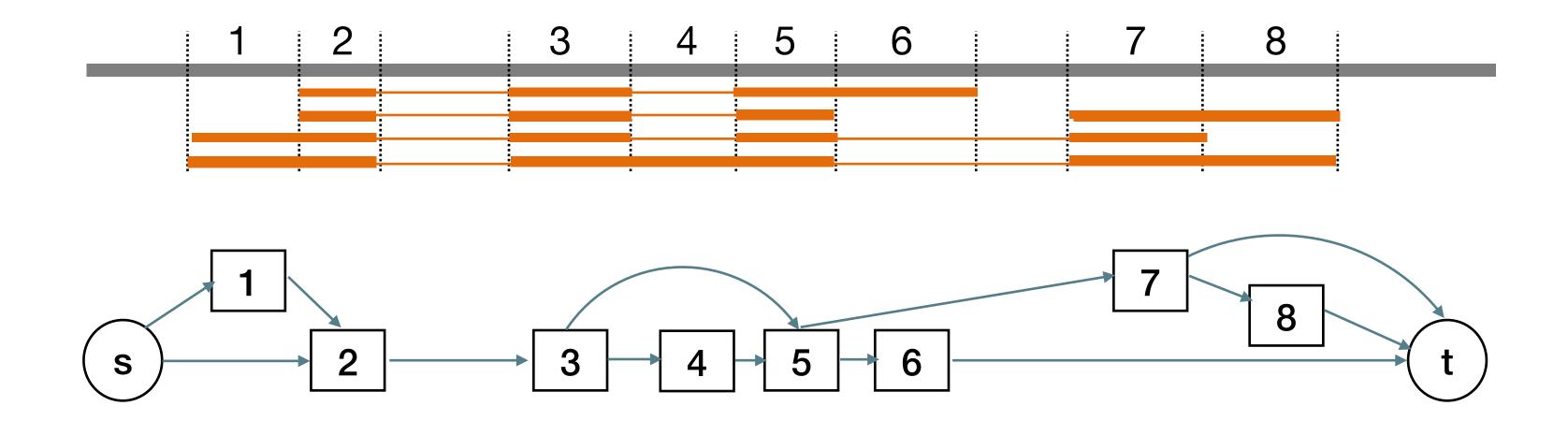
Skips this locus if too many (>95%) of the reads here are multi-mapping

Otherwise, reads are naively given 1/k mass at each of their k multi-mapping loci.

Splice graph is a DAG where nodes are contiguous genomic regions not interrupted by spliced alignments, and edges are placed between two nodes between which a spliced alignment occurs.

Building of Splice Graph

ASG example (adapted from supp fig. 1)



Processing the Splice Graph

StringTie identifies transcripts using the ASG with the following iterative process:

1. Heuristically choose a "heavy" path (a path with the heaviest node) in the ASG

2. Estimate path expression by computing maxflow in a flow graph corresponding to this subpath of the ASG. Subtract the read mass assigned to the nodes in this path & repeat.

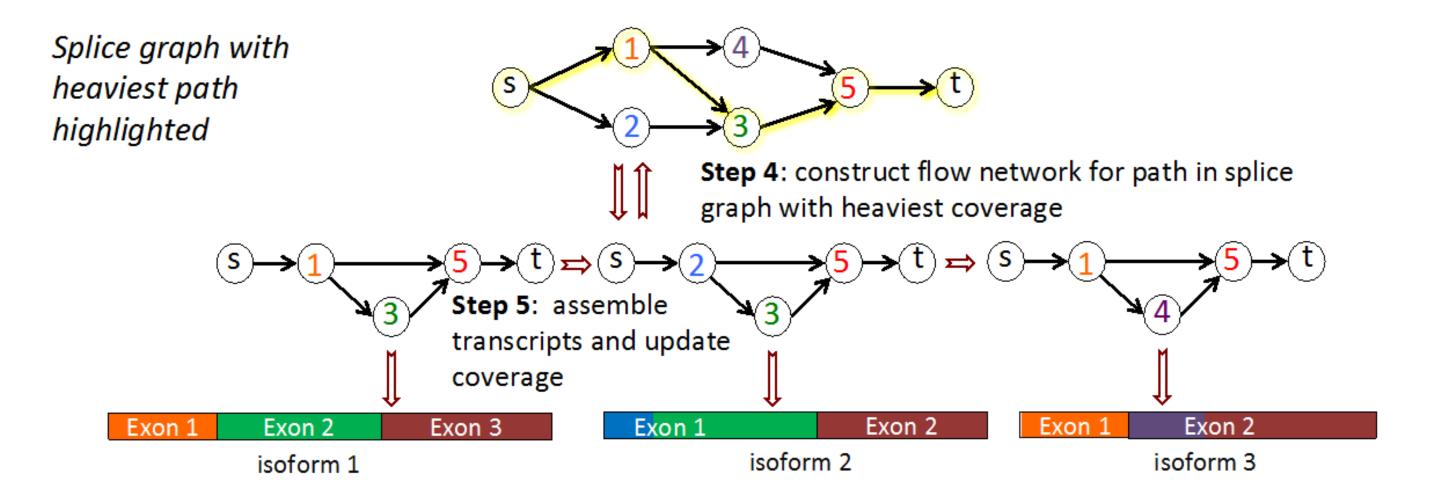
Choosing a Heaviest Path

StringTie chooses the heaviest path greedily, as follows (this is an O(n) algorithm):

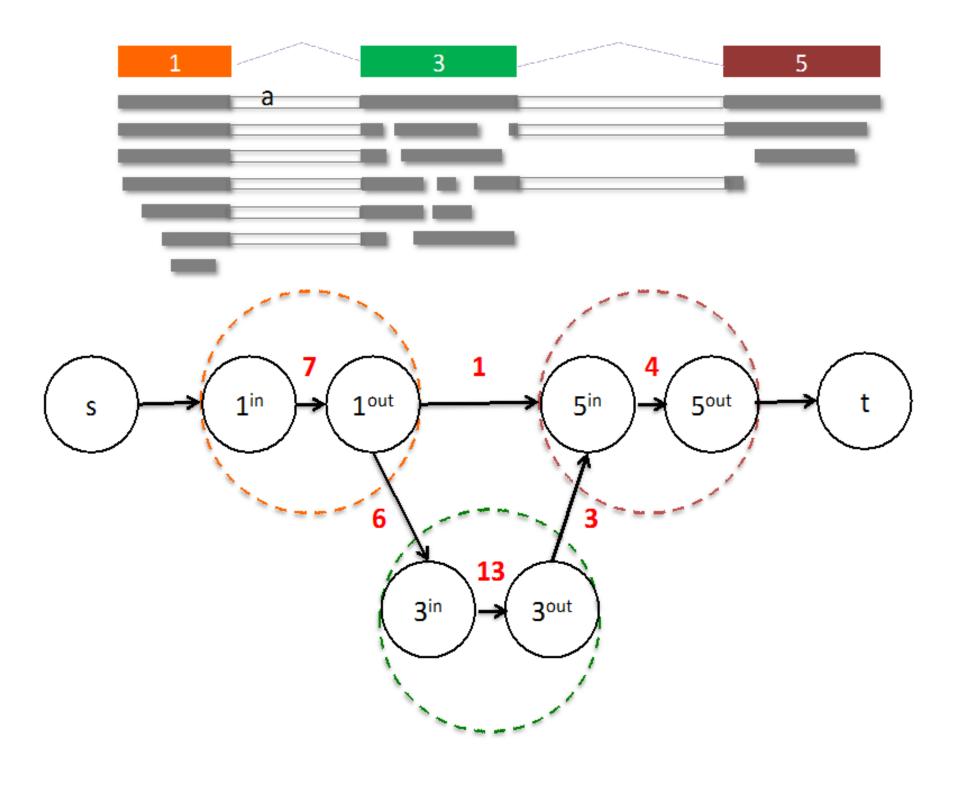
Pick the ASG node with the highest per-base read coverage.

Extend nodes to the **source** by adding to the path the adjacent node with the largest # of compatible read fragments.

Extend nodes to the **sink** by adding to the path the adjacent node with the largest # of compatible read fragments.



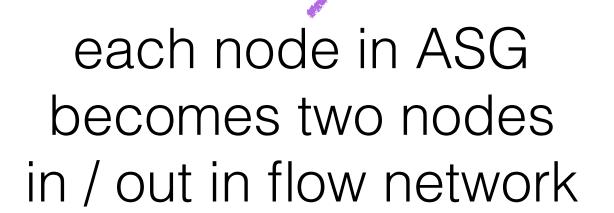
Note: The flow network is constructed separately for each selected transcript — the network on which the flow problem is solved does *not* correspond to the entire ASG!



Supplementary Figure 13. Flow network associated with a transcript (shown with colored nodes). 15 fragments (shown in grey) align to the transcript. Two nodes in the flow network are connected iff a fragment starts and ends at those nodes. E.g., nodes 1 and 5 are connected because fragment (a) starts at node 1 and ends at node 5. For each colored node in the transcript, two nodes are created in the flow network. Capacities on edges (not connecting source or sink) are shown in red.

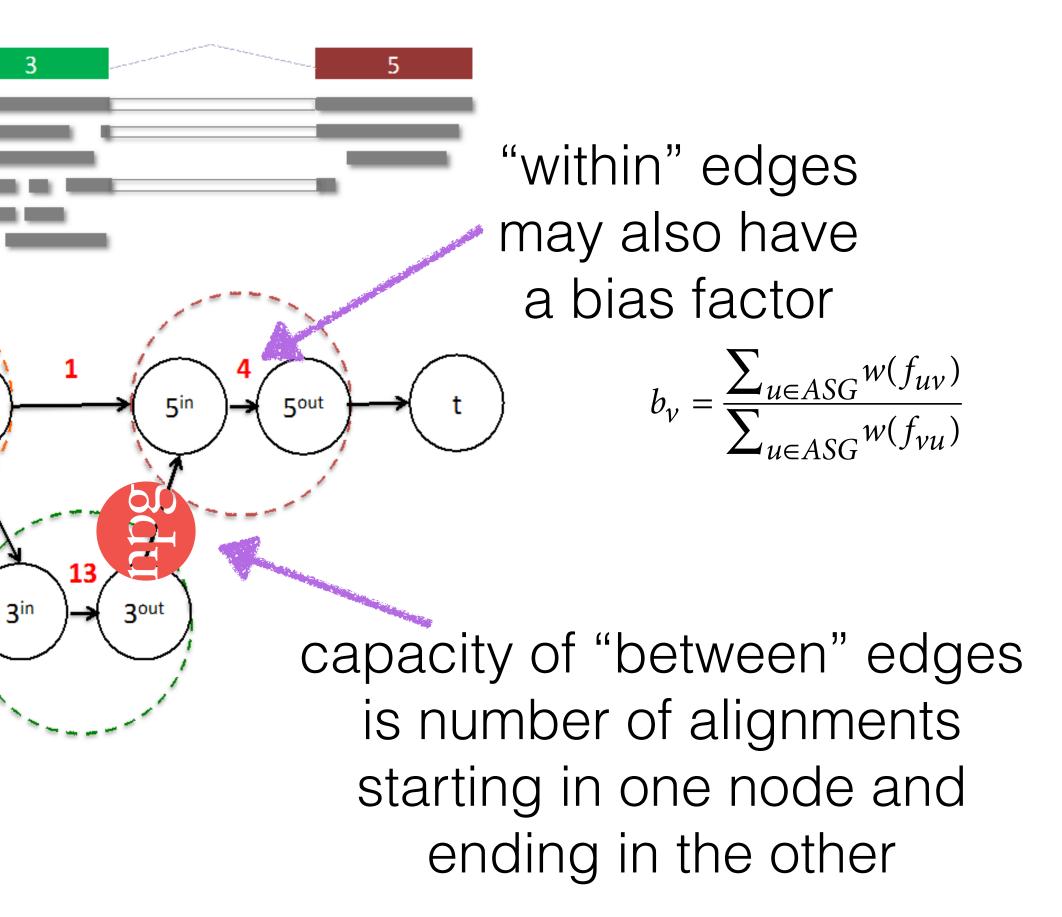
Pertea, Mihaela, et al. "StringTie enables improved reconstruction of a transcriptome from RNA-seq reads." Nature biotechnology 33.3 (2015): 290.

1 out



Supplementary Figure 13. Flow network associated with a transcript (shown with colored nodes). 15 fragments (shown in grey) align to the transcript. Two nodes in the flow network are connected iff a fragment starts and ends at those nodes. E.g., nodes 1 and 5 are connected because fragment (a) starts at node 1 and ends at node 5. For each colored node in the transcript, two nodes are created in the flow network. Capacities on edges (not connecting source or sink) are shown in red.

Pertea, Mihaela, et al. "StringTie enables improved reconstruction of a transcriptome from RNA-seq reads." *Nature biotechnology* 33.3 (2015): 290.



Given the flow network, StringTie solves a *generalized* max-flow problem

generalized — edges may have multipliers (bias factors), so flow may be gained or lost as it is sent through the network.

$$N = (G, s, t, c), \text{ where } G = (V, E), \text{ with } E \subseteq V \times V$$

$$s \in V^{f} \text{ and } T \in \mathbb{R}^{V}$$

$$c \stackrel{f}{f} \stackrel{E}{E} \xrightarrow{R} \mathbb{R}^{R}^{+}$$

$$f : E \rightarrow \mathbb{R}^{+}$$

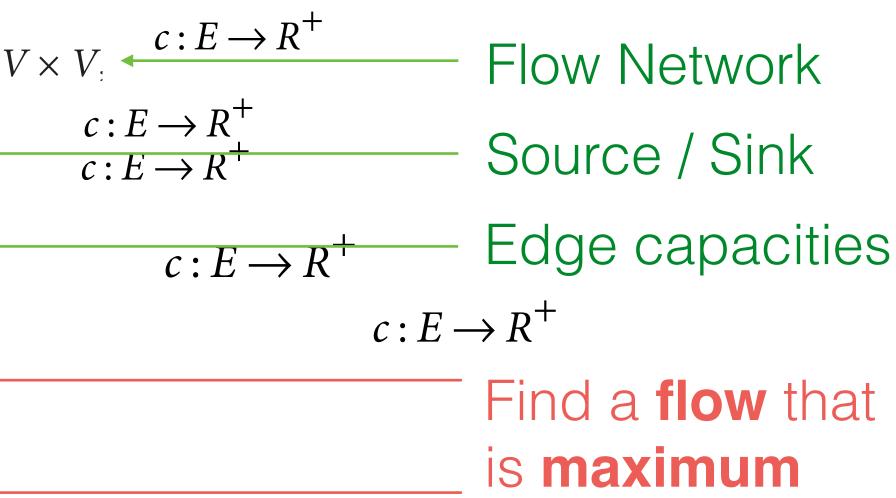
$$f : E \rightarrow \mathbb{R}^{+}$$

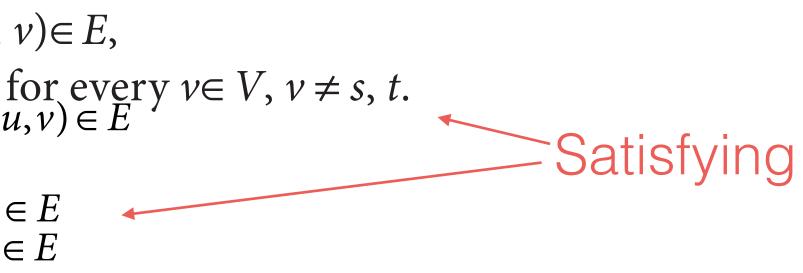
$$||f|| = \Sigma_{(v, t) \in E} f((v, t))$$

$$(1) \quad 0 \leq f((u, v)) \leq c \quad ((u, v)), \text{ for every } (u, v) \in (2) \quad \sum_{(u, v) \in E} f(((u, v))) = \sum_{(v, u) \in E} f((v, u)), \text{ for every } (u, v)$$

$$l_{(u, v)} \leq f(((u, v))) \leq c(((u, v))), \text{ for every } (u, v) \in E$$

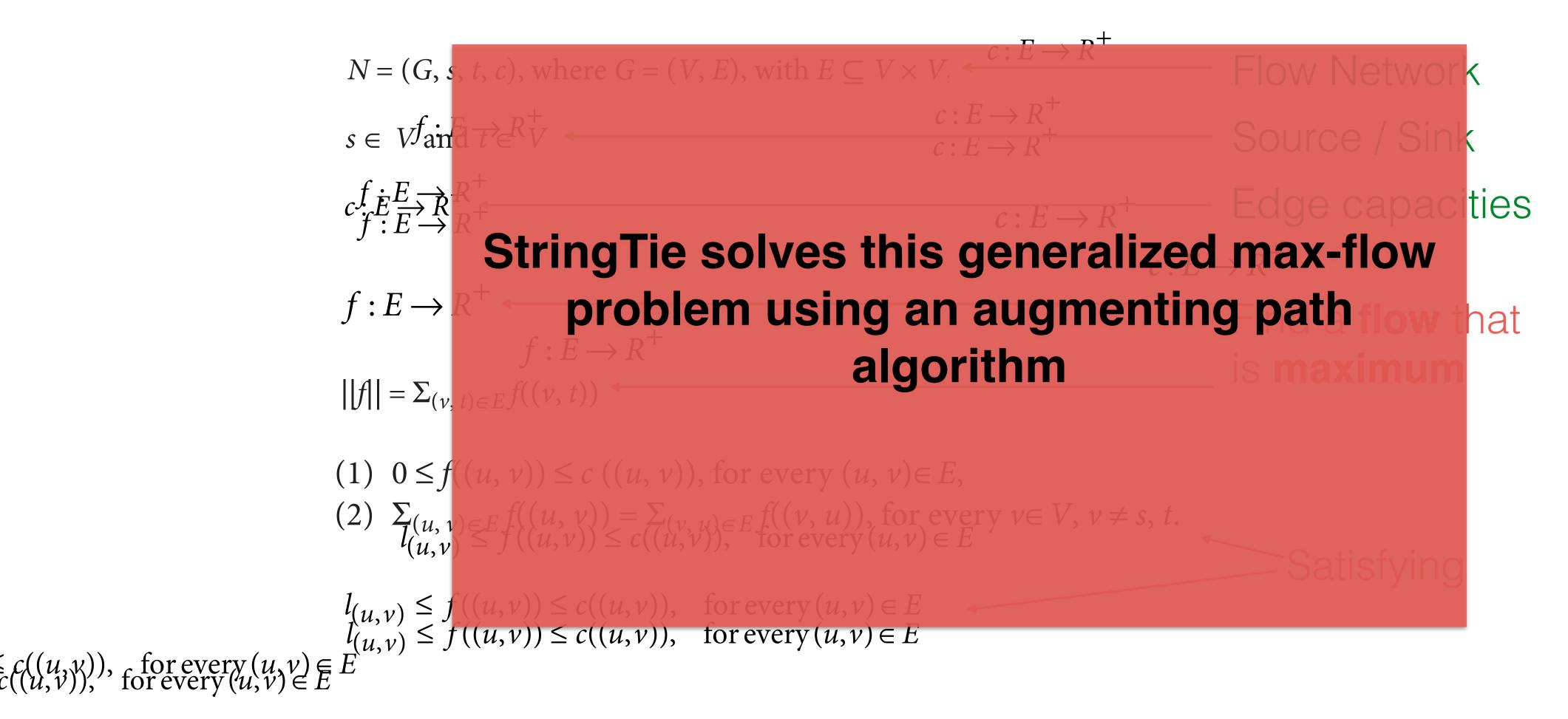
$$l_{(u, v)} \leq f(((u, v))) \leq c(((u, v))), \text{ for every } (u, v) \in E$$





Constructing the Flow Network

generalized — edges may have multipliers (bias factors), so flow may be gained or lost as it is sent through the network.



Given the flow network, StringTie solves a *generalized* max-flow problem

Flow network: G = (V, E, s, t, c)

Find a flow $f : E \rightarrow R^+$ of maximum value

Subject to: (1) Capacity : $0 \le f(e) \le c_e$ for all $e \in E$

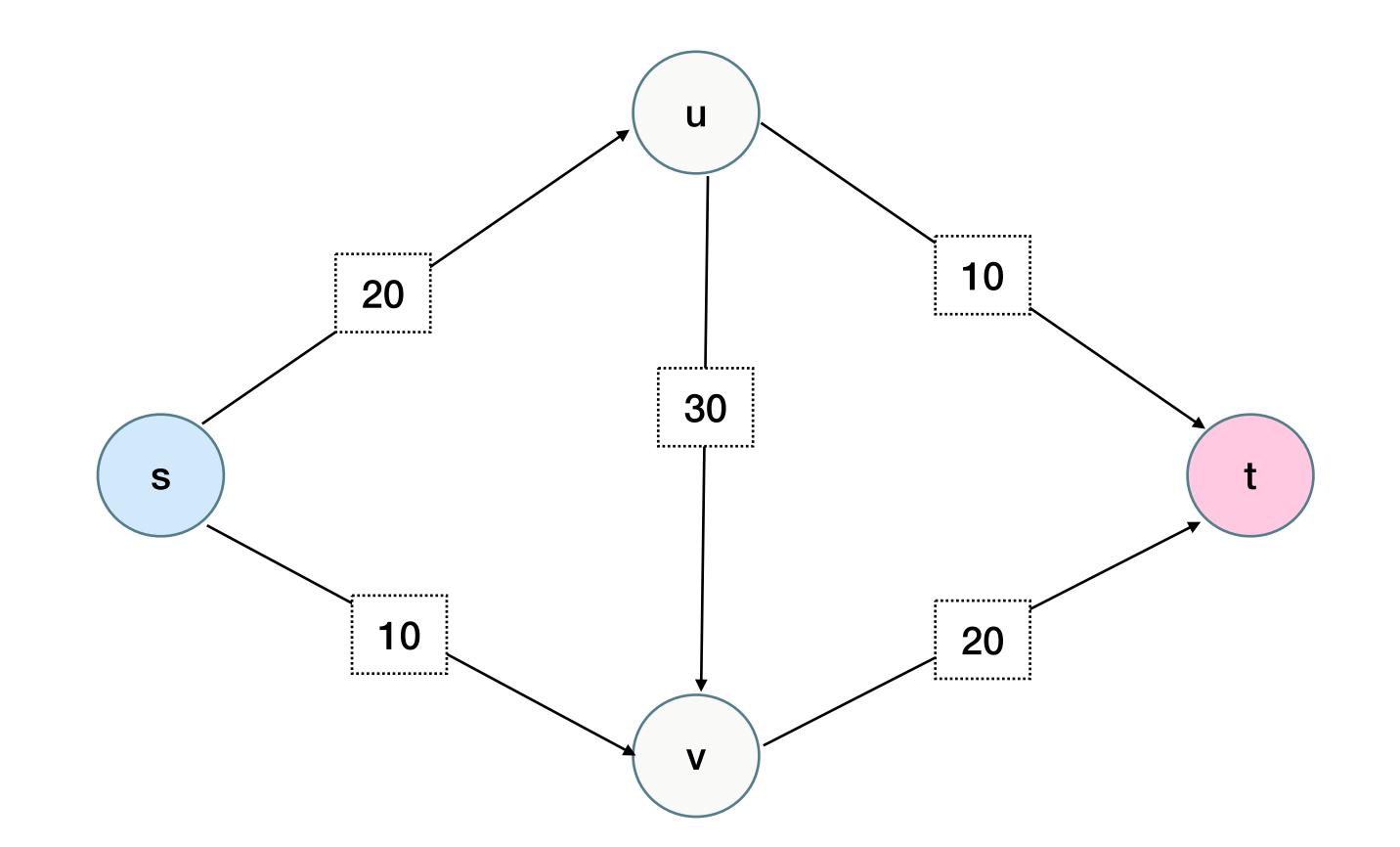
Value of the flow is given by:

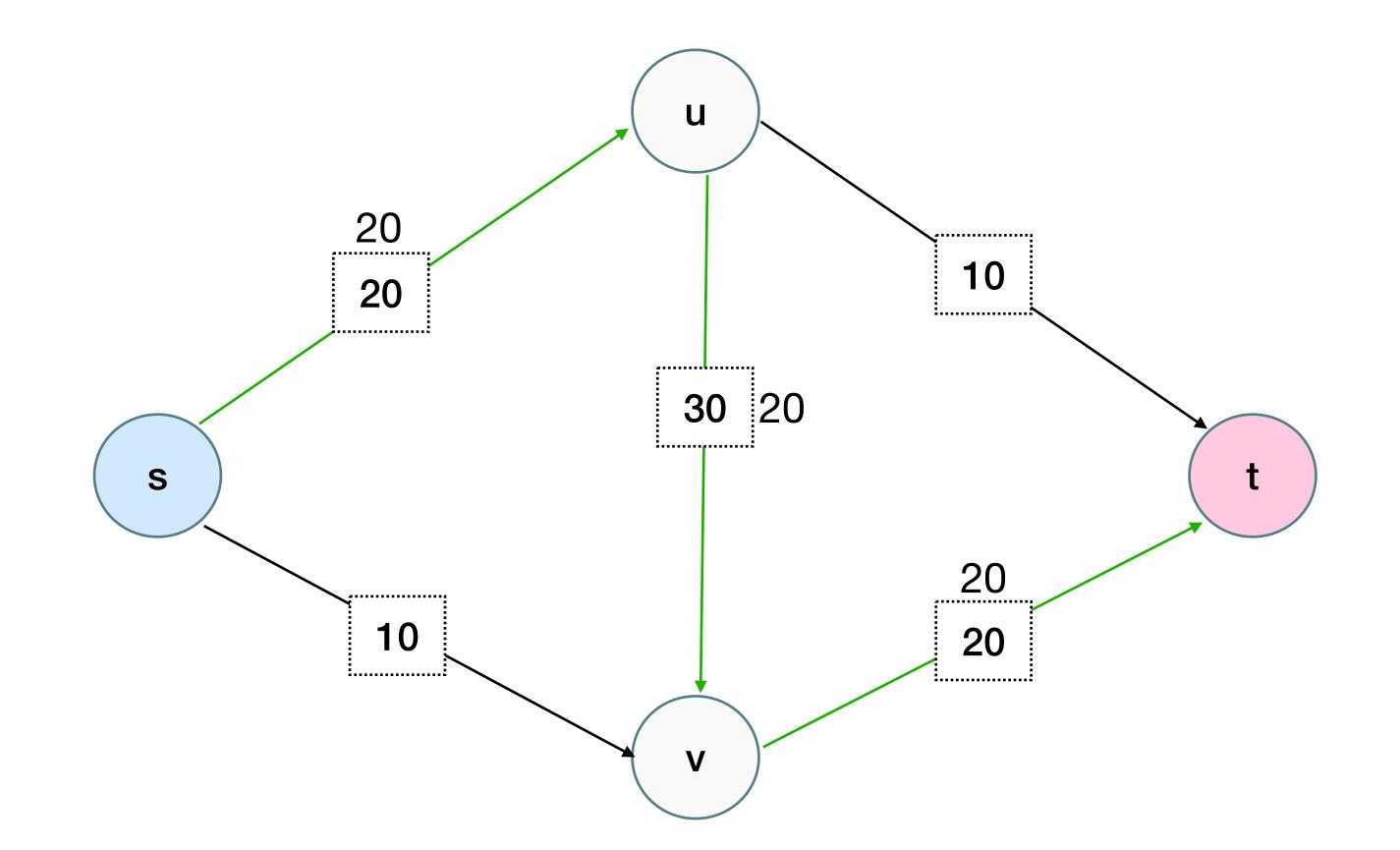
The below slides follow 7.1 in Kleinberg & Tardos

- Recall: Max Flow

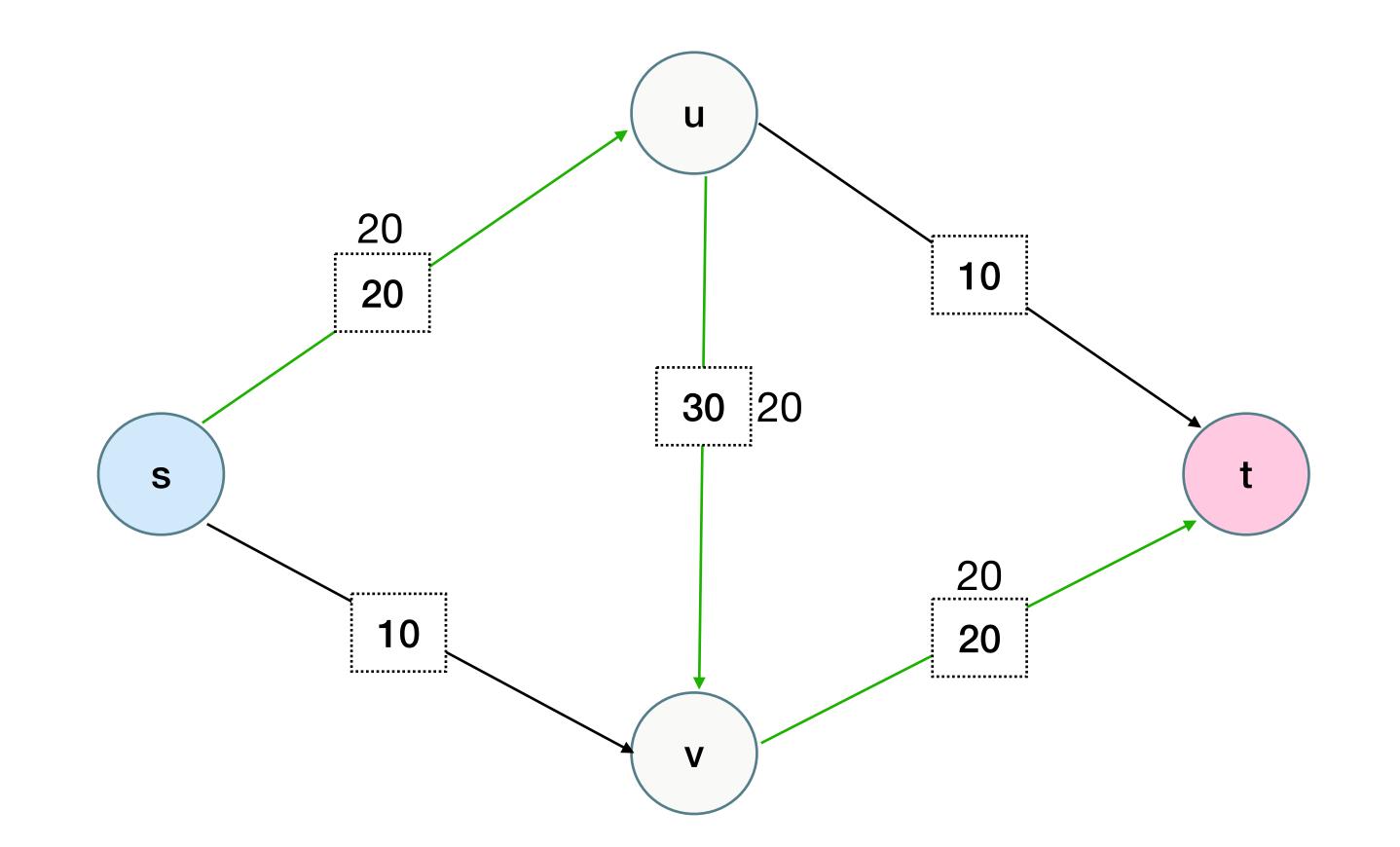
- (2) Conservation : For every $v \in V$ (apart from s and t) $\sum f(e) = \sum f(e')$ *e* into v *e'* out of v

 - $v(f) = \sum_{e \text{ out of } s} f(e)$

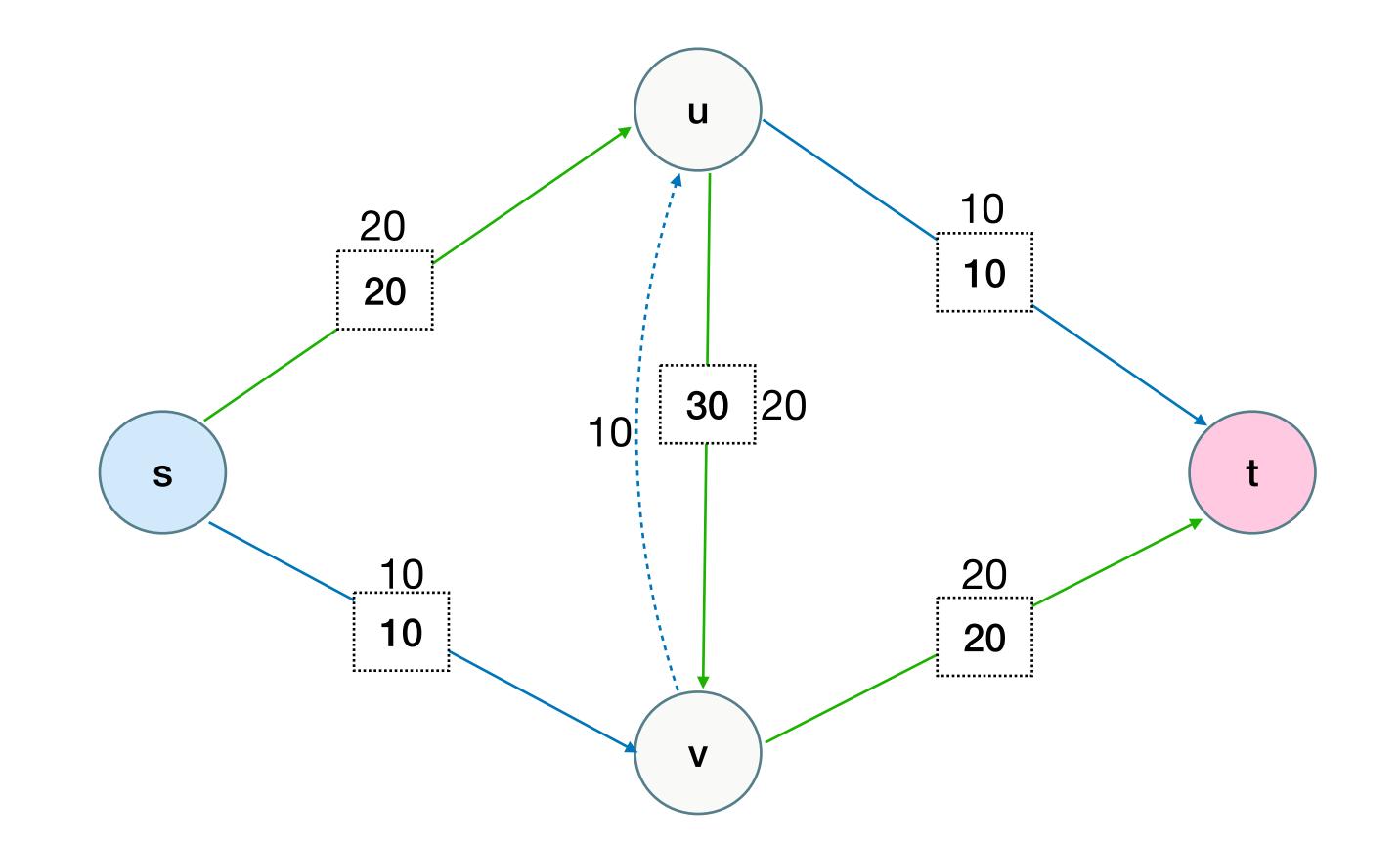




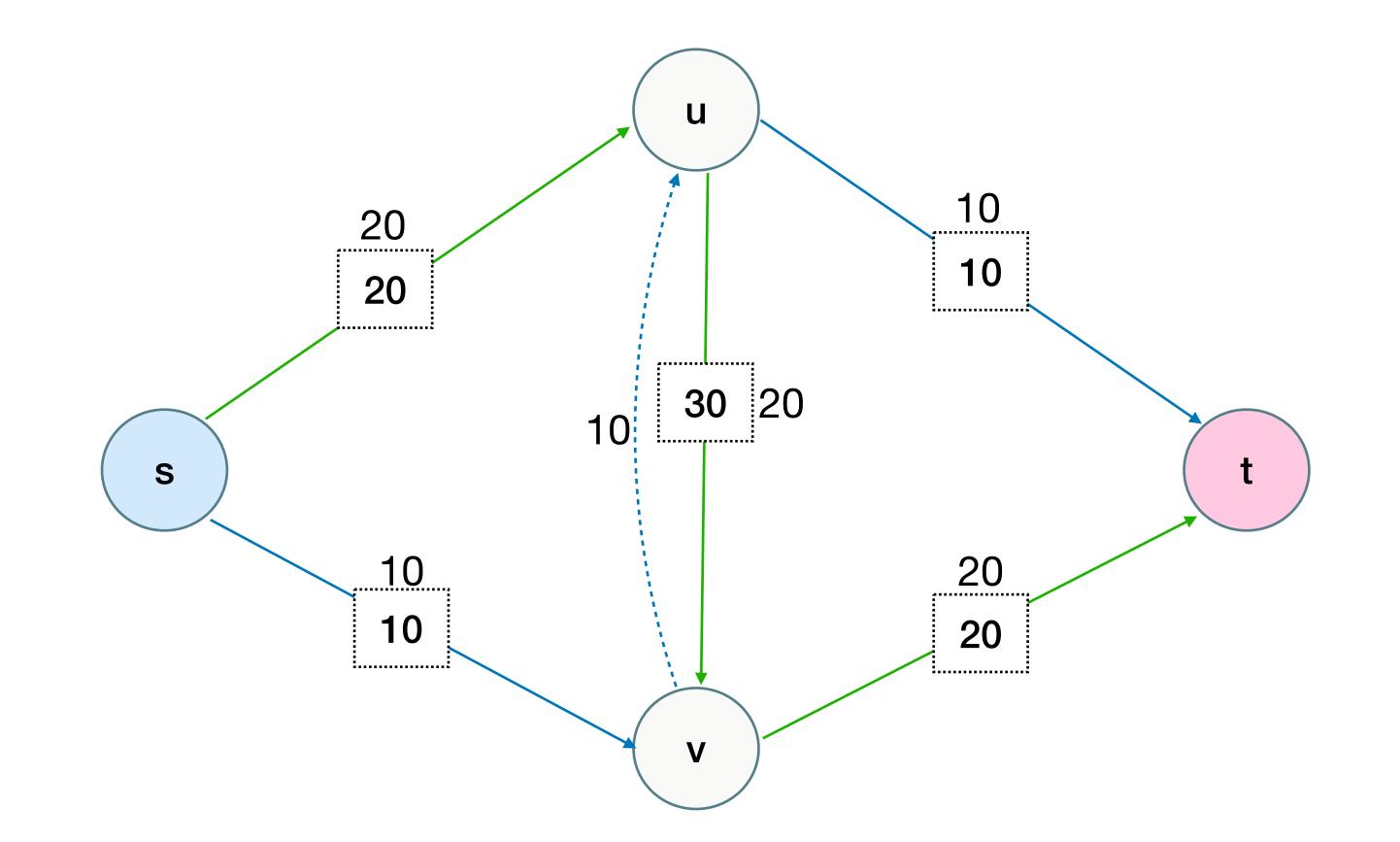
This achieves a flow of value 20, which respects (1) and (2). Is it maximum?



This achieves a flow of value 20, which respects (1) and (2). Is it maximum? No, but now we are "stuck" by the edges we chose. What if we could "undo" some of the flow?



This achieves a flow of value 20, which respects (1) and (2). Is it maximum? No, but now we are "stuck" by the edges we chose. What if we could "undo" some of the flow?



The "dotted" line here is a "backward" edge — it doesn't exist in the original graph. But flows realized using such residual edges can always be realized in the original graph by changing the forward flows. This leads to the formal idea of the residual graph.

If G is a flow network with a valid flow f, then the residual

Graph G_f:

Has the same node set as G

e=(u,v) with capacity given by $c_e - f(e)$.

for each e = (u,v) in G where f(e) > 0, G_f has an edge

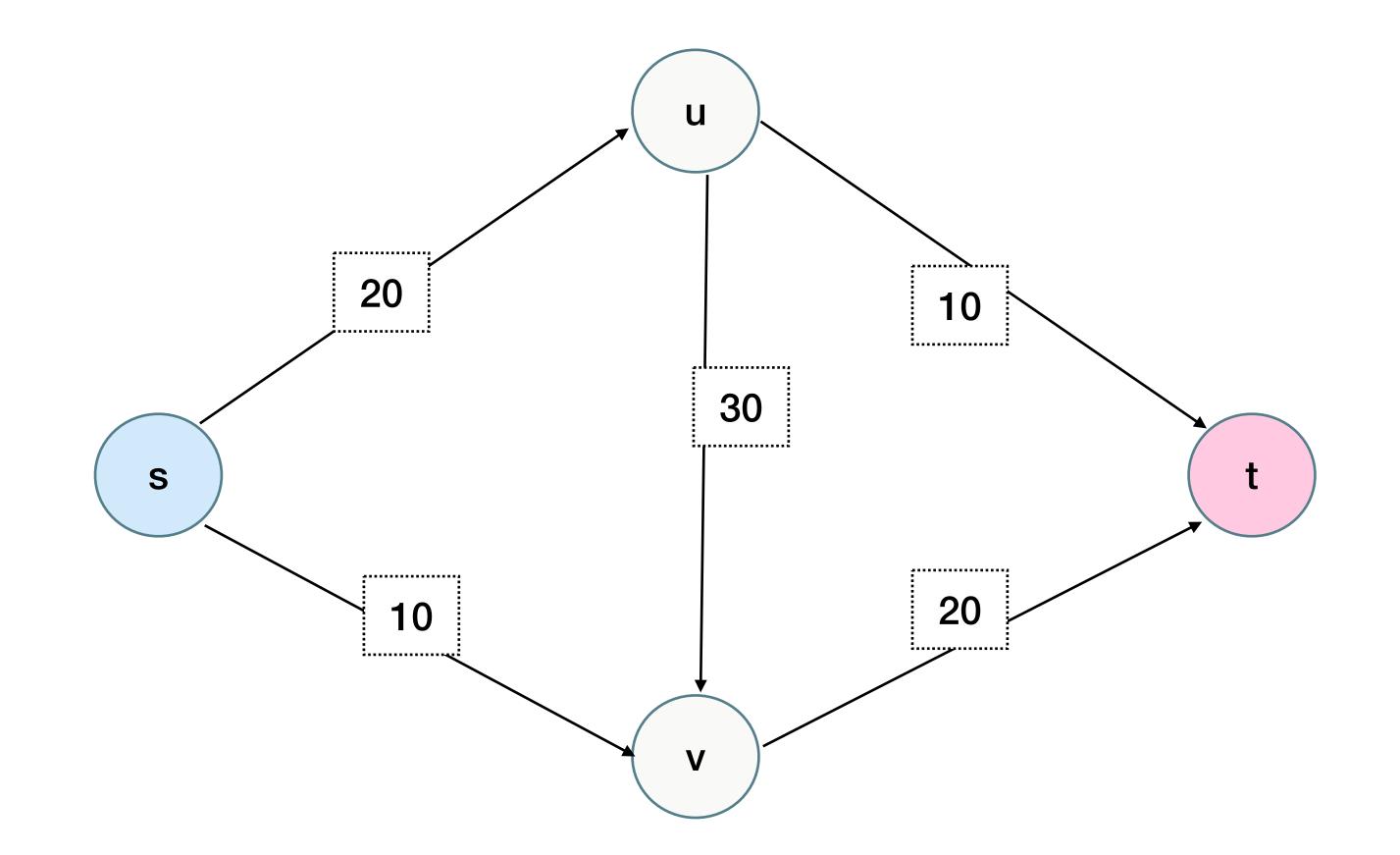
- for each e = (u,v) in G where $f(e) < c_e$, G_f has an edge
- e'=(v,u) with capacity f(e) these are "backward edges"

Let **bottleneck**(P,f) for a simple s-t path P with flow f be the minimum residual capacity of any edge on P. We define the following subroutine:

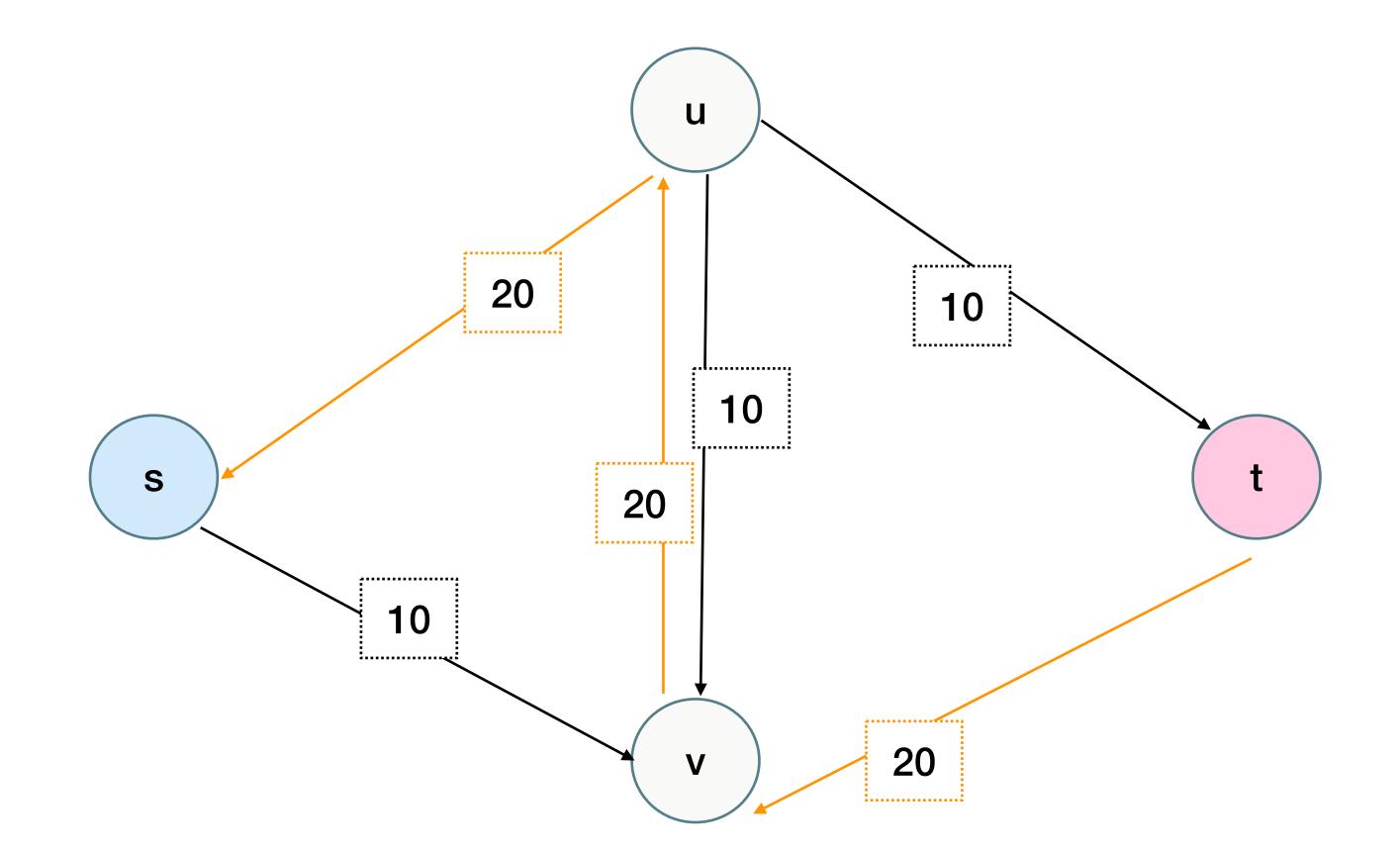
```
augment(f,P)
  let b = bottleneck(P,f)
  for e = (u,v) in P
    if e = (u,v) is forward
        increase f(e) in G by b
    else (u,v) is backward let e = (v,u)
        decrease f(e) in G by b
    endif
    endfor
    return f
```

We can then find a maximum flow as follows

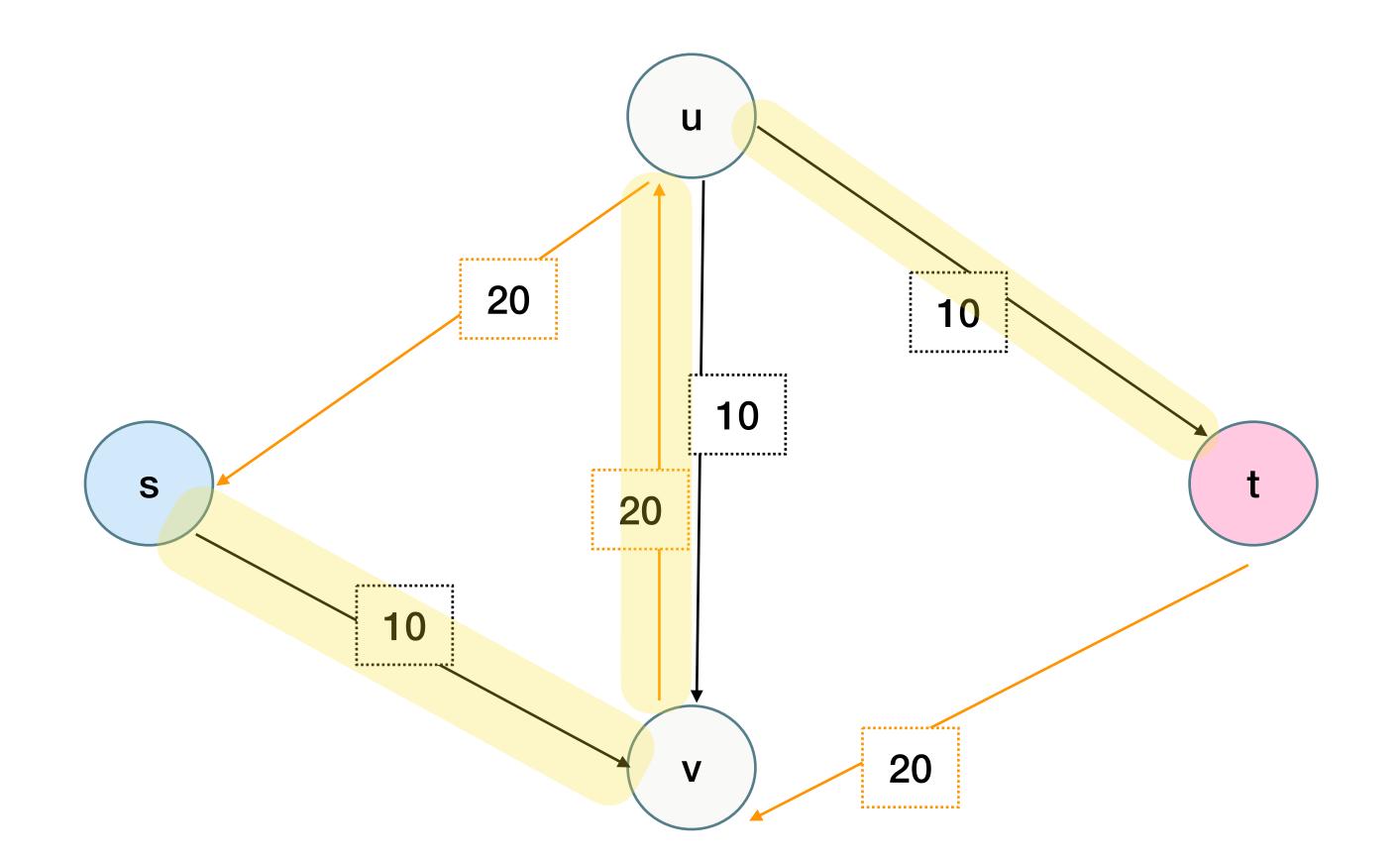
```
all e in G
n s-t path in G<sub>f</sub>
ole s-t path in G<sub>f</sub>
, P)
```



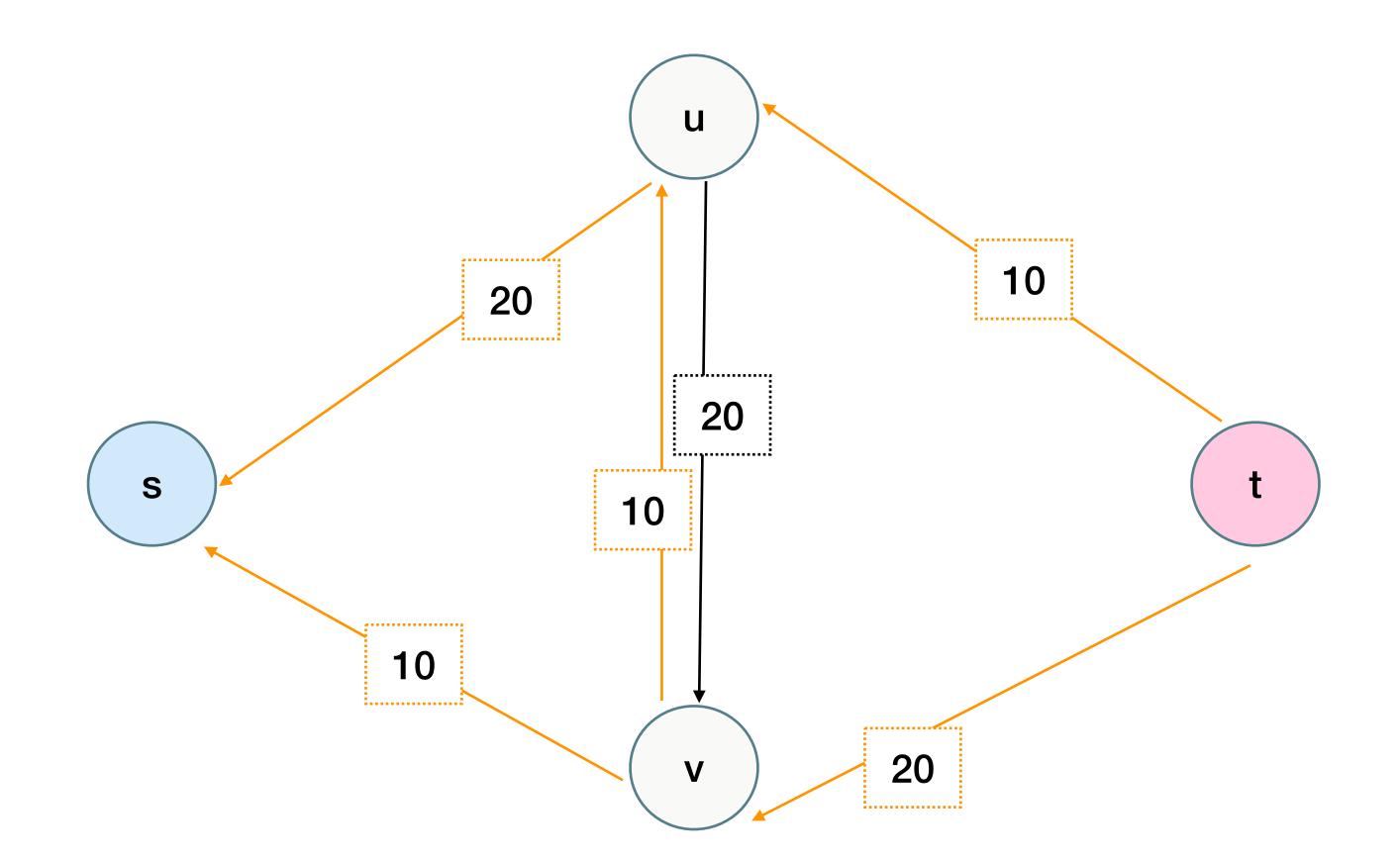
Initially, flow is 0, and $G_f = G$



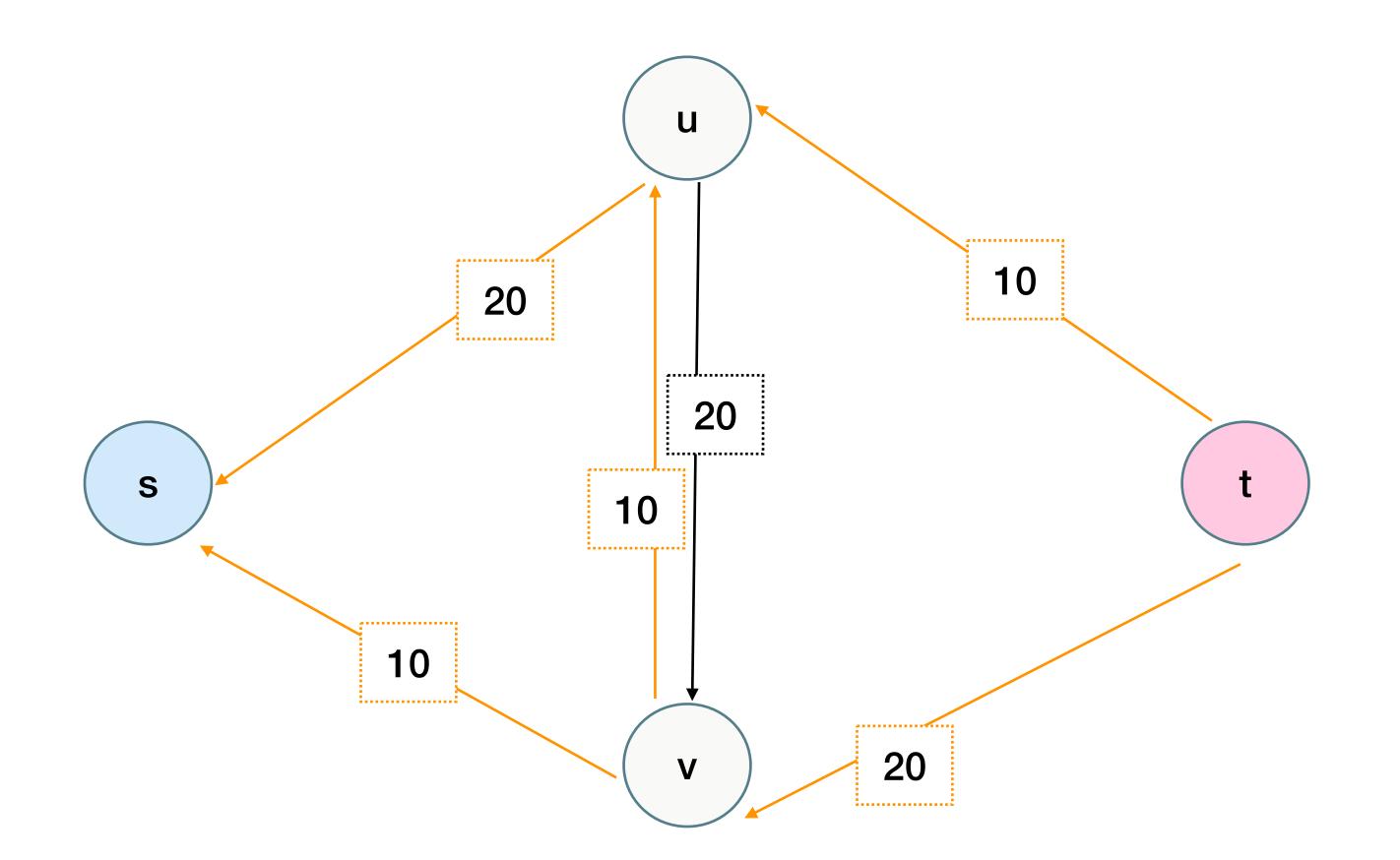
S -> u -> v -> t is chosen, and we push 20 units across it We update G_f



S -> v -> u -> t is chosen, and we push 10 units across it



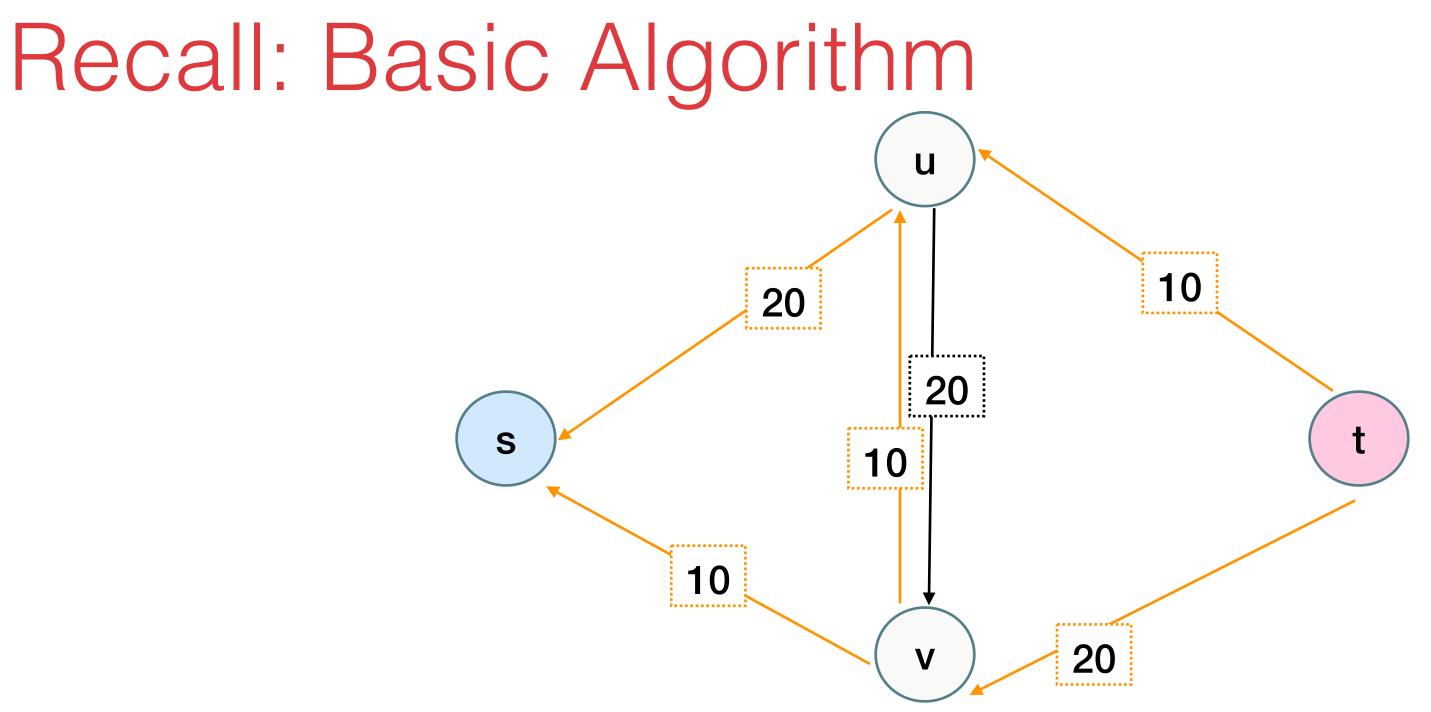
S -> v -> u -> t is chosen, and we push 10 units across it We update G_f



No more s-t paths in the residual graph. Algorithm terminates with v(f) = 30 (the maximum).

One can reduce Max Flow with minimum bounds to Max Flow

One can also add gain / loss as is necessary in StringTie



- This is the basic Ford-Fulkerson algorithm. Running time is O(mC)
- Strongly-polynomial algorithms exist (e.g. Dinitz-Edmonds-Karp O(nm²))

Bias-aware MaxFlow algorithm

Max-flow procedure

Input: flow network with sink, source, multipliers (b_v as defined in Methods), and capacities on the edges **Output:** maximum flow flow_{max}

```
Initialization: set flow<sub>max</sub>=0
               for all edges (u,v) in network
                     flow<sub>uv</sub>=0
               end for
```

```
while there is an augmenting path p^2 in network
     set u to sink (the last node in p)
     bias(u) = 1
     increment = ∞
     while there is predecessor v of node u in p
           increment = min(increment, capacity<sub>vu</sub> - bias(u) *flow<sub>vu</sub>)
           if there is a predecessor w of v in p
                if v comes before u in the ASG
                      if w comes before v in the ASG
                           bias(v) = bias(u) * b_v
                      else bias(v)=bias(u)
                      end if
                else if w comes before v in the ASG
                           bias(v)=bias(u)
                      else bias (v) = bias (u) / b_v
                      end if
                end if
           end if
           u = v
     end while
     for all consecutive nodes u, v (u before v) in p
           flow<sub>uv</sub> += increment/bias(u)
           flowvu -= increment/bias(u)
     end for
     flow<sub>max</sub> += increment
```

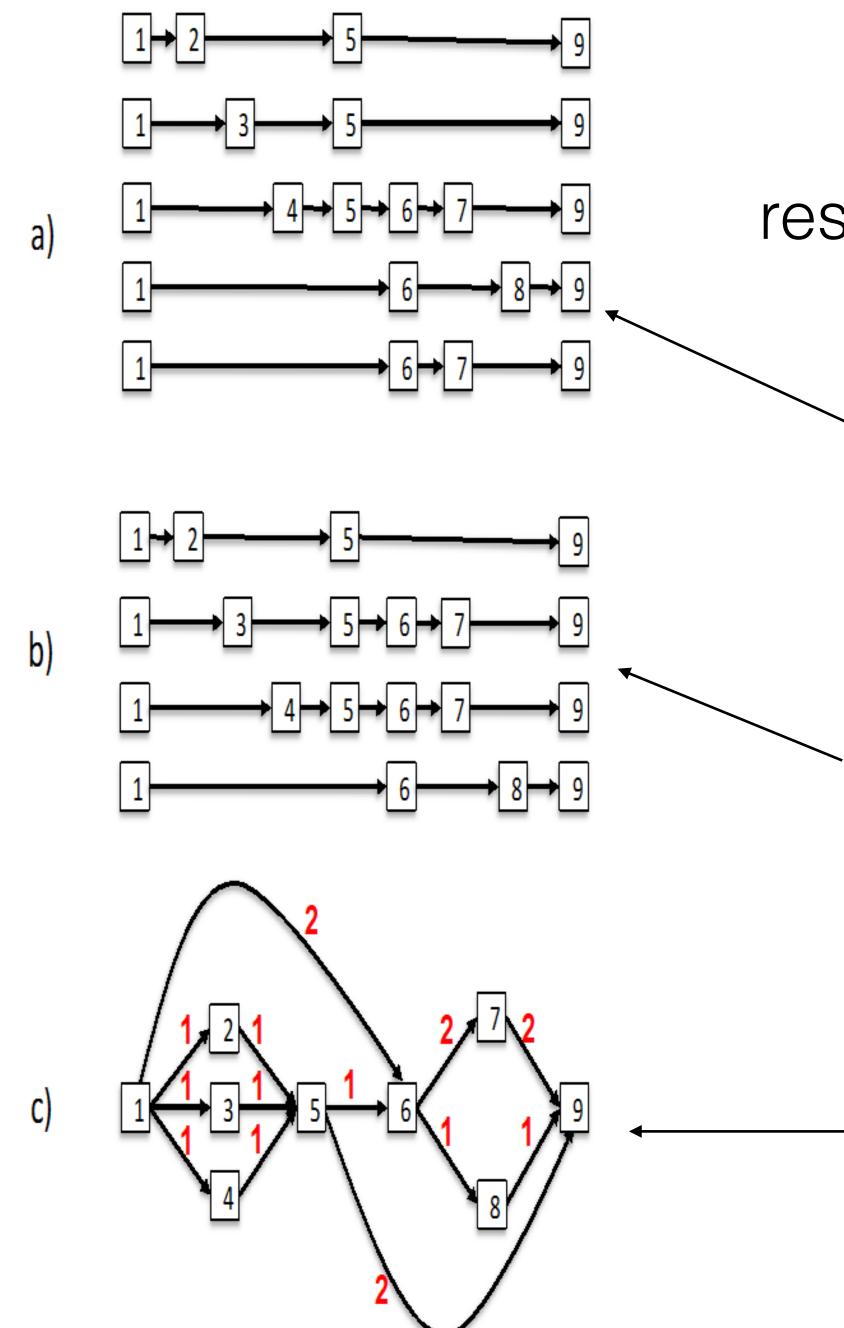
Processing the Splice Graph

Repeat:

- 1. Heuristically choose a "heavy" path (a path) with the heaviest node) in the ASG
- 2. Estimate path expression by computing maxflow in a flow graph corresponding to this subpath of the ASG. Subtract the read mass assigned to the nodes in this path & repeat.
- Until: Coverage of heaviest path falls below 2.5 reads per-base

the selected path.

Interestingly: Unlike other approaches that try to use the flow graph to *find* and *quantify* the paths, StringTie uses a heuristic to select the transcript, and flow only to quantify



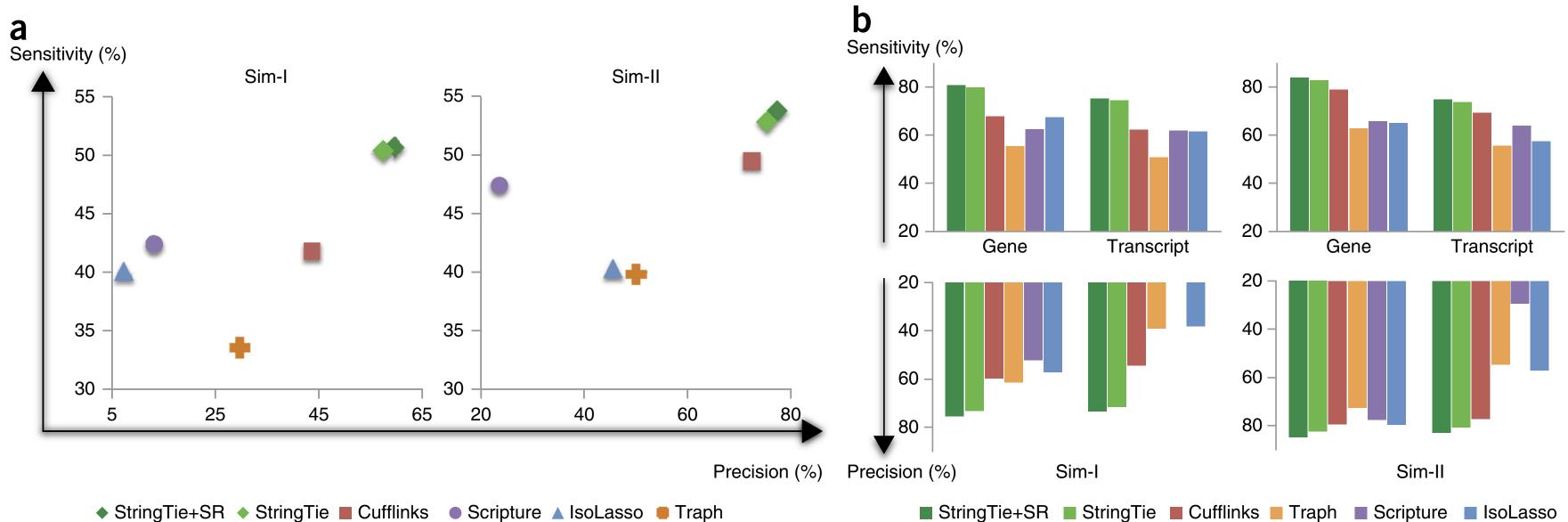
Pertea, Mihaela, et al. "StringTie enables improved reconstruction of a transcriptome from RNA-seq reads." Nature biotechnology 33.3 (2015): 290.

Illustration of how coverage information yields different results from Cufflinks' "parsimony" approach

> transcripts extracted if we consider coverage

parsimonious set of "covering" transcripts





◆ StringTie+SR ◆ StringTie ■ Cufflinks ● Scripture ▲ IsoLasso ■ Traph

Figure 2 Transcriptome assemblers' accuracies in detecting expressed transcripts from two simulated RNA-seq data sets. (a) Transcriptome assemblers' accuracies in detecting expressed transcripts from two simulated RNA-seq data sets. In data set Sim-I (left), the fragment sizes follow an empirical distribution based on Illumina sequences, and in Sim-II (right) the fragment sizes follow a parameterized normal distribution. StringTie+SR preassembles the reads into super-reads when possible. (b) Accuracy of transcriptome assemblers on gene loci from the same two data sets, considering only those transcripts that were completely covered by input reads. Scripture's precision on Sim-I was 17.7%, below the 20% minimum shown here.

Results

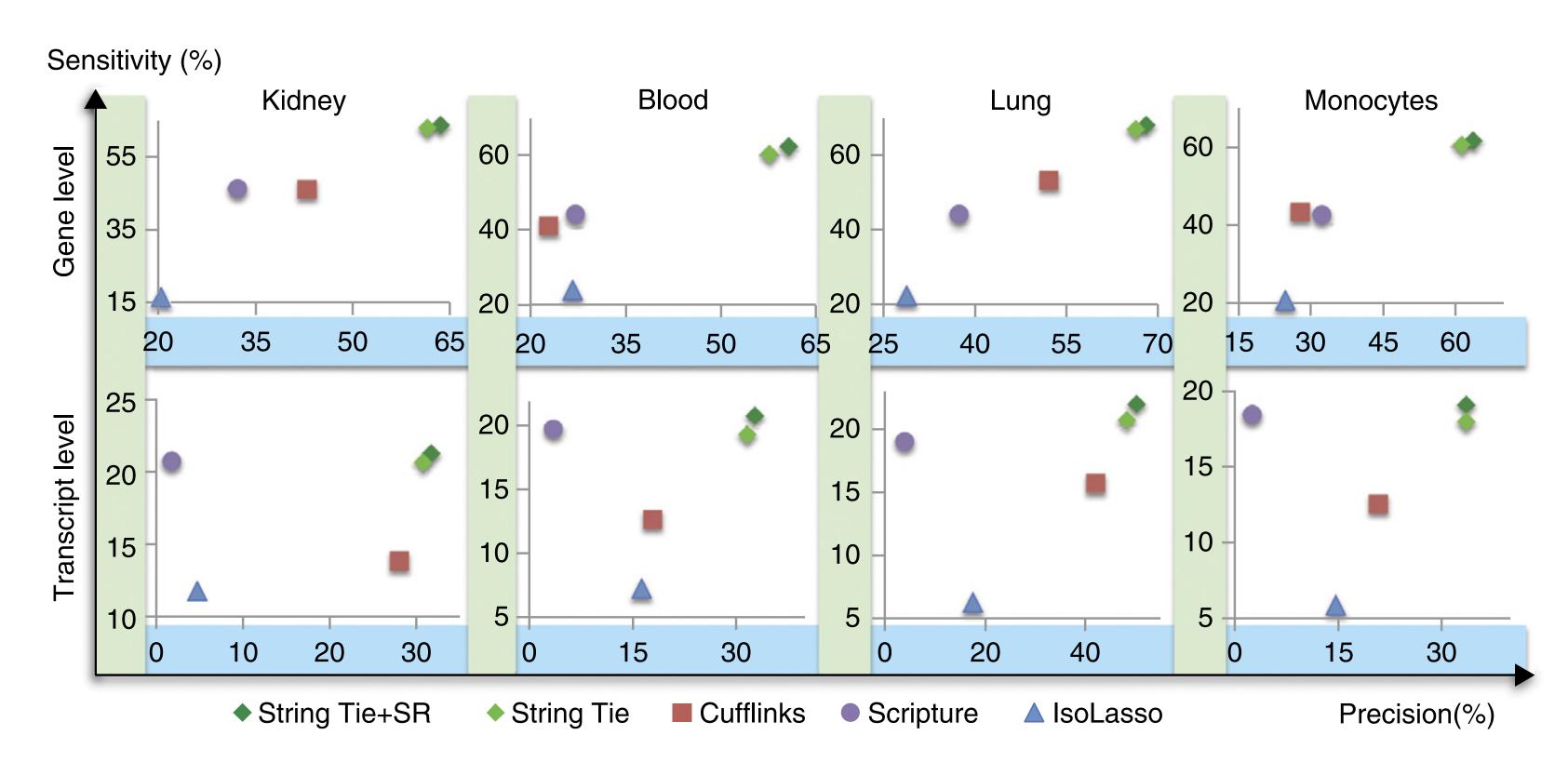


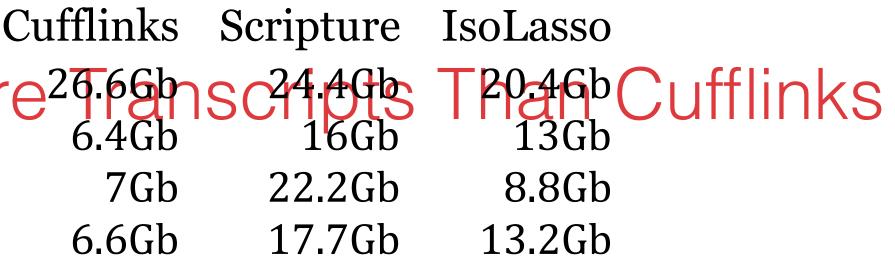
Figure 3 Accuracy of transcript assemblers at assembling known genes, measured on real data sets from four different tissues. Known genes are defined as those annotated in either the RefSeq, UCSC or Ensembl human gene databases. Gene level sensitivity (y axis) measures the percentage of genes for which a program got at least one isoform correct, whereas transcript sensitivity measures the percentage of known transcripts that were correctly assembled. Precision (x axis) is measured as the percentage of all predicted genes (transcripts) that match an annotated gene (transcript).

Results

Strin	gTie+SR	StringTie	(
KidneyringTie Blood	1176	fies126b	r
Blood	4.7Gb	4.3Gb	
Lung	6.9Gb	6.4Gb	
Monocytes	1.6Gb	1.8Gb	

Supplementary Table 11. Symmetric differences between StringTie and Cufflinks on four real data sets. For each data set, the table shows the number of transcripts identified correctly by StringTie but missed by Cufflinks, the number identified by Cufflinks but missed by StringTie, and the number identified correctly by both programs.

Data set	Unique to StringTie	Unique to Cufflinks	Common to both
Kidney	6652	2177	7068
Blood	5834	2031	5156
Lung	5272	1937	8434
Monocytes	5296	2050	5452

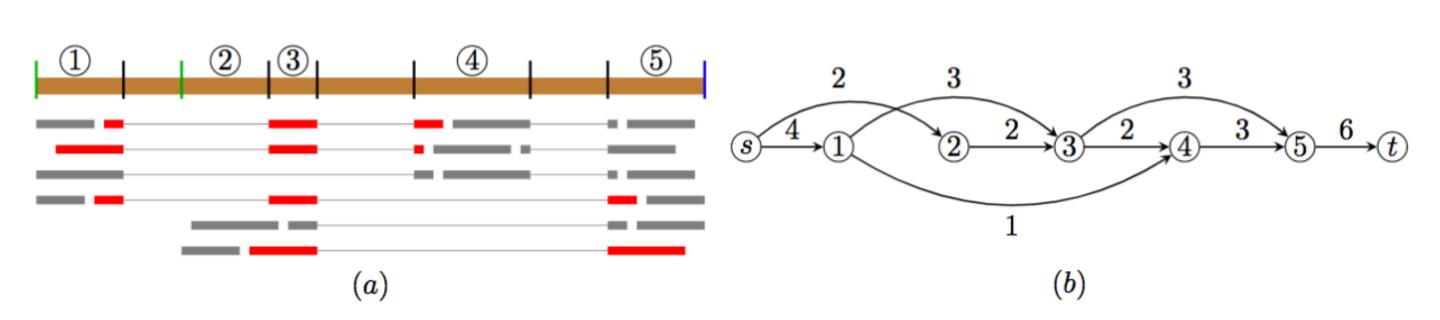


Scallop improves assembly by preserving "phasing paths"

nature biotechnology

Mingfu Shao & Carl Kingsford

Accurate assembly of transcripts through phase-preserving graph decomposition



Supplementary Figure 1: Example of building splice graph and phasing paths. (a) Alignment of reads to the reference genome. Inferred splice positions are marked with black bars; inferred starting and ending positions are marked with green and blue bars, respectively. Exons and partial exons are labeled with numbers above the reference genome. Reads that span more than two exons are colored red, from which we can get the set of phasing paths as $\{(1,3,4), (2,3,5), (1,3,5)\}$. The abundance of these phasing paths are g(1,3,4) = 2, g(2,3,5) = 1, and g(1,3,5) = 1. (b) The corresponding splice graph and weights for all edges.

Shao, Mingfu, and Carl Kingsford. "Accurate assembly of transcripts through phase-preserving graph decomposition." Nature biotechnology 35.12 (2017): 1167.

BRIEF COMMUNICATIONS

phasing paths = sub-paths of the splicing graph where read evidence supports >1 splicing junction.

Scallop preserves observed sub-paths.

Preserving "phasing paths" improves accuracy

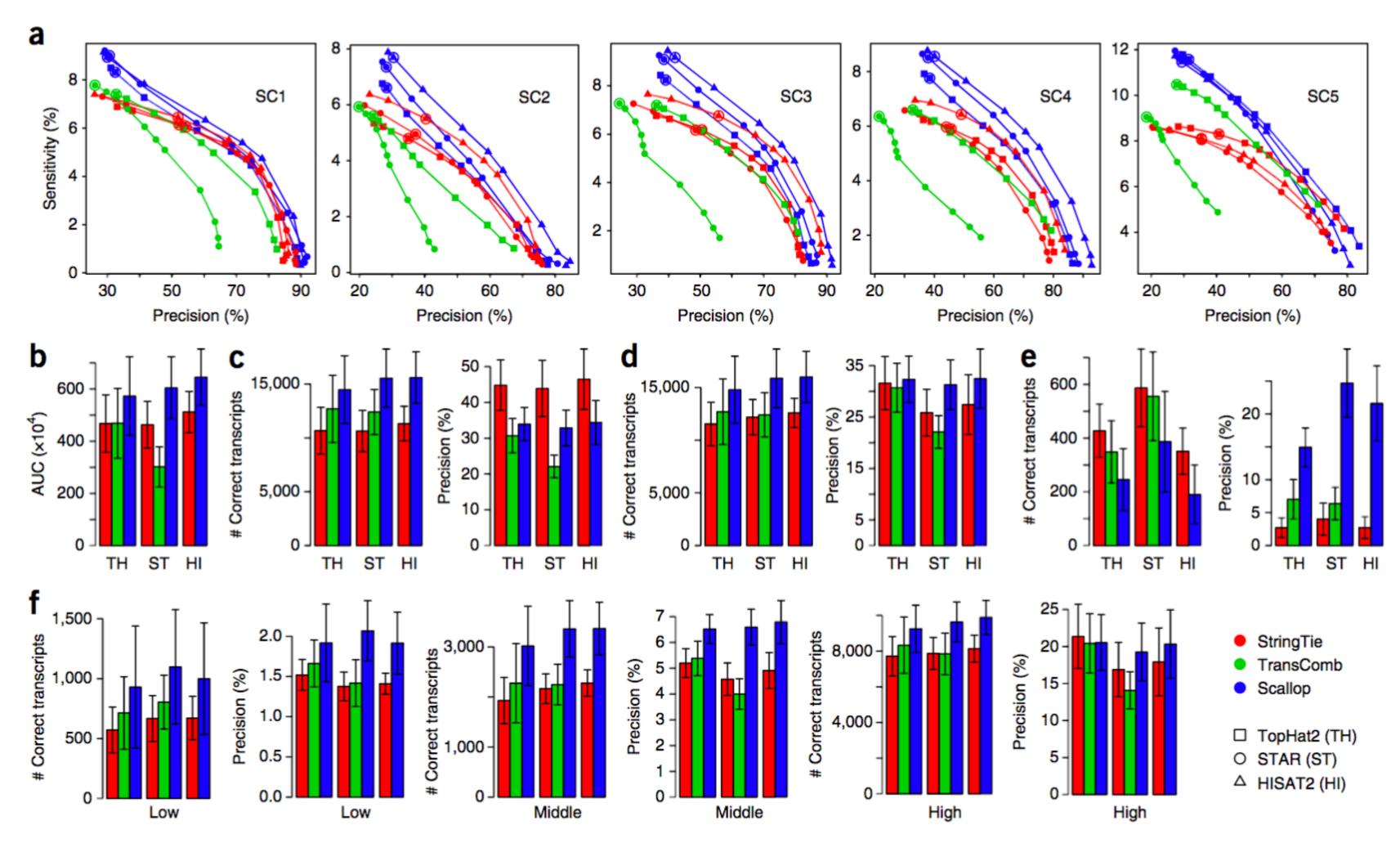


Figure 1 Comparison of the three methods (StringTie, TransComb, and Scallop) over the five testing samples. (a) The precision-sensitivity curves for multiexon transcripts. Each curve connects ten points, corresponding to minimum coverage thresholds {0, 1, 2.5, 5, 7.5, 10, 25, 50, 75, 100}; the default value is circled. (b) The average AUC (area under the precision-sensitivity curve) over the five samples. The error bars show the s.d. (the same for other panels). (c) The average sensitivity and precision of multi-exon transcripts running at default parameters. (d) The average sensitivity and precision of multi-exon transcripts running with minimum coverage set to 0. (e) The average sensitivity and precision of single-exon transcripts running at default parameters. (f) The average sensitivity and precision of multi-exon transcripts corresponding to low, middle, and high expression levels running with minimum coverage set to 0.

Shao, Mingfu, and Carl Kingsford. "Accurate assembly of transcripts through phase-preserving graph decomposition." *Nature biotechnology* 35.12 (2017): 1167.

Some other interesting assemblers

RESEARCH ARTICLE

Strawberry: Fast and accurate genomeguided transcript reconstruction and quantification from RNA-Seq

Ruolin Liu, Julie Dickerson*

METHOD

Bayesian transcriptome assembly

Lasse Maretty[†], Jonas Andreas Sibbesen[†] and Anders Krogh^{*}

Gene expression

Sparselso: a novel Bayesian approach to identify alternatively spliced isoforms from RNA-seq data

Xu Shi¹, Xiao Wang¹, Tian-Li Wang², Leena Hilakivi-Clarke³, Robert Clarke³ and Jianhua Xuan^{1,*}

Open Access

These methods, in particular, solve identification and quantification simultaneously.

Conceptually, this seems like the strongest approach given how related the problems are.